

# Cost Optimization of Column

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**Abstract:** *The cost differences between circular and square column increase with the increase in gross area of concrete. The ratio of longitudinal steel area to gross concrete section is in the range from 0.01 to 0.08, according to BNBC/ACI Code. The common practice is to choose an arbitrary section and check that for bending and axial load with a reinforcement ratio around 2-3% but we don't know whether it is economical or not. However, for a particular moment and load there is only one section which is economical, it means only for a certain percentage of reinforcement the section will be optimized. Since the cost of concrete and reinforcement are different which may increase or decrease independently, the percentage of reinforcement in the optimized section varies with the price ratio of steel to concrete. Analysing for the present cost ratio of steel and concrete, it is seen that a column section is optimized at 1 percent of reinforcement for low-rise to medium rise building. This is true for any column that after a certain price ratio it is optimized at reinforcement of the order of 1 percent on that loading and moment condition. Use of high strength concrete in the column has an effect of minimizing the cost. Using 5000 psi concrete instead of 3000 psi concrete saves 20-50 percent of total cost in general. For same axial load and moment resisting capacity, a circular column is found to be more costly than a square column. Also, the cost differences between circular and square column increase with the increase in gross area of concrete.*

## 1. Introduction

According to BNBC 2006, the ratio of longitudinal steel area ( $A_{st}$ ) to gross concrete area ( $A_g$ ) in column is in the range from 0.01 to 0.08. But, in practice, designers do not usually provide more steel than 4% of the gross concrete area ( $A_g$ ) because of the difficulty owing to congestion of the reinforcement. The common practice in designing a column is to choose arbitrary sections and check them for bending and axial load with a reinforcement about 1% to 4% of the gross concrete area. However, for a particular loading condition, there is only one section which can be found Economical, which means for a certain percentage of reinforcement the section is optimized. The percentage of reinforcement in the optimized section is found to vary with the price ratio of steel to concrete.

Use of high strength concrete in the column is another way to minimize the total cost of the column. High strength concrete reduces the requirement of high percentage of steel reinforcement in the column. Cost of steel being the governing factor in the optimization of the column section, the section gets optimized with the increase in strength of concrete. Therefore, the effect of percentage of reinforcement and the strength of concrete both in the optimum design of column section is dealt with in this paper. Also, the cost comparison between circular and rectangular column sections having same axial load and moment resisting capacity is analyzed in this paper to select an economical section.

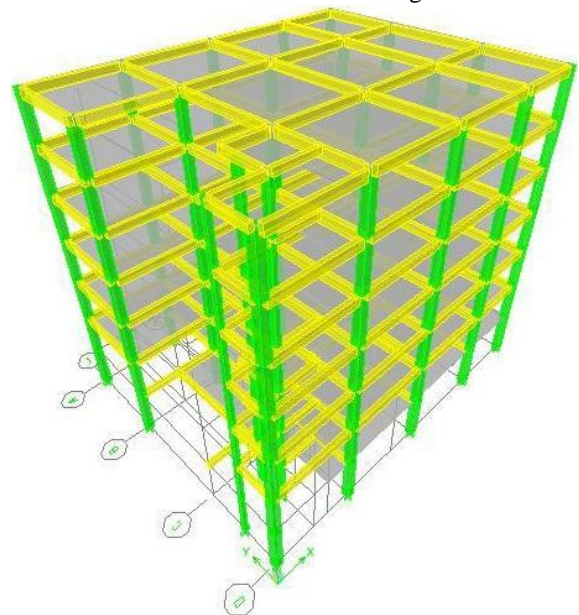
## 2. Methodology

Cost optimization analysis is carried out in this paper for three cases:

- To find a optimized percentage of reinforcement considering existing price of concrete and reinforcement
- To compare the cost of column for various strength of concrete
- To compare the cost of circular and square column for

similar loading condition.

