

# Structural and Elastic Properties of $\text{Li}^+$ and $\text{W}^{6+}$ Metal Ions Doped With Sodium Borate Glass Using Pulser – Receiver Technique

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**Abstract:** Longitudinal, shear ultrasonic velocities and attenuation were measured in different compositions of the glass systems of  $20\text{Na}_2\text{O}-(80-x)\text{B}_2\text{O}_3-x\text{Li}_2\text{O}$  and  $20\text{Na}_2\text{O}-(80-x)\text{B}_2\text{O}_3-x\text{WO}_3$  (where  $x = 0$  to  $10$  in steps of  $2$  mol%) at room temperature by using Pulser - receiver technique at  $5$  MHz. The glass samples were prepared by conventional melt-quenching method. The amorphous nature of the samples was ascertained using X-ray diffractometry (XRD). The density of the glass samples were measured by relative measurement method. The measured experimental values are utilized to evaluate elastic moduli, Poisson's ratio, acoustic impedance, internal friction, microhardness, Debye temperature, and thermal expansion coefficient. Trends of the coordination number, cross-link density, mechanical and thermal stability for the systems are discussed in terms of the structural changes taking place due to variations in composition.

**Keywords:** Ultrasonic velocity, Attenuation, X-ray diffractometry, Elastic moduli, Microhardness.

## 1. Introduction

Elastic properties of solids are very significant, because their measurement gives information regarding the forces that are acting between the constituent atoms of a solid. This is important in interpreting and understanding the nature of bonding in the solids and non-destructive nature of the technique. Hence, elastic properties are suitable for describing the glass structure as a function of composition [1]. The role of  $\text{Na}_2\text{O}$  in the  $\text{B}_2\text{O}_3$  network is to modify the host structure through the transformation of the structural units of the borate network from  $[\text{BO}_3]$  to  $[\text{BO}_4]$ . Tungsten-containing glasses have been studied for the favorable properties of tungsten ions, such as high electro-negativity, polarizability, large ion radius, and changeable valance [2, 3]. A review of literature indicates that attempts have been made to study the structural and physical properties of  $x\text{Li}_2\text{O}-(30-x)\text{Na}_2\text{O}-10\text{WO}_3-60\text{B}_2\text{O}_3$  through IR [4] however, to the best of our knowledge, no ultrasonic study has been made on this kind of sodium borate glasses at room temperature. Therefore the objective of the present ultrasonic-based investigation has been made.

## 2. Materials and Methods

The glass samples of the formula  $20\text{Na}_2\text{O}-(80-x)\text{B}_2\text{O}_3-x\text{Li}_2\text{O}$  and  $20\text{Na}_2\text{O}-(80-x)\text{B}_2\text{O}_3-x\text{WO}_3$  (where  $x = 0$  to  $10$  in steps of  $2$  mol%) have been prepared by the conventional melt-quenching technique. Required quantities of analytical grade of  $\text{Na}_2\text{CO}_3$ ,  $\text{B}_2\text{O}_3$ ,  $\text{Li}_2\text{CO}_3$  and  $\text{WO}_3$  were obtained from E-Merck, Germany and Sd-Fine chemicals, India. The mixture is melted in alumina crucible at about  $1053\text{K}$  for  $45$  minutes to homogenize the melt. Then the glass samples were annealed at  $573\text{K}$  for two hours to avoid the mechanical strains developed during the quenching process. The amorphous nature of glass samples was confirmed by X-ray diffraction technique using an x-ray diffractometry

Density ( $\rho$ ), at room temperature was measured by following Archimedes principle. The ultrasonic wave (longitudinal and shear) velocities and attenuation of the glass specimens were measured using ultrasonic high energy Pulser receiver (PANAMETRICS – 5800 PR) technique at room temperature by making use of X-cut and Y-cut transducers at  $5$  MHz. The attenuation coefficient  $a$  of the sample in neper per unit length is obtained from the relation

$$I = I_0 e^{-\alpha t}$$

Where,  $t$  is the thickness of the sample,  $I_0$  and  $I$  are the ratios of amplitude of the two successive echoes.

