

Unified Theory of Force

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Abstract: Unified theory of force defines that not only gravity but any kind of force depends upon space-time curvature and a general equation of unified force is suggested.

Keywords: Unified force theory, space-time curvature, force field

If S is the position in space of a particle of mass 'm' at a time $t=t$ then its velocity after a time interval of dt will be as follows if $\frac{d^i s}{dt^i} = \text{constant}$

$$S|_{t=t+dt} = S|_{t=t} + \frac{ds}{dt} \frac{t}{1!} + \frac{d^2 s}{dt^2} \frac{t^2}{2!} + \frac{d^3 s}{dt^3} \frac{t^3}{3!} + \dots + \frac{d^i s}{dt^i} \frac{t^i}{i!}, \text{ for } \frac{d^i s}{dt^i} = \text{constant}$$

$$\text{Now, } \frac{ds}{dt}|_{t=t+dt} = \frac{ds}{dt}|_{t=t} + \frac{d^2 s}{dt^2} \frac{t}{1!} + \frac{d^3 s}{dt^3} \frac{t^2}{2!} + \frac{d^4 s}{dt^4} \frac{t^3}{3!} + \dots + \frac{d^i s}{dt^i} \frac{t^{(i-1)}}{(i-1)!}$$

And so on.

$$\text{Thus, } \frac{d^{(i-1)} s}{dt^{(i-1)}}|_{t=t+dt} = \frac{d^{(i-1)} s}{dt^{(i-1)}}|_{t=t} + \frac{d^i s}{dt^i} \frac{t}{1!} \text{ and finally } \frac{d^i s}{dt^i} = \text{constant}$$

$$\begin{aligned} \text{Then force } F &= m \left\{ \frac{d^i s}{dt^i} + \frac{d^{(i-1)} s}{dt^{(i-1)}} + \dots + \frac{d^2 s}{dt^2} \right\} \\ &= m \left[\frac{d^i s}{dt^i} \left\{ 1 + \frac{t}{1!} + \frac{t^2}{2!} + \dots + \frac{t^{(i-2)}}{(i-2)!} \right\} + \frac{d^{(i-1)} s}{dt^{(i-1)}} \left\{ 1 + \frac{t}{1!} + \frac{t^2}{2!} + \dots + \frac{t^{(i-3)}}{(i-3)!} \right\} + \dots + \frac{d^2 s}{dt^2} \right] \end{aligned}$$

$$\text{Now, let us assume } f = 1 + \frac{t}{1!} + \frac{t^2}{2!} + \dots + \frac{t^n}{n!}$$

$$\text{Thus, } \frac{df}{dt} = 1 + \frac{t}{1!} + \frac{t^2}{2!} + \dots + \frac{t^{(n-1)}}{(n-1)!} = f - \frac{t^n}{n!}$$

Now taking integration in both side, $f = ft - \frac{t^{(n+1)}}{(n+1)!} + c$ [if $t=0, c=f$]

$$\text{Thus, } ft = \frac{t^{(n+1)}}{(n+1)!} \text{ or } f = \frac{t^n}{(n+1)!}$$

$$\text{So, force } F = m \left[\frac{d^i s}{dt^i} \frac{t^{(i-2)}}{(i-1)!} + \frac{d^{(i-1)} s}{dt^{(i-1)}} \frac{t^{(i-3)}}{(i-2)!} + \dots + \frac{d^3 s}{dt^3} \frac{t^1}{(2)!} + \frac{d^2 s}{dt^2} \right]$$

Now if $F = \text{constant}$, it will be independent of 't' thus $\frac{d^2 s}{dt^2} = \text{constant}$ and $\frac{d^3 s}{dt^3} = 0$. So, $F = m \frac{d^2 s}{dt^2}$

Now if $\frac{dF}{dt} = \text{constant}$, means it will be independent of 't' thus $\frac{d^3 s}{dt^3} = \text{constant}$ and $\frac{d^4 s}{dt^4} = 0$ so, $F = m \left[\frac{d^3 s}{dt^3} \frac{t^1}{(2)!} + \frac{d^2 s}{dt^2} \right]$ and so on.