Figure 1 shows the three dimensional and plan view of a typical six storied building which is analyzed for designing the columns. For a specific loading condition, the required percentage of reinforcement for a column will decrease with the increase in gross concrete area. This will decrease up to a certain section and after that the required amount of reinforcement will increase. To find the optimized section, columns of a particular building are chosen and designed for various section and percentage of reinforcement for a specific loading condition. Finally, total cost versus percentage of reinforcement graph is plotted for different price ratios to find out the optimized percentage of reinforcement. ETABS 9.7 is used to design the column.



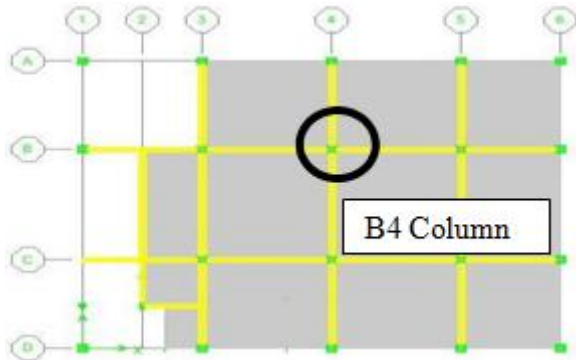


Figure 1: 3D view and plan of a six storied building

paper, the analysis results (tables and figures) are shown only for a six storied irregular type of building as shown in figure 1. The column B4 of the building is analyzed here for optimum cost calculation.

**Cost Analysis**

A ground floor column with a story height of 10ft is considered. 60 grade reinforcement and 4000 psi concrete is chosen for the analysis. The present cost of 60 grade steel and 4000 psi concrete are given below.

Cost of 60 grade Reinforcement= 60000 BDT/ton

Cost of 4000 psi concrete= 210 BDT/ cft

Again, in comparing the cost of column for different strength of concrete, column of a particular building is chosen and designed for different strength of concrete by ETABS 9.7. Finally, a graph of total cost versus strength of concrete is plotted to show the result. For similar loading condition, both square and circular column are designed firstly by changing the concrete gross area and secondly by changing the percentage of reinforcement. The cost of ties in both cases is neglected as difference of cost of ties is very little. Finally, two graphs are plotted for either of the cases showing the variation of cost. PCA COL software is used here to design the column.

**3. A Optimized Percentage of Reinforcement Considering Existing Price**

The applied axial load and moment in the square column is resisted both by concrete and steel simultaneously. As the cost of concrete and reinforcement may increase or decrease independently, the economic section is found to depend on a factor called price ratio X where,  $X = \text{Price of 1cft reinforcement (490 lb)}/\text{Price of 1 cft concrete} = (\text{Price of reinforcement (ton)}/\text{Price of concrete (cft)}) \times 223 \times 10^{-3}$

**Selection of Structure**

The cost optimization analysis is performed for various types of buildings. The conclusions and remarks are given on the basis of the structures which have been dealt with. In this

The following table shows the cost analysis of B4 column at ground floor of the selected building for different price ratios.