## 3. Theory and Calculation

The elastic and thermal properties of the glass specimens were calculated at room temperature by using the measured values of density ( $\rho$ ), longitudinal velocity ( $U_l$ ), shear velocity ( $U_s$ ) and attenuation ( $\alpha$ ).

(i) Longitudinal modulus (L)

$$L = \rho U_l^2 \quad (1)$$

(ii) Shear modulus (G)

$$G = \rho U_s^2 \quad (2)$$

(iii) Bulk modulus (K)

$$K = L - \left(\frac{4}{3}\right)G \quad (3)$$

(iv) Poisson's ratio ( $\sigma$ )

$$\sigma = \left(\frac{L - 2G}{2(L - G)}\right) \quad (4)$$

(v) Young's modulus (E)

$$E = (1 + \sigma) 2G \quad (5)$$

(vi) Acoustic impedance (Z)

$$Z = U_l \rho \quad (6)$$

(vii) Internal friction ( $Q^{-1}$ )

$$Q^{-1} = \frac{\alpha}{8.66\pi f U_l} \quad (7)$$

Where,  $\alpha$  - attenuation coefficient and  $f$  -frequency of the quartz crystal

(viii) Microhardness (H)

$$H = (1 - 2\sigma) \frac{E}{6(1 + \sigma)} \quad (8)$$

(ix) Debye temperature ( $\theta_D$ )

$$\theta_D = \frac{h}{k} \left( \frac{9N}{4\pi V_m} \right)^{1/3} U_m \quad (9)$$

where,  $h, k, N, V_m$  and  $U_m$  are the Planck's constant ( $6.626 \times 10^{-34}$  JS), the Boltzmann's constant ( $1.38 \times 10^{-23}$  JK<sup>-1</sup>), the Avogadro's number ( $6.023 \times 10^{23}$  mol<sup>-1</sup>), the molar volume and mean sound velocity of the sample respectively

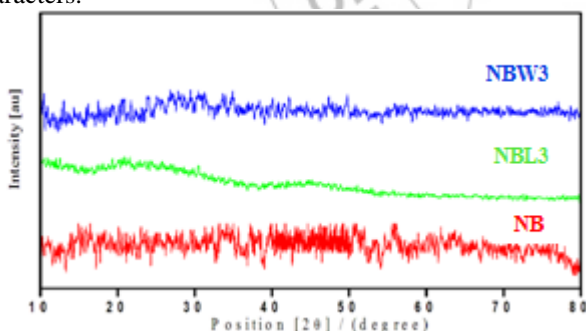
where  $U_m = \left[ \frac{1}{3} \left( \frac{2}{U_s^3} + \frac{1}{U_l^3} \right) \right]^{-1/3}$

(x) Thermal expansion coefficient ( $\alpha_p$ )

$$\alpha_p = 23.2 (U_l - 0.57457) \quad (10)$$

#### 4. Result and Discussion

The experimental values of density ( $\rho$ ), longitudinal ultrasonic velocity ( $U_l$ ), shear ultrasonic velocity ( $U_s$ ), and attenuation ( $\alpha$ ) of the sodium borate glasses with respect to the change in mol percentage of Li<sub>2</sub>O and WO<sub>3</sub> used as network modifier (NWM) are listed in the Table 1. The related computed parameters are presented in the Tables 2-3. The X-ray diffraction patterns (Fig. 1) of the studied glass systems reveals the absence of any discrete or continuous sharp crystalline peaks, but show homogenous glassy characters.