Now if $\frac{d^i s}{dt^i} = \text{constant}$ then $\frac{d^{(i-2)} F}{dt^{(i-2)}} = \text{constant}$.

$$\begin{aligned} \text{and } F &= m \left[\frac{d^i s}{dt^i} \frac{t^{(i-2)}}{(i-1)!} + \frac{d^{(i-1)} s}{dt^{(i-1)}} \frac{t^{(i-3)}}{(i-2)!} + \dots + \frac{d^3 s}{dt^3} \frac{t^1}{(2)!} + \frac{d^2 s}{dt^2} \right] \\ &= m \sum_{k=2}^i \frac{d^k s}{dt^k} \frac{t^{(k-2)}}{(k-1)!} = m \sum_{k=0}^i \frac{d^k f}{dt^k} \frac{t^{(k)}}{(k+1)!} \text{ where } f = \frac{d^2 s}{dt^2} \end{aligned}$$

Now, for any kind of force field $\frac{d^2 s}{dt^2} = f = c/d^2$ where $c = \text{constant}$ depending upon the intensity of force field $d = \text{space between them}$

$$F = \lim_{i \rightarrow \infty} m \sum_{k=0}^i \frac{d^k f}{dt^k} \frac{t^{(k)}}{(k+1)!} \text{ where } f = \frac{d^2 s}{dt^2} = c/d^2$$

If a particle creating force field having mass M , electric charge Q and magnetic intensity m_1 then $c = GM$ (for gravitational field), KQ (for electric field), $\mu m_1 / 4\pi$ (for magnetic field)

Now for $f = c/d^2$ if initial velocity $u = 0$,

$$\frac{df}{dt} = (-2c/d^3) u = 0 \text{ \{ as } u = 0 \}$$

$$\frac{d^2 f}{dt^2} = [(3)!c/d^4] S^2 + (-2c/d^3) f = (-2c/d^3) (c/d^2)$$

$$\frac{d^3 f}{dt^3} = (2.5 c^2/d^6) u = 0$$

$$\frac{d^4 f}{dt^4} = 0 + (2.5 c^2/d^6) f = (2.5 c^2/d^6) (c/d^2) \text{ and so on.}$$

So, for $k = 2n$

$$\frac{d^{2n} f}{dt^{2n}} = (-1)^{(n+1)} \prod_0^n (3n-1) c^{(n+1)} / d^{(3n+2)}$$

$$F = \lim_{i \rightarrow \infty} m \sum_{n=0}^i \frac{d^{2n} f}{dt^{2n}} \frac{t^{(2n)}}{(2n+1)!}$$

$$F = \lim_{i \rightarrow \infty} m \sum_{n=0}^i (-1)^{(n+1)} \prod_0^n (3n-1) c^{(n+1)} / d^{(3n+2)} \times t^{(2n)} / (2n+1)!$$

$$F = \lim_{i \rightarrow \infty} \frac{m}{d^2} \sum_{n=0}^i (-1)^{(n+1)} \frac{\prod_0^n (3n-1)}{(2n+1)!} (GM)^{(n+1)} \frac{t^{(2n)}}{d^{(3n)}}$$

This is for gravitational field only where force depending upon $\frac{t^2}{d^3}$ (space time) curvature with n^{th} power. Similarly for

electric and magnetic fields also force depends upon $\frac{t^2}{d^3}$ (space time) curvature with n^{th} power.

For electric field on a particle having charge q

$$F = \lim_{i \rightarrow \infty} \frac{q}{d^2} \sum_{n=0}^i (-1)^{(n+1)} \frac{\prod_0^n (3n-1)}{(2n+1)!} (KQ)^{(n+1)} \frac{t^{(2n)}}{d^{(3n)}}$$

And for magnetic field on a particle having magnetic intensity m_2

$$F = \lim_{i \rightarrow \infty} \frac{m_2}{d^2} \sum_{n=0}^i (-1)^{(n+1)} \frac{\prod_0^n (3n-1)}{(2n+1)!} (\mu m_1 / 4\pi)^{(n+1)} \frac{t^{(2n)}}{d^{(3n)}}$$

So, if F is the unified force applied by object (1) (having mass M , electric charge Q , magnetic intensity m_1) upon a stationary object (2) (having mass m , electric charge q , magnetic intensity m_2) whose initial velocity $u = 0$ then

$$F = \lim_{i \rightarrow \infty} \frac{1}{d^2} \sum_{n=0}^i (-1)^{(n+1)} \frac{\prod_0^n (3n-1)}{(2n+1)!} \frac{t^{(2n)}}{d^{(3n)}} \{ m(GM)^{(n+1)} + q(KQ)^{(n+1)} + m_2(\mu m_1 / 4\pi)^{(n+1)} \}$$

$$F = \lim_{i \rightarrow \infty} \frac{1}{d^2} \sum_{n=0}^i C \frac{t^{(2n)}}{d^{(3n)}} \{ m(GM)^{(n+1)} + q(KQ)^{(n+1)} + m_2(\mu m_1 / 4\pi)^{(n+1)} \}$$

Where, a constant $C = \frac{(-1)^{(n+1)} \prod_0^n (3n-1)}{(2n+1)!} = f(n)$

So, conclusion is not only gravity but all kinds of force depend upon space-time curvature.