**Table 1: Cost analysis of B4 column (Square) for different price ratios**

| BxL (Column Size) | Ag (Column area) | Ast (Steel area) | Percentage of Steel | Total Cost (BDT) for X=5 | Total Cost (BDT) for X=10 | Total Cost (BDT) for X=15 | Total Cost (BDT) for X=20 | Total Cost (BDT) for X=25 | Total Cost (BDT) for X=30 | Total Cost (BDT) for X=50 | Total Cost (BDT) for X=65 |
|-------------------|------------------|------------------|---------------------|--------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|
| 16x18             | 288              | 17.864           | 6.203               | 5503                     | 6805                      | 8108                      | 9410                      | 10713                     | 12016                     | 17226                     | 21134                     |
| 18x18             | 324              | 14.925           | 4.606               | 5813                     | 6902                      | 7990                      | 9078                      | 10166                     | 11255                     | 15608                     | 18873                     |
| 18x20             | 360              | 13.532           | 3.759               | 6237                     | 7223                      | 8210                      | 9197                      | 10184                     | 11170                     | 15117                     | 18077                     |
| 18x22             | 396              | 11.922           | 3.011               | 6644                     | 7514                      | 8383                      | 9252                      | 10122                     | 10991                     | 14468                     | 17076                     |
| 18x24             | 432              | 10.672           | 2.470               | 7078                     | 7856                      | 8635                      | 9413                      | 10191                     | 10969                     | 14082                     | 16416                     |
| 20x22             | 440              | 9.348            | 2.125               | 7098                     | 7780                      | 8462                      | 9143                      | 9825                      | 10506                     | 13233                     | 15278                     |
| 20x24             | 480              | 8.04             | 1.675               | 7586                     | 8173                      | 8759                      | 9345                      | 9931                      | 10518                     | 12863                     | 14621                     |
| 22x22             | 484              | 6.598            | 1.363               | 7539                     | 8021                      | 8502                      | 8983                      | 9464                      | 9945                      | 11869                     | 13313                     |
| 22x23             | 506              | 5.802            | 1.147               | 7802                     | 8225                      | 8648                      | 9071                      | 9494                      | 9918                      | 11610                     | 12879                     |
| 22x24             | 528              | 5.280            | 1.000               | 8085                     | 8470                      | 8855                      | 9240                      | 9625                      | 10010                     | 11550                     | 12705                     |

Two graphs are plotted from the above table to represent the result. Figure 2 implies for the comparison of cost for

various price ratios and figure 3 shows the variation of optimizing percentage of reinforcement with the price ratios.