**Figure 1:** The powder XRD pattern of glass samples of NB, NBL3, and NBW3 at room temperature

The density is a powerful tool capable of exploring the changes in the structure of glasses. The density values (Table 1) were found to decrease with direct substitution of Li<sub>2</sub>O and WO<sub>3</sub> by B<sub>2</sub>O<sub>3</sub>, Na<sub>2</sub>O. The density values of NBL glass system are much higher than that of NBW glasses. Further, it is observed from the above table, the values of longitudinal velocity ( $U_l$ ) and shear velocity ( $U_s$ ) are increasing with increasing of Li<sub>2</sub>O contents, and the same has decreased with increasing of WO<sub>3</sub> contents, but the rate of increase of  $U_l$  is greater than that of  $U_s$ . The increase of ultrasonic velocities is related to the decrease in the number of non-bridging oxygen and consequently the increase in connectivity of the glass network [5]. Further, the elastic moduli and attenuation explores more information about the structural changes and stability of the glass network [6]. Table-1 shows the values of attenuation are increasing with increasing of Li<sub>2</sub>O concentrations, and it decreases with increasing of WO<sub>3</sub> concentrations which confirms the strengthening nature of these glasses as suggested from the composition dependence ultrasonic velocities [7].

The variation of longitudinal, shear, bulk and Young's moduli (Table 2) increases with increase in concentration of Li<sub>2</sub>O and, it decreases with increasing of WO<sub>3</sub> concentrations. The obvious decreases in elastic moduli are due to the continuous reduction in the rigidity of glass samples [8]. In the studied glass system, the values of Poisson's ratio (Table 2) are increases with increasing of Li<sub>2</sub>O and it reverses in WO<sub>3</sub> glasses. Further, these values are varying from 0.2 to 0.3. The decrease in Poisson's ratio is due to making of network linkages and formation of smaller structural units in the glass samples [9]. Further, an increase in cross-link density leads to a decrease in Poisson's ratio and vies-versa. Further, the increase in acoustic impedance and internal friction (Table 3) is due to the increase in compactness and rigidity of the structure of the Li<sub>2</sub>O compared to WO<sub>3</sub> glass. The continuous decrease in microhardness, Debye temperature and thermal expansion coefficient observed in WO<sub>3</sub> glasses (Table 3) reveals the presence of Non-bridging oxygen ion (NBO) and this causes the formation of soft glassy network [10,11].

**Table 1:** Composition, measured values of density ( $\rho$ ), longitudinal velocity ( $U_l$ ), shear velocity ( $U_s$ ) and attenuation ( $\alpha$ ) Of NB, NBL, and NBW glasses at room temperature.

Sample Label	Composition (mol %)	Density $\rho$ /( $\times$ kg.m <sup>-3</sup> )	Ultrasonic Velocity U/(m.s <sup>-1</sup> )		Attenuation $\alpha$ /(nepers.unit length <sup>-1</sup> )
			Longitudinal ( $U_l$ )	Shear ( $U_s$ )	
Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> (NB)					
NB	80-20	1353.6	5209.30	2786.06	44.88
System 1 : Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> -Li <sub>2</sub> CO <sub>3</sub> (NBL)					
NBL 1	20-78-2	1323.0	5485.44	2942.70	50.88
NBL 2	20-76-4	1309.9	5756.10	2994.92	51.58
NBL 3	20-74-6	1302.5	6020.94	3026.16	52.56
NBL 4	20-72-8	1204.7	6084.66	3074.87	71.00
NBL 5	20-70-10	1184.9	6250.00	3108.10	72.85

System 2 : Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> -WO <sub>3</sub> (NBW)					
NBW 1	20-78-2	1322.2	4919.15	2947.37	65.99
NBW 2	20-76-4	1261.0	4869.57	2879.58	57.91
NBW 3	20-74-6	1252.4	4695.65	2833.33	50.82
NBW 4	20-72-8	1224.9	4675.21	2813.57	38.39
NBW 5	20-70-10	1155.2	4641.35	2790.87	35.20

