Finite Element Analysis of Two Stage Gear Pair to Finding Natural Frequencies with Effect of Design Parameters

Dayaram Chouhan¹, Akhilesh Lodwal²
¹M.E Research Scholar, IET DAVV, Indore, India
²Assistant Professor, IET DAVV, Indore, India

Abstract: Gearing is a very important term in automobiles, industrial, production and every place where power transmission requires. Gear is an important machine component in much mechanical power transmission system. It has a wide range of applications because of its high degree of reliability and compactness. Vibration induced by gear is a major problem in much power transmission system and has been widely studied; it is an important topic for further studies in engineering field. Natural frequencies and mode shapes are the important design parameters of a system. Mathematical modelling of system may be done to find the natural frequency & mode shape. In present work, the effects of design parameters on the natural frequencies are investigated.

Keywords: 3D modelling, modal analysis: two stage gear-rotor assembly, natural frequency, mode shape

1. Introduction

Gear transmission has become the most common and important mode in today's mechanical world, due to its advantages such as compact structure, high drive efficiency, accurate transmission ratio and large power transmission range. With the rapid development of automobile, aviation, shipbuilding, mining and other industries, the demand of gear transmission has increased. Vibration is a major problem in many power transmission applications at higher operating speeds, have vibratory excitations is related to the gear transmission error. Most of the mechanical systems are subjected to dynamic loading which induces vibration in gears and leads to crack, fatigue and noise. In general the total effective work for the mechanical system is lowered. Reasons for such behaviour are type of loading, construction and conditions of work, where mechanical system operates. The spur gear is the first choice for gear vibration analysis and parameters such as natural frequencies and vibration mode, can be calculated.

Modal analysis is a technique used to determine, improve and optimize the dynamic behaviours of the engineering structures. It can be used for determining the inherent dynamic characteristics of natural frequencies and mode shapes.

2. Literature Review

Akur Saxena, AnandParey and Manoj Chouksey[2016] studied the inherent dynamic characteristics of gear rotor system in the form of natural frequencies, damping factor and mode shapes using modal analysis. Modal analysis has been done using solid element in Ansys workbench. It is also found that the variation in bearing stiffness, affect the natural frequencies of the system.

FU Shengping, LUO Ning and LI Shengbo [2017], this paper comprehensively and deeply studied the dynamic characteristics under the multi boundary conditions.

ShoyabHussin[2015] studied the torsional vibration characteristic of multi rotor using finite element method. Outcomes is that the natural frequencies for any systems can help to avoid the failure. The results are compared with Holzer and Ansys 14.0 to establish the effectiveness of finite element method.

Edward J. Dielhl and J. Tang [2016] proposed the systematic approach to modelling and analysis of two stage gear box to predict the fault. The research demonstrates that the modelling method in combination with HWT data analysis has the potential for facilitating successful diagnosis for gearbox system.

Ankur Saxena, Anand Parey and Manoj Chouksey [2016] described the dynamic behaviour of the multi mesh geared-rotor system. Modal analysis technique is used to find the natural frequencies and force harmonic response of the system. It has been found that the position of the gear and coupling, affect the gear dynamic behaviour. Also show the effect of bearing stiffness on natural frequencies.

Kadam G. N. and Prof. Bajaj D.S,[2015], to reduce the weight of the gear system, the authors studied the effect of design parameters on natural frequency and vibration mode. To evaluate the alternative design choice, reduction in weight and tune of the system, modal parameters are often altered during the design phase.

WANG Tao, XIE Chen, WANG Feng, HU XIAO-Rui and HU Li-ming [2014], aiming of this paper is that the static linear modal analysis methods fail to meet the working conditions of high and frequent variable speeds. This paper provides the guidance and reference data for design, use and
Jairo Alberto Ruiz-Botero, Juan Fernando Lopez and Hector FabiaQuintero- Riaza [2014], studied the detection of failure in two stage gear box and shows the variation on gear mesh stiffness for different amount of damage.

James Kuria and John Kithiu [2008], described the effect of time varying mesh stiffness, time varying frictional torque on vibration and stress level of multi stage gear box. This model can be used as a tool for optimum gear design parameter for any multistage spur gear train.

J. S.Wu and C.-H. Chen [2001] described a simple approach for eliminating the dependent torsional angles present in the gear branched system. This study also find the influence of shaft mass on the natural frequencies.

3. Methodology

1) Model development

Model of three shafts and two pairs of the gears in mesh is developed. The essential elements of the gear train model shown in fig. 1. Model contains two pairs of gear meshes each with a shaft stiffness, moment of inertia of gears, Moment of inertia of the input and output masses. Equivalent system is shown in fig.2. This yielded a six degree of freedom system which is modelled

Equations of motion for free un- damped vibration are derived-

\[ \ddot{\theta}_k + K_k (\dot{\theta}_k - \dot{\theta}_c) = 0 \]

\[ I_{bc} \ddot{\theta}_{bc} + K_1 (\dot{\theta}_{bc} - \dot{\theta}_c) + K_2 (\dot{\theta}_{bc} - \dot{\theta}_d) = 0 \]

\[ I_{de} \ddot{\theta}_{de} + K_2 (\dot{\theta}_{de} - \dot{\theta}_c) + K_3 (\dot{\theta}_{de} - \dot{\theta}_f) = 0 \]

\[ I_f \ddot{\theta}_f + K_3 (\dot{\theta}_f - \dot{\theta}_d) = 0 \]