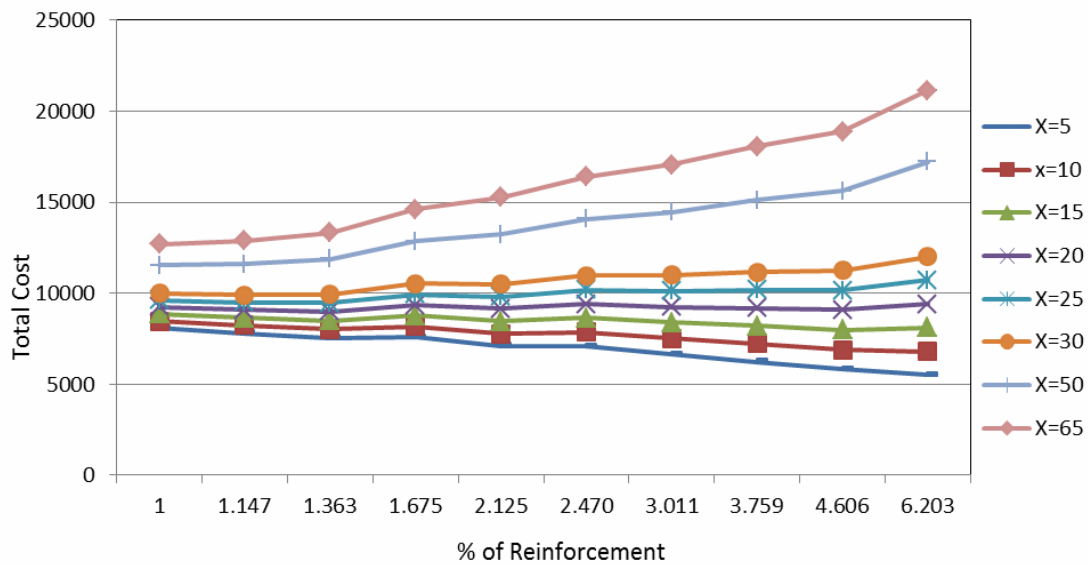


Figure 2: Graphical analysis of cost for various price ratios

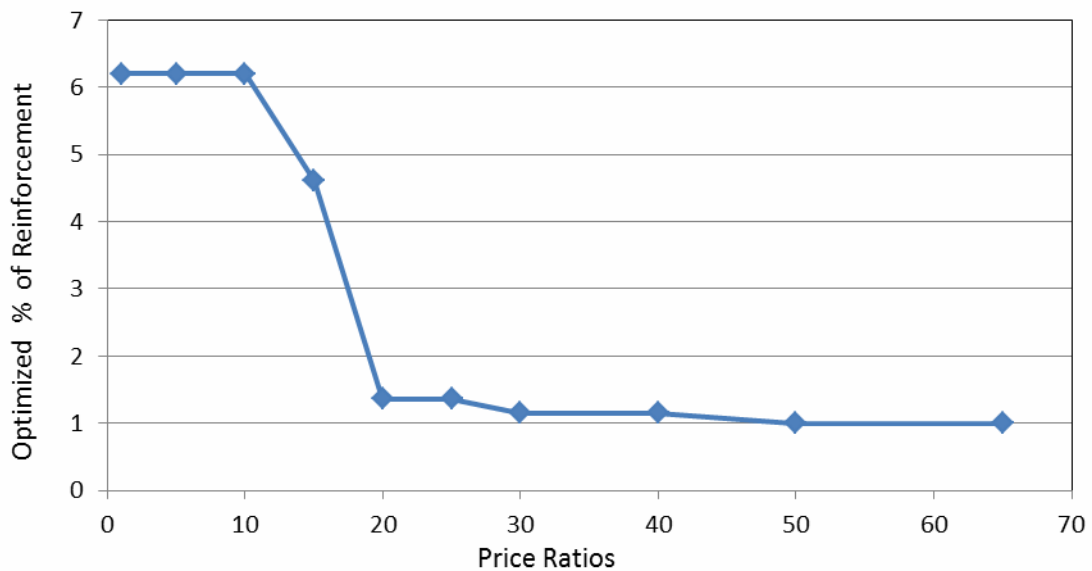


Figure 3: Variation of Optimized percentage of reinforcement with price ratios

For current price of reinforcement and concrete, the estimated price ratio is 65. It can be seen from the figure 2 that use of 1 percent of reinforcement at the existing price ratio gives the most cost effective design of column and the estimated cost is found 12705 BDT. The corresponding cost for 2.47 percent of reinforcement is estimated 16416 BDT. The difference in cost is 3711 BDT may seem very small. But considering the overall structure, this amount will not be so small. For the B4 column of this particular building, use of 2.47 percent of reinforcement instead of 1 percent of reinforcement increases the column cost by 29.21percent. Again, column designed using 4.6 percent of reinforcement is about 1.5 times more costly than column designed using 1 percent of reinforcement.

Figure 3 shows how the optimized percentage of reinforcement changes with the changes of price ratios. When the price of concrete and reinforcement are same, i.e

$X=1$ , the column section needs about 6.2 percent of reinforcement to get optimized. With the increase in price ratio, the optimized percentage of reinforcement decreases and after a certain price ratio the economical percentage of reinforcement becomes of the order of 1 percent. This is true for any column that after a certain price ratio ( $X=30$ ) the column design is optimized at reinforcement of the order of 1 percent on that loading and moment condition.

#### 4. Cost Comparison of Column for Various Strength of Concrete

The same structure is now analyzed for a given section of column (20"x20") at the ground floor level but for different strength of concrete. The price of concrete increases with increased concrete strength. The cost analysis result for B4 column is summarized below in the table 2.

**Table 2:** Cost analysis of B4 column for different strength of concrete

| Concrete Strength (psi) | Price of Concrete Per Cft (BDT) | Column Size (inxin) | Reqd. Reinforcement (in <sup>2</sup> ) | Cost of Reinforcement (BDT) | Cost of Concrete (BDT) | Total Cost (BDT) |
|-------------------------|---------------------------------|---------------------|--|-----------------------------|------------------------|------------------|
| 2000                    | 195                             | 20X20               | 22.397                                 | 20785                       | 5417                   | 26202            |
| 2500                    | 198                             | 20X20               | 19.177                                 | 17797                       | 5500                   | 23297            |
| 3000                    | 201                             | 20X20               | 15.876                                 | 14733                       | 5583                   | 20317            |
| 3500                    | 205                             | 20X20               | 13.101                                 | 12158                       | 5694                   | 17853            |
| 4000                    | 210                             | 20X20               | 10.547                                 | 9788                        | 5833                   | 15621            |
| 4500                    | 215                             | 20X20               | 8.059                                  | 7479                        | 5972                   | 13451            |
| 5000                    | 220                             | 20X20               | 5.849                                  | 5428                        | 6111                   | 11539            |
| 5500                    | 223                             | 20X20               | 4.000                                  | 3712                        | 6194                   | 9907             |