**Table 2:** Values of elastic moduli and Poisson's ratio of NB, NBL and NBW glasses at room temperature.

Sample Label	Longitudinal Modulus L/( $\times 10^{10}$ N.m <sup>-2</sup> )	Shear Modulus G/( $\times 10^{10}$ N.m <sup>-2</sup> )	Bulk Modulus K/( $\times 10^{10}$ N.m <sup>-2</sup> )	Young's Modulus E/( $\times 10^{10}$ N.m <sup>-2</sup> )	Poisson's Ratio ( $\sigma$ )
Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> (NB)					
NB	3.6732	1.0507	2.2723	2.7311	0.2997
System 1 : Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> -Li <sub>2</sub> CO <sub>3</sub> (NBL)					
NBL 1	3.9808	1.1457	2.4534	2.9740	0.29880
NBL 2	4.3401	1.1749	2.7735	3.0886	0.3144
NBL 3	4.7218	1.1928	3.1314	3.1752	0.3310
NBL 4	4.4602	1.1390	2.9415	3.0264	0.3285
NBL 5	4.6285	1.1447	3.1023	3.0579	0.3357
System 2 : Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> -WO <sub>3</sub> (NBW)					
NBW 1	3.1990	1.1486	1.6675	2.8023	0.2199
NBW 2	2.9902	1.0456	1.5960	2.5746	0.2311
NBW 3	2.7614	1.0054	1.4209	2.4528	0.2198
NBW 4	2.6773	0.9697	1.3844	2.3584	0.2161
NBW 5	2.4886	0.8998	1.2888	2.1898	0.2168

**Table 3:** Values of acoustic impedance (Z), internal friction ( $Q^{-1}$ ), microhardness ( $H_v$ ), Debye temperature ( $\theta_D$ ) and thermal expansion coefficient ( $\alpha_p$ ) of NB, NBL and NBW glasses at room temperature.

Sample Label	Acoustic Impedance Z/( $\times 10^7$ kg. m <sup>-2</sup> s <sup>-1</sup> )	Internal Friction ( $Q^{-1}$ )/( $\times 10^{-11}$ dB.s <sup>2</sup> m <sup>-2</sup> )	Micro Hardness $H_v$ /( $\times 10^9$ N.m <sup>-2</sup> )	Debye Temperature $\theta_D$ (K)	Thermal Expansion Coefficient $\alpha_p$ /( $\times 10^2$ m.s <sup>-1</sup> )
Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> (NB)					
NB	0.7051	2.1683	1.4032	296.60	1208.42
System 1 : Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> -Li <sub>2</sub> CO <sub>3</sub> (NBL)					
NBL 1	0.7257	3.4110	1.5431	298.62	1273.49
NBL 2	0.7540	3.2954	1.4538	303.44	1335.28
NBL 3	0.7843	3.2103	1.3439	306.67	1396.73
NBL 4	0.7330	4.2912	1.3021	309.00	1411.51
NBL 5	0.7406	4.2865	1.2536	322.92	1449.87
System 2 : Na <sub>2</sub> CO <sub>3</sub> -B <sub>2</sub> O <sub>3</sub> -WO <sub>3</sub> (NBW)					
NBW 1	0.6504	4.9333	2.1448	292.34	1141.11
NBW 2	0.6141	4.3734	1.8742	227.90	1129.61
NBW 3	0.5881	3.9801	1.8780	268.85	1089.26
NBW 4	0.5727	3.0197	1.8353	261.86	1084.52
NBW 5	0.5362	2.7890	1.6986	260.75	1076.66

## 5. Conclusion

The elastic moduli of the 20Na<sub>2</sub>O-(80-x) B<sub>2</sub>O<sub>3</sub>-xLi<sub>2</sub>O and 20Na<sub>2</sub>O-(80-x)B<sub>2</sub>O<sub>3</sub>-xWO<sub>3</sub> glass systems show many enhancements with the progressive addition of Li<sub>2</sub>O and WO<sub>3</sub>. The enhancements were attributed to the increase in the cross link density, and the rigidity of the glass network. The decrease in density of the glass specimens show that it

depends on the atomic weight of the metal atom in the network modifier (NWM). The decreasing elastic moduli indicate a reduction in network rigidity of the glass samples. It is generally accepted that lithium and tungsten ion enter the glass structure originally in one valance state viz., Li<sup>+</sup> and W<sup>6+</sup>. The estimated acoustical, elastic and mechanical properties of the lithium and tungsten doped with sodium borate glasses throw light on the rigidity and compactness in

structural network. However the NBL series of glass possess higher rigidity, strength and compactness of the glass network over the NBW glasses.

