

# Analysis of the Comments of Dr. Sanjay Jain and Adarsh Mangal on S. Nahar and Md. Abdul Alim (2017) A New Statistical Method to Solve Multiobjective Linear Programming Problem

Chandra Sen

Professor (Rtd.), Department of Agricultural Economics, Institute of Agricultural Sciences, Banaras Hindu University, Varanasi-221005, India

**Abstract:** An error in the estimation of multiobjective function has been pointed out by Dr. Sanjay and Dr. Adarsh in a research paper on Multiobjective Optimization (MOO) problems. The calculations should have been checked several times to avoid any such mistakes. There are few more aspects of Multiobjective Optimization (MOO) problems discussed here for improving the MOO methodologies.

**Keywords:** New statistical averaging method, Multiobjective optimization, Harmonic average, Sen's multiobjective optimization

## 1. Introduction

The comments of Dr. Sanjay Jain and Dr. Adarsh Mangal [33] on the paper entitled "A new statistical method to solve multiobjective linear programming" by S. Nahar and Md. Abdul Alim are appreciable. Though, it was a minor error in formulation of multiobjective function and there was no methodological or conceptual issues due to this error. Calculations should be checked thoroughly prior to submitting any manuscript for publication. The example used by S. Nahar & Md. Abdul Alim [20] is reproduced here for few methodological issues.

### Example 1

$$\text{Max. } Z_1 = X_1 + 2X_2$$

$$\text{Max. } Z_2 = X_1$$

$$\text{Min. } Z_3 = -2X_1 - 3X_2$$

$$\text{Min. } Z_4 = -X_2$$

Subject to:

$$6X_1 + 8X_2 \leq 48$$

$$X_1 + X_2 \geq 3$$

$$X_1 \leq 4$$

$$X_2 \leq 3$$

$$X_1, X_2 \geq 0$$

### Solution

The problem was solved for achieving all the four objective individually to see the conflicts amongst objectives. The solutions of MOO technique using harmonic mean technique by Nahar & Alim and Sanjay & Adarsh are also mentioned in Table 1:

**Table 1:** Individual and Multiobjective Optimization

Item	Individual Optimization				Sen's MOO Technique
	Max. $Z_1$	Max. $Z_2$	Min. $Z_3$	Min. $Z_4$	
$X_1, X_2$	4, 3	4, 3	4, 3	4, 3	4, 3
$Z_1$	10	10	10	10	10
$Z_2$	4	4	4	4	4
$Z_3$	-17	-17	-17	-17	-17
$Z_4$	-4	-4	-4	-4	-4
$Z^*$					9.8593
$Z^{**}$					9.9164

$Z^*$  = Multiobjective function (Nahar & Alim)

$Z^{**}$  = Multiobjective function (Sanjay & Adarsh)

The solutions of all the individual optimizations are the same and hence there is no conflicts amongst objectives. The solution of MOO is also same with minor error in the value of  $Z^*$  due to error in formulation MOO function. The example is not suitable for the application of any MOO technique. There are few relevant issues in the formulation and application of MOO techniques as discussed below.

## 2. Basic Conceptual Drawbacks

A number of MOO techniques [2], [3] ----- [28] have been proposed during the past three decades. The efforts were made to formulate multiobjective function using various mathematical equations ignoring the basic nature of the MOO problems as given below:

- (i) The objective functions may be non commensurable. The mathematical operations like addition /subtraction of the values of different dimensions seems illogical.
- (ii) There may be high deviations in the coefficients of decision variables  $X_i$  in the objective functions. The MOO solution may be biased to the dominating objective function.

These problems have been well resolved in several studies [1], [29], [30], [31], [32].

## 3. Inappropriate Examples

The examples used for validation of MOO techniques by most of the studies [2], [3] ----- [28] were not appropriate. A MOO technique is supposed to generate a compromise solution for achieving all the conflicting objectives. There was no conflicts amongst objectives in the examples used in these studies. Hence, there was no need of using any MOO technique to solve these examples. This is also true with the present study under review.

#### 4. Misinterpretation of the Results

Most of the studies [2], [3] ----- [28] considered the value of the combined objective function as the main achievement of the MOO technique. The multiobjective function is optimized to generate a compromising solution. However, the examples of these studies were non conflicting and should not be optimized by any MOO technique.

#### 5. Appropriate Example

The following example has been formulated and solved using Sen's MOO technique [1]

##### Example 2

$$\text{Max. } Z_1 = 6500X_1 + 5500X_2 + 7000X_3 + 7500X_4 + 4500X_5$$

$$\text{Max. } Z_2 = 70X_1 + 80X_2 + 90X_3 + 50X_4 + 100X_5$$

$$\text{Min. } Z_3 = 90X_1 + 130X_2 + 100X_3 + 160X_4 + 150X_5$$

$$\text{Min. } Z_4 = 1200X_1 + 800X_2 + 900X_3 + 1500X_4 + 1400X_5$$

Subject to:

$$X_1 + X_2 + X_3 + X_4 + X_5 = 13$$

$$X_1 \geq 1.5$$

$$X_3 \geq 0.5$$

$$X_1, X_2, X_3, X_4, X_5 \geq 0$$

##### Solution

All the four objectives have been achieved individually to see the presence of conflicts amongst objectives. The results of individual and MOO are presented in Table 2.