Price Source: Various Construction Firms, Bangladesh, August 2011

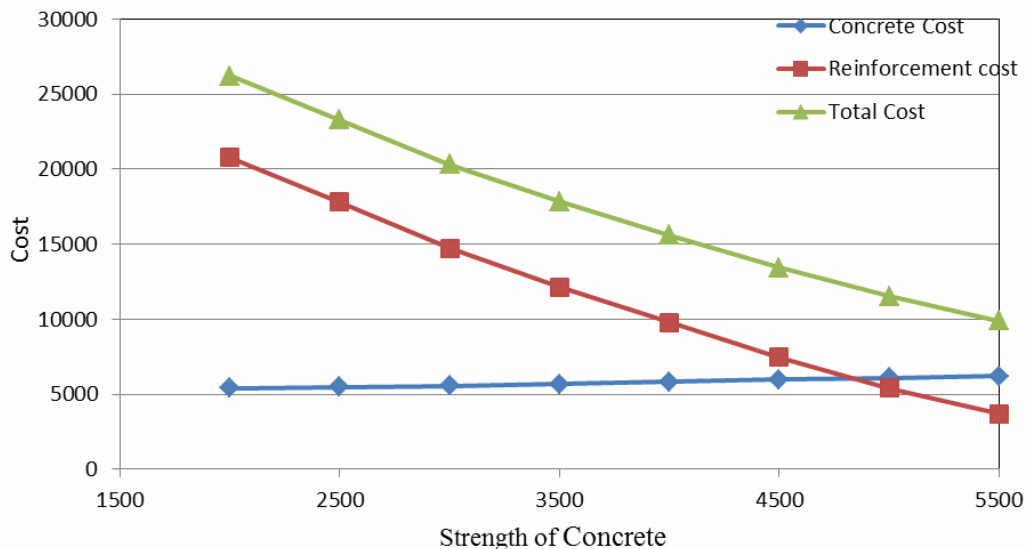


Figure 4: Variation of cost with increase in the strength of concrete

The analysis shows the required amount of reinforcement decreases with the increasing strength of concrete for a specific loading condition. The moment and axial load on a column is resisted by concrete and reinforcement simultaneously. As the selected column section is fixed and the loading condition is similar, so the required reinforcement decreases with the increasing strength of concrete. From the graph, it is also seen that when the concrete strength is increased, the increase in cost of concrete is very small compared to the decrease in cost of steel. Also, the total cost reduces 2 times for this particular column when 5000 psi concrete is used instead of 3000 psi concrete. After performing the similar analysis for some high rise buildings, it is found that using 5000 psi concrete instead of 3000 psi concrete saves 20-50 percent of total column construction cost.

### 5. Comparison of the Cost between Circular and Square Column for Similar Loading Conditions

For architectural purposes, engineers frequently use circular columns. Therefore, it is of prime importance to know the cost effectiveness of circular column with respect to square or rectangular column. For comparison purposes, 8 (A~H) column samples are taken and are designed as both circular and square columns in two ways:

- Keeping the gross concrete area same but changing the required reinforcement
- Keeping the reinforcement same but changing the required gross area.

The result is shown in the table 3 and table 4.