Where: \[ I_{bc} = I_c^2 - (G_1)^2 I_c \]

\[ I_{de} = I_d^2 - (G_2)^2 I_d \]

\[ I_f = (G_3)^2 I_f \]

\[ K_1 = (G_1)^2 K_2 \]

\[ K_2 = (G_2)^2 K_3 \]

4. Numerical Solution

Assuming the motion of the form of

\[ \ddot{\theta}_k = A_k \cos \omega t \]

The equations of motion can be arranged in matrix form as,

\[ M \ddot{\theta} + K \theta = 0 \]

Where, \[ [M]=\text{mass matrix}, \]

\[ [K]=\text{stiffness matrix} \]

To find the natural frequencies and mode shapes of the two stage gear transmission system, two methods are used-

(I) Eigen values and Eigenvectors method

\[ |\lambda I - [K]| = 0 \]

Where, C=[M]^{-1}[K], dynamic matrix and \( \lambda = \omega^2 \)

Mass matrix,

\[ [M]= \begin{bmatrix} I_c & 0 & 0 & 0 \\ 0 & I_{bc} & 0 & 0 \\ 0 & 0 & I_{de} & 0 \\ 0 & 0 & 0 & I_f \end{bmatrix} \]

Stiffness Matrix, \[ [K]= \begin{bmatrix} K_1 & -K_1 & 0 & 0 \\ -K_1 & (K_1 + K_2) & -K_2 & 0 \\ 0 & -K_2 & (K_2 + K_3) & -K_3 \\ 0 & 0 & -K_3 & K_3 \end{bmatrix} \]

Solution is done by using MATLAB Code to find the Natural frequencies and mode shapes.

(II) Holzer’s Method,

For SHM we may substitute, \( -\omega^2 \theta = \ddot{\theta} \) in the governing equations and by assuming the suitable value of \( \omega \) and \( \theta_c = 1 \)
we get the deflections-
\[ \theta_a = 1 \]

\[ \theta_{bc} = \theta_a - (I_a \theta_a) \omega^2 / K_1 \]

\[ \theta_{de} = \theta_{bc} - (I_a \theta_e + I_p \theta_{bc}) \omega^2 / K_2 \]

\[ \theta_f = \theta_{de} - (I_a \theta_e + I_p \theta_{de}) \omega^2 / K_3 \]

If \( \sum l \omega^2 \theta = 0 \) then we get the natural frequency

### III) Finite Element Analysis

The spur gears are sketched, modelled and assembled in Creo-2.0. The IGES assembly file is imported to the finite element software (Ansys 16.0) for model analysis. By define contacts, meshing and applying proper boundary conditions and solve, we get the natural frequencies and mode shapes of the two stage geared system.

![Figure 3: Model of Two Stage Gear System](image)

### 5. Results and Discussion

1) **Comparison of Natural Frequencies**

![Figure 5: Model Solution](image)

2) **Natural Frequencies:**

<table>
<thead>
<tr>
<th>S.No</th>
<th>Holzer Method</th>
<th>Eigen Method</th>
<th>Ansys Holzer-Ansys</th>
<th>Eigen-Ansys</th>
<th>Holzer-Eigen</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>58</td>
<td>32</td>
<td>33.3</td>
<td>33.3</td>
<td>33.3</td>
</tr>
<tr>
<td>2</td>
<td>1253</td>
<td>948.6</td>
<td>707.57</td>
<td>707.57</td>
<td>707.57</td>
</tr>
<tr>
<td>3</td>
<td>2370.4</td>
<td>2288.5</td>
<td>2260.8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>2990.4</td>
<td>2473.2</td>
<td>2276.5</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Mode Shapes:** Following Mode Shapes were obtained at different natural frequencies of the system. The calculations were done on MATLAB program.

![Mode Shapes](image)

### 6. Conclusion

The mathematical modal was developed to analyse the vibration characteristics of two stage gear transmission. The modal consists four equations of motion, which were solved using Eigenvalue & Eigenvector and Holzer’s method. Modal analysis was done in finite element software (Ansys 16.0). Parametric studies were also conducted to examine the effect of two design variables, module and pressure angle. The following specific conclusions can be drawn from the study:

1) The results of natural frequencies and mode shapes are reported.
2) Increasing the module from 2.0 to 2.5 and 3.0, decrease the natural frequencies.
3) Increasing the pressure angle of the gears from 14.5˚ to 20˚, increase the natural frequencies.
4) This type of study may be helpful in understanding modal behaviour of geared branched system and for proper gear design as per our requirement.

### References


**Author Profile**

**Mr. Akhilesh Lodwal** working as Assistant Professor of Mechanical Engineering Department in the Department at IET DAVV INDORE. His areas of research is Design Engineering. He is having 13 years of teaching experience.

**Mr. Dayaram Chouhan** is a lecturer at Govt. Polytechnic College, Jhabua. He is having 8 years of teaching experience. He presently is a M. E, research scholar at IET DAVV, Indore.