**Table 2:** Individual and Multiobjective Optimization

Item	Individual Optimization				Sen's MOO Technique
	Max. $Z_1$	Max. $Z_2$	Min. $Z_3$	Min. $Z_4$	
$X_1$	1.5, 0, 0.5, 10.5, 0	1.5, 0, 0.5, 0, 10.5	12.5, 0, 0.5, 0, 0	1.5, 10.5, 0.5, 0, 0	1.5, 0, 11.5, 0, 0
$Z_1$	92000	60500	84750	71000	90250
$Z_2$	675	1200	920	990	1140
$Z_3$	2855	1760	1175	1550	1285
$Z_4$	18000	16950	15450	10650	12150

The results of all the individual optimization are different. When first objective  $Z_1$  was maximized, It achieved the highest value of 92000. However, the remaining three objectives have not achieved. The similar trend was observed in optimization of other three objectives. The solution indicated the presence of high degree of conflicts amongst the objectives. When these objectives were optimized using Sen's MOO technique, all the objectives have been achieved simultaneously. Though, none of the objectives achieved its individual optimal value, but the solution seems more compromising and acceptable.

#### 6. Conclusion

The present analysis suggests that mathematical calculations in the manuscript should be thoroughly checked. It is also suggested to use appropriate examples and suitable methodologies for improving the utility of the research.

#### References

- [1] Sen, C. (1983) A new approach for multi-objective rural development planning. *The Indian Economic Journal* 30(4), 91-96.
- [2] Nejmaddin A. Sulaiman and Gulnar, W. Sadiq. (2006) Solving the Multi Objective Programming Problem Using Mean and Median Value. *Raf. J. of Comp. & Math's*. Vol. 3(1).
- [3] Sulaiman, N.A. and Othman, A.Q.,(2007).Optimal transformation Technique to solve multi-objective linear programming problem. *Journal of University of Kirkuk*,Vol. 2, No. 2.
- [4] Sulaiman, N.A. and Hamadameen, Abdul-Qader O.(2008), Optimal Transformation Technique to Solve Multi-Objective Linear Programming Problem (MOLPP), *Journal of Kirkuk University – Scientific Studies* , Vol. 3 (2), 158-168.
- [5] Nejmaddin A. Sulaiman and Abdul-Qader O. Hamadamin (2009) Solving Multi-Objective complementary programming problem (MOCPP) by using Optimal average. *Al-Rafidain Journal of computer Sciences & Mathematics* Vol.6 (3), 65-79.
- [6] Sulaiman, N. A. & Salih A. D. (2010).“ Using mean and median values to solve linear fractional multi-objective programming problem”, *Zanco Journal for Pure and Applied Science*, Salahaddin-Erbil University, Vol. 22, (5).
- [7] Basim A. Hassan (2011) Suggested Method For Solving Multi-Objective Linear Programming Problems. *Tikrit Journal of Pure Science*, Vol. 16(3), 255-260.
- [8] Nejmaddin A. Suleiman, Maher A. Nawkhass (2013) Transforming and Solving Multi-objective Quadratic Fractional Programming Problems by Optimal Average of Maximin&Minimax Techniques. *American Journal of Operational Research* 3(3), 92-98.
- [9] Sulaiman, N. A. and Abdulrahim, B. K. (2013) Using Transformation Technique To Solve Multi-Objective Linear Fractional Programming Problem. *International Journal of Research and Reviews in Applied Sciences*, Vol.14 (3), 559-567.
- [10] Nejmaddin A. Sulaiman, Basiya K. Abulrahim (2013) Arithmetic Average Transformation Technique to Solve Multi-Objective Quadratic Programming Problem. *Journal of Zankoy Sulaimani*, 15(1), 57-69.
- [11] Nejmaddin A. Sulaiman, Gulnar W. Sadiq & Basiya K. Abdulrahim. (2014) New Arithmetic average technique to solve Multi-Objective Linear Fractional Programming: Problem and its comparison with other techniques *International Journal of Research and Reviews in Applied Sciences*, Vol.18 (2), 122-131.
- [12] Abdulqader Othman Hamadameen and Zaitul Marlizawati Zainuddin (2014) Multiobjective Fuzzy Stochastic Linear Programming Problems with Inexact Probability Distribution. *AIP Conf. Proc.* 1602, 546-558.
- [13] Abdulqader O. Hamadameen and Zaitul Marlizawati Zainuddin (2015) A reciprocated result using an approach of multi-objective stochastic linear programming models with partial uncertainty. *International Journal of Mathematics in Operational Research*, Vol. 7 (4), 395-414.