**Table 3:** Cost comparison between square and circular columns changing the gross concrete area

| Sample | L   | B     | Ag    | No. of Bar | Ast  | Percentage of Steel | Axial Load Capacity | Moment Capacity Mx | Moment Capacity My | Cost of Concrete (BDT) | Cost of Reinforcement (BDT) | Total cost |
|--------|-----|-------|-------|------------|------|---------------------|---------------------|--------------------|--------------------|------------------------|-----------------------------|------------|
| A      | 12  | 12    | 144   | 8#6        | 3.52 | 2.44                | 128                 | 73                 | 73                 | 2100                   | 3267                        | 5367       |
|        | Dia | 16.75 | 220.5 | 8#6        | 3.52 | 1.6                 | 128                 | 74                 | 74                 | 3216                   | 3267                        | 6482       |
| B      | 15  | 15    | 225   | 8#8        | 6.32 | 2.81                | 220                 | 164                | 164                | 3281                   | 5865                        | 9146       |
|        | Dia | 21.25 | 355   | 8#8        | 6.32 | 1.78                | 220                 | 166                | 166                | 5177                   | 5865                        | 11042      |
| C      | 16  | 16    | 256   | 8#8        | 6.32 | 2.47                | 252                 | 190                | 190                | 3733                   | 5865                        | 9598       |
|        | Dia | 22.75 | 406.5 | 8#8        | 6.32 | 1.55                | 252                 | 194                | 194                | 5928                   | 5865                        | 11793      |
| D      | 19  | 19    | 361   | 8#9        | 8    | 2.22                | 369                 | 312                | 312                | 5265                   | 7424                        | 12689      |
|        | Dia | 27    | 572.5 | 8#9        | 8    | 1.4                 | 366                 | 316                | 316                | 8349                   | 7424                        | 15773      |

|   |     |       |     |      |       |      |     |     |     |       |      |       |
|---|-----|-------|-----|------|-------|------|-----|-----|-----|-------|------|-------|
| E | 20  | 20    | 400 | 8#9  | 8     | 2    | 413 | 350 | 350 | 5833  | 7424 | 13258 |
|   | Dia | 28.35 | 638 | 8#9  | 8     | 2.01 | 413 | 359 | 359 | 9304  | 7424 | 16728 |
| F | 22  | 22    | 484 | 8#10 | 10.16 | 2.1  | 505 | 481 | 481 | 7058  | 9429 | 16487 |
|   | Dia | 31.25 | 767 | 8#10 | 10.16 | 2.07 | 488 | 488 | 488 | 11185 | 9429 | 20614 |
| G | 24  | 24    | 576 | 8#10 | 10.16 | 1.76 | 611 | 585 | 585 | 8400  | 9429 | 17829 |
|   | Dia | 34    | 908 | 8#10 | 10.16 | 1.77 | 602 | 595 | 595 | 13242 | 9429 | 22670 |
| H | 25  | 25    | 625 | 8#10 | 10.16 | 1.63 | 657 | 643 | 643 | 9115  | 9429 | 18543 |
|   | Dia | 35.5  | 990 | 8#10 | 10.16 | 1.65 | 648 | 657 | 657 | 14438 | 9429 | 23866 |