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## References

- [1] M. Venkata Subba Reddy, M. Sudhakara Reddy, C. Narayana Reddy, R.P.S. Chakradhar. Elastic properties of  $\text{Na}_2\text{O}-\text{B}_2\text{O}_3-\text{V}_2\text{O}_5$  glasses. *Journal of Alloys and Compounds* 479 (2009) 17–21.
- [2] A. Sheoran, A. Agarwal, S. Sanghi, V.P. Seth, S.K. Gupta, M. Arora. Effect of  $\text{WO}_3$  on EPR, structure and electrical conductivity of vanadyl doped  $\text{WO}_3\cdot\text{M}_2\text{O}\cdot\text{B}_2\text{O}_3$  (M=Li,Na) glasses. *Physica B*. 406, (2011) 4505-4511.
- [3] J. Pisarska, R. Lisiecki, W. Ryba-Romanowski, G. Dominiak-Dzik, T. Goryczka, L. Grobelny, W.A. Pisarski. Glass preparation and temperature-induced crystallization in multicomponent  $\text{B}_2\text{O}_3-\text{PbX}_2-\text{PbO}-\text{Al}_2\text{O}_3-\text{WO}_3-\text{Dy}_2\text{O}_3$  (X = F,Cl,Br) system. *Journal of Non-Crystalline Solids* 357 (2011) 1228-1231.
- [4] A. Edukondalu, B. Kavitha, M.A. Samee, Shaik Kareem Ahmed, Syed Rahman, K. Siva Kumar. Mixed alkali tungsten borate glasses – Optical and structural properties. *Journal of Alloys and Compounds* 552 (2013) 157–165.
- [5] Samir Y. Marzouk. Ultrasonic and infrared measurements of copper-doped sodium phosphate glasses. *Materials Chemistry and physics* 114 (2009) 188-193.
- [6] A. Nishara Begam, V. Rajendran. Structure investigation of  $\text{TeO}_2$ -BaO glass employing ultrasonic study. *Materials Letters* 61 (2007) 2143-2146.
- [7] El. Abd A. Moneim. Quantitative analysis of ultrasonic attenuation in  $\text{TiO}_2$ -doped  $\text{CaO}-\text{Al}_2\text{O}_3-\text{B}_2\text{O}_3$  glasses. *Materials Chemistry and Physics* 98 (2006) 261-266.
- [8] R. El-Mallawany, N. El-Khoshkhany, and H. Afifi. Ultrasonic studies of  $(\text{TeO}_2)_50-(\text{V}_2\text{O}_5)_{50-x}(\text{TiO}_2)_x$  glasses, *Materials Chemistry and Physics* 95 (2006) 321-327.
- [9] S.V. Pakade, S.P. Yawale, and W.J. Gawande. Ultrasonic velocity and elastic constant measurements in some borate glasses. *Acoustics Letters* 18 (1995) 212-216.
- [10] Yasser B. Saddeek, Elastic properties of  $\text{Gd}^{3+}$ -doped tellurovanadate glasses using pulse-echo technique. *Materials Chemistry and Physics* 91 (2005) 146-153.
- [11] M.A. Sidkey, A.M. Abd-El Fattah, L. Abd-El Latif, and R.I. Nakhla. Ultrasonic studies in some sodium borate glasses, *Journal of Pure and Applied Ultrasonics*. 12 (1990) 93-97.