- [14] Nejmaddin A. Sulaiman, Maher A. Nawkhass (2015) Using Short-Hierarchical Method to Solve Multi-Objective Linear Fractional Programming Problems. *Journal of Garmian University*, 1-15.
- [15] Nejmaddin A. Sulaiman, Rebaz B. Mustafa, (2016) Using harmonic mean to solve multi-objective linear programming problems. *American Journal of Operations Research*, 6, 25-30.
- [16] Nejmaddin A. Sulaiman, Ronak M. Abdullah and Snur O. Abdull (2016) Using Optimal Geometric Average Technique to Solve Extreme Point Multi-Objective Quadratic Programming Problems *Journal of Zankoy Sulaimani*, 18(3), 63-72.
- [17] Nejmaddin, A. Sulaiman and Rebaz B. Mustafa (2016) Transform extreme point Multi-Objective Linear Programming problem to extreme point single objective Linear Programming Problem by Using Harmonic Mean. *Applied Mathematics* Vol. 6(5) 95-99.
- [18] Nejmaddin A. Sulaiman, Maher A. Nawkhass (2016) Using standard division to solve Multi-Objective Quadratic fractional programming. *Journal of Zankoy Sulaimani*, 18(3) 157-163.
- [19] Akhtar Huma, Modi Geeta and Duraphe Sushma, (2017), Transforming and Optimizing Multi-Objective Quadratic Fractional Programming Problem. *International Journal of Statistics and Applied Mathematics*, Vol. 2, (1) 01-05.
- [20] Samsun Nahar, Md. Abdul Alim (2017) A New Statistical Averaging Method to Solve Multi-Objective Linear Programming Problem. *International Journal of Science and Research*. Vol. 6(8), 623-629.
- [21] Akhtar, Huma, Geeta Modi and Sushma Duraphe (2017) An Appropriate Approach for Transforming and Optimizing Multi-Objective Quadratic Fractional Programming Problem. *International Journal of Mathematics Trends and Technology* Vol. 50 (2), 80-83
- [22] Maher A. Nawkhass, Hawkar Qasim Birdawod (2017) Transformed and Solving Multi-Objective Linear Programming Problems to Single-Objective by Using Correlation Technique. *Cihan International Journal of Social Science* Vol. 1, (1), 30-36.
- [23] Huma Akhtar and Geeta Modi (2017) An approach for solving Multi-Objective fractional programming problem and it's comparison with other techniques. *International Journal of Scientific and Innovative Mathematical Research*, Vol. 5 (11), 1-5.
- [24] Samsun Nahar, Md. Abdul Alim (2017). A New Geometric Average Technique to Solve Multi-Objective Linear Fractional Programming Problem and Comparison with New Arithmetic Average Technique. *IOSR Journal of Mathematics (IOSR-JM)* Vol. 13, (3), 39-52.
- [25] Abdulqader O. Hamadameen and Nasruddin Hassan (2018) Pareto optimal solution for multiobjective stochastic linear programming problems with partial uncertainty. *International Journal of Mathematics in Operational Research*, Vol. 12.(2), 139-166.
- [26] Zahidul Islam Sohag, Md. Asadujjaman (2018).A Proposed New Average Method for Solving Multi-Objective Linear Programming Problem Using Various Kinds of Mean Techniques. *Mathematics Letters* , 4(2): 25-33.
- [27] Samsun Nahar, Samima Akther, Mohammad Abdul Alim (2018) Statistical Averaging Method and New Statistical Averaging Method for Solving Extreme Point Multi-Objective Linear Programming Problem, *Mathematics Letters*, 4(3): 44-50.
- [28] Zahidul Islam Sohag, and M. Asadujjaman (2019) A Proposed Method for Solving Quasi-Concave Quadratic Programming Problems by Multi-Objective Technique with Computer Algebra, *IOSR Journal of Mathematics*, Vol. 15,(1)12-18.
- [29] Chandra Sen (2018) Multi Objective Optimization Techniques: Misconceptions and Clarifications. *International Journal of Scientific and Innovative Mathematical Research* Vol. 6, Issue 6, 29-33.
- [30] Chandra Sen (2018) Sen's Multi-Objective Programming Method and its Comparison with Other Techniques. *American Journal of Operational Research*, Vol. 8 (1): 10-13.
- [31] Chandra Sen (2019) Improved Scalarizing Techniques for Solving Multi-Objective Optimization Problems. *American Journal of Operational Research*, Vol. 9 (1): 8-11.
- [32] Chandra Sen (2020) Improved Averaging Techniques for Solving Multi-Objective Optimization (MOO) Problems. *SN Applied Sciences*.2: 286.
- [33] Sanjay Jain and Adarsh Mangal (2020) A comment on S. Nahar & Md. Abdul Alim (2017) A New Statistical Averaging Method to Solve Multi-Objective Linear Programming Problem. *International Journal of Science and Research*, Vol.9(6),573-576.