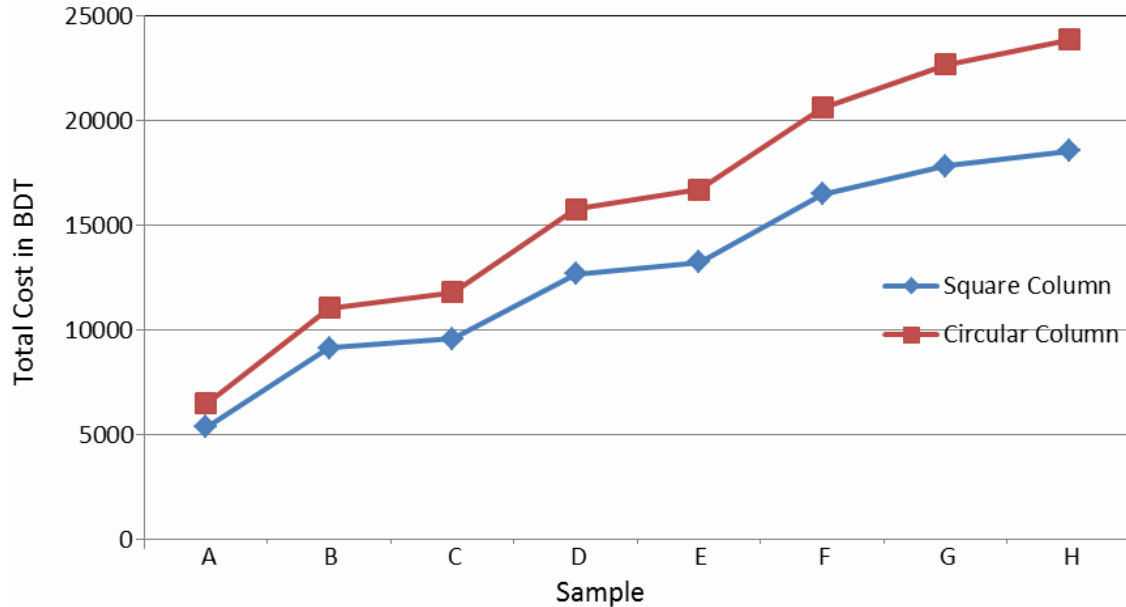
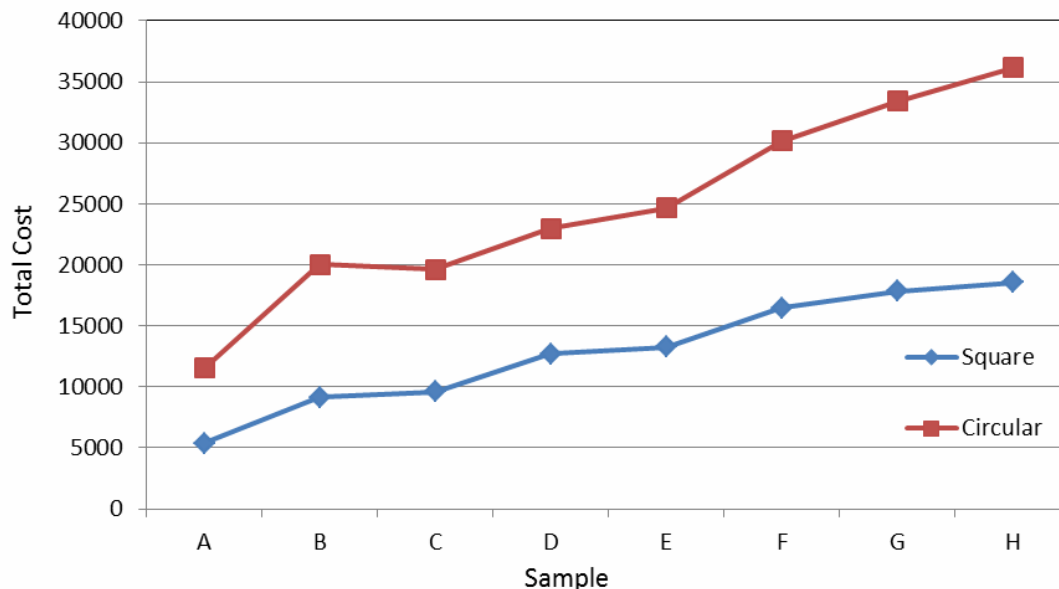


Figure 5: Difference in cost for various samples (Same reinforcement)

Table 4: Cost comparison between square and circular columns changing the reinforcement

