

Implication of Advanced Vogel Approximation Method

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Abstract: The study in this paper is to discuss about advanced Vogel approximation method (AVAM) which does not always give better feasible solution than Vogel's approximation method (VAM). As by V.K.Das, 'M.A.babu, A.R.Khan, and M.S.Uddin(2015) It is shown that AVAM is more effective than VAM and gives solution nearer to optimal solution more than VAM. In the end a counter example is given to prove my claim.

Keywords: AVAM, VAM, Feasible solution, optimal solution, transportation problem

1. Introduction

Transportation problem is special types of linear programming problem where the goal is to minimize the total transportation cost. In general, it is concerned with distributing any single commodity from any group of supply centre, called sources, to any group of receiving centre, called destination. All destinations can receive its demand from one or more sources. Each sources has a fixed supply of unites, where the entire supply must be distributed to the destination. Similarly, each destination has fixed demand of units, where the entire demand must be received from the sources.

The liner programming problem of a transportation model is given below;

$$\begin{aligned} \text{Minimize: } & \sum_{i=1}^m \sum_{j=1}^n c_{ij} x_{ij} \\ \text{subject to: } & \\ & \sum_{j=1}^n x_{ij} \leq s_i, \text{ for } i = 1, 2, 3, \dots, m \\ & \sum_{i=1}^m x_{ij} \geq d_j, \text{ for } j = 1, 2, 3, \dots, n \\ & x_{ij} \geq 0, \text{ for all } i, j \end{aligned}$$

$I=1,2,\dots,m$ is the set of origins

$J=1,2,\dots,n$ is the set of destinations

X_{ij} =The quality transported from the i-th origin to the j-th destination

C_{ij} = Per unit cost in transporting goods from i-th origin to j-th destination

S_i =The amount available at the the i-th origin

D_j =The demand at the j-th destination

2. Numerical Example

Here counter example is given in which transportation problem is solved using AVAM and VAM. A mathematical model of a transportation problem is given below:

Table 1

Source	D1	D2	D3	D4	SUPPLY
S1	3	4	3	5	5
S2	7	6	4	6	6
S3	3	5	7	8	2
S4	5	4	9	5	6
DEMAND	4	6	2	7	19

SOLUTION of transportation problem using Vogel's approximation method (VAM):-

Table 2

Source	D1	D2	D3	D4	Supply
S1	2			3	5
		3	4	3	5
S2		7	6	4	6
S3	2				2
	3		5	7	8
S4		6			6
	5	4	9	5	
Demand	4	6	2	7	19

Total Transportation Cost =
 $2*3+3*5+2*4+4*6+2*3+6*4=83$

SOURCE	D1	D2	D3	D4	SUPPLY
S1	4			1	5
		3	4	3	5
S2		7	6	2	6
			4	4	6
S3		3	2		2
			5	7	8
S4			4		6
		5	4	2	5
DEMAND	4	6	2	7	19

Solution of example using Advanced Vogel's approximation method (AVAM):-

SOURCE	D1	D2	D3	D4	SUPPLY
S1	4			1	5
		3	4	3	5
S2		7	6	2	6
			4	4	6
S3		3	2		2
			5	7	8
S4			4		6
		5	4	2	5
DEMAND	4	6	2	7	19

Total transportation cost =
 $4*3+1*5+2*4+4*6+2*5+4*4+2*5=85$
 Optimal solution: The optimal solution determined BY
 MODI is 83

3. Result Analysis

In above example, we observed that feasible solution using AVAM has not better solution than VAM. the comparison table of the solution is given below:

Methods	Transportation problem
VAM	83
AVAM	85
Optimal solution	83

4. Conclusion

In this paper, we have find out that Vogel approximation method (VAM) does not always create computational error. Even it gives better solution than advanced Vogel approximation method (AVAM) in some cases.

References

- [1] HAMDY A. Taha operation research : an introduction ,eighth edition , ISBN-13: 9780132555937,
- [2] P.Rama Murthy operation research , second edition , ISBN(13) :978-81-224-29944-2
- [3] Hamdy taha TORA optimizing system software.
- [4] Hiller, f.s. and G.J. Lieberman 1995 introduction to operations research 6th Ed. New York ; McGraw- Hill ,inc
- [5] Nagraj balakrishnan, Tulane University. Modified Vogel's approximation method for the unbalanced transportation problem. appl.math.lett.vol.3, no2,pp.s11,1990
- [6] M.a hakim, an alternative method to find initial basic feasible solution of a transportation problem. annals of pure and applied mathematics ,vol .1,no2,2012.pp203-209,issn:2279-087x(p),2279-0888(online)
- [7] Ramakrishnan, g.s .an improvement to goyal, s modified VAM for the unbalanced transportation problem, journal of operational research society. 39(6)(1988)609-610
- [8] Aminur rahamn khan. a re-solution of the transportation problem : an algorithmic approach. Jahangirnagar university journal of science, vol 34.no2.pp.49-62ISSN1022-8894(2011)
- [9] Mathirajan , m. And.b meenakshi, experimental analysis of some variants of Vogel approximation method ,Asia pacific journal of operational research 21(4)(2004)447-462
- [10] Shimshak dg, J.A. kaslik and T.D. Barclay, a modification of Vogel approximation method through the use of heuristics, INEOR, 19(1981)259-263.
- [11] Refined, n.v and w.r. Vogel. Mathematical programming, prentice –hall, Englewood cliffs, New Jersey (1958).