| Sample | L   | B    | Ag     | No. of Bar | Ast   | Percentage of Steel | Axial Load Capacity | Moment Capacity Mx | Moment Capacity My | Cost of Concrete (BDT) | Cost of Rein for cement (BDT) | Total cost |
|--------|-----|------|--------|------------|-------|---------------------|---------------------|--------------------|--------------------|------------------------|-------------------------------|------------|
| A      | 12  | 12   | 144    | 8#6        | 3.52  | 2.44                | 128                 | 73                 | 73                 | 2100                   | 3267                          | 5367       |
|        | Dia | 13.5 | 143.14 | 8#10       | 10.16 | 7.10                | 132                 | 74                 | 74                 | 2087                   | 9429                          | 11516      |
| B      | 15  | 15   | 225    | 8#8        | 6.32  | 2.81                | 220                 | 164                | 164                | 3281                   | 5865                          | 9146       |
|        | Dia | 17   | 226.98 | 8#14       | 18    | 7.93                | 231                 | 170                | 170                | 3310                   | 16705                         | 20015      |
| C      | 16  | 16   | 256    | 8#8        | 6.32  | 2.47                | 252                 | 190                | 190                | 3733                   | 5865                          | 9598       |
|        | Dia | 18   | 254.47 | 11#11      | 17.16 | 6.74                | 258                 | 193                | 193                | 3711                   | 15925                         | 19636      |
| D      | 19  | 19   | 361    | 8#9        | 8     | 2.22                | 369                 | 312                | 312                | 5265                   | 7424                          | 12689      |
|        | Dia | 21.5 | 363.05 | 15#10      | 19.05 | 5.25                | 372                 | 310                | 310                | 5295                   | 17679                         | 22974      |
| E      | 20  | 20   | 400    | 8#9        | 8     | 2.00                | 413                 | 350                | 350                | 5833                   | 7424                          | 13258      |
|        | Dia | 22.5 | 397.61 | 16#10      | 20.32 | 5.11                | 420                 | 352                | 352                | 5798                   | 18858                         | 24656      |
| F      | 22  | 22   | 484    | 8#10       | 10.16 | 2.1                 | 505                 | 481                | 481                | 7058                   | 9429                          | 16487      |
|        | Dia | 25   | 490.87 | 11#14      | 24.75 | 5.04                | 504                 | 481                | 481                | 7159                   | 22969                         | 30127      |
| G      | 24  | 24   | 576    | 8#10       | 10.16 | 1.76                | 611                 | 585                | 585                | 8400                   | 9429                          | 17829      |
|        | Dia | 27   | 572.56 | 12#14      | 27    | 4.72                | 613                 | 587                | 587                | 8350                   | 25057                         | 33407      |
| H      | 25  | 25   | 625    | 8#10       | 10.16 | 1.63                | 657                 | 643                | 643                | 9115                   | 9429                          | 18543      |
|        | Dia | 28   | 615.75 | 13#14      | 29.25 | 4.75                | 671                 | 664                | 664                | 8980                   | 27145                         | 36125      |



**Figure 6:** Difference in cost for various samples (Same concrete gross area) Considering the same reinforcement (Table 3), it can be seen that a circular column requires more concrete area than a square column for same loading conditions.

Therefore, circular column costs about 20-30 percent more than square column in this case. Considering the similar gross concrete area (Table 4), it can be seen that a circular column requires more reinforcement than a square column. Therefore, circular column costs about 80-130 percent more than square column in this case. So when column is designed as circular it should be designed keeping the reinforcement same as square or rectangular column.

## 6. Conclusion

When the price ratio is more than 30, column section gets optimized at reinforcement of the order of 1 percent. For present market price of concrete and reinforcement ( $X=65$ ) in Bangladesh, a column section is optimized at 1 percent of reinforcement. This implies a column of larger section with reinforcement around 1.0 percent is more economical than a column of smaller section with 3-4 percent of reinforcement. Therefore, engineers should go for larger concrete section instead of larger percentage of reinforcement for optimum design for low rise buildings.

If proper high strength of concrete can be obtained in field condition, it can result in minimizing the total cost of column. Using 5000 psi concrete instead of 3000 psi concrete saves 20-50 percent of total cost. Use of 1.0 percent of reinforcement sometimes increases the column dimension more than the acceptable limit. High strength concrete may be used in this case to reduce the section and at the same time it is economical too.

The circular column is more costly than a square column having same axial load and moment resisting capacity. However, sometimes engineers prefer circular column for Architectural beauty or other practical purposes. But when cost is a vital factor, circular columns should be avoided as much as possible.

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