

Analytical and Numerical Investigation of Mixed Convection Flow and Boundary Layer Control of a Nano Fluid with Heat Generation

Raj Kumar¹, Valmeti Sudheer²

¹M.Tech in Thermal Engineering from CMR Engineering College, JNTU, Hyderabad, Telangana, India

²Professor, CMR Engineering College, JNTU, Hyderabad, Telangana, India

Abstract: In this project, boundary layer mixed convection fluid flow, heat transfer generation of a Nano fluid over a semi-infinite flat plate of 50*10*2mm with heat generation effects are investigated analytically. The velocity, Nusselt number, Reynolds number, entropy, heat transfer coefficient profiles as well as skin friction and heat transfer rates are determined for different Prandtl number 0.01, 0.1, 1, 10, 100 for different Nano fluids. The base fluid water is mixed with Nano particles of Aluminium oxide, Copper Oxide with different volume fractions 0.4 & 0.6 are considered. The properties of the Nano fluids are calculated theoretically. CFD Fluent analysis is done in ANSYS. The boundary condition for CFD analysis is velocity of fluid which is calculated for different Prandtl number and mixed convection values.

Keywords: Nano particles, Aluminium oxide, Copper Oxide, Ansys

1. Introduction and Literature Survey

In the paper by M.Chandrasekar, M. S. Kasiviswanathan [1], is focused on the numerical solution of steady MHD mixed convection boundary layer flow of a nanofluid over a semi-infinite flat plate with heat generation/absorption and viscous dissipation effects in the presence of suction and injection. In The Paper by SatyajitMojumder [2]; A lid-driven L-shaped cavity filled with a porous medium is analyzed. The Galerkin weighted residual method is applied to obtain numerical solutions. The effect of the Reynolds number ($Re = 1-100$), Grashof number ($Gr = 10^3-10^5$) and Darcy number ($Da = 10^{-5}-10^{-3}$) on the velocity and temperature fields is examined. For the vertical wall, a higher heat transfer rate is observed when a low Grashof number, higher Darcy number and higher Reynolds number are applied, but the opposite characteristic is found in the horizontal wall. It is evident that heat transfer decreases up to 63% in the horizontal wall when the flow has a high Reynolds number ($Re = 100$).

Objective of this paper

- Two fluids Aluminium oxide and Copper oxide are mixed with base fluid water with different volume fractions 0.4 & 0.6. The properties of fluid Viscosity, Density, Thermal Conductivity and Specific heat are calculated theoretically.
- The boundary conditions for CFD analysis are velocity of fluid and mixed convection values. The velocities are calculated for different Prandtl numbers 0.01, 0.1, 1, 10 & 100.
- The outputs determined are outlet velocities, Reynolds number, nusselt number, heat transfer coefficient, skin friction coefficient and heat transfer rates.

2. Proposed Nano Fluid Properties and Calculations

The properties of the Aluminium oxide and Copper oxide Nano fluids mixed with base fluid water are calculated for different volume fractions 0.4 & 0.6 of both fluids.

Formulae: (Quoted from Journals)

Density (ρ):

$$\rho_{nf} = \phi \rho_s + (1-\phi) \rho_w$$

Where

ρ_{nf} = Density of Nano fluid

ρ_s = Density of the substance (Al_2O_3 or CuO)

ρ_w = Density of Base fluid (Water)

ϕ = Volume fraction of the substances

Specific Heat (C_p):

$$C_{p(nf)} = \phi (C_{ps}) + (1-\phi) C_{pw}$$

Where $C_{p(nf)}$ = Specific Heat of Nano fluid

C_{ps} = Specific Heat of the substance (Al_2O_3 / CuO)

C_{pw} = Specific Heat of Base fluid (Water)

Thermal Conductivity (K):

$$K_{nf} = \frac{K_s + 2K_w + 2(K_s - K_w)(1+\beta)^3 \times \phi}{K_s + 2K_w - (K_s - K_w)(1+\beta)^3 \times \phi} \times K_w$$

Where K_{nf} = Thermal conductivity of Nano fluid ;

K_s = Thermal conductivity of the substance (Al_2O_3 / CuO)

K_w = Thermal conductivity of Base fluid (Water)

β = Film temperature

Viscosity (μ):

$$\mu_{nf} = Pr^* \frac{k_{nf}}{c_{p(nf)}}$$

Where Pr = Prandtl number

Velocity Calculations by Varying Prandtl Number

Velocities are calculated for different Prandtl number, which is used as inlet in the CFD analysis.

Volume 6 Issue 8, August 2017

www.ijssr.net

Licensed Under Creative Commons Attribution CC BY

$$Pr = \frac{c_p \mu}{k}$$

$$\mu = \frac{Pr k}{c_p}$$

$$v = \frac{\mu}{\rho}$$

$$\frac{Re v}{L} = u(\text{velocity})$$

Re = Reynolds number

v = kinematic Viscosity (m^2/s)

L = length of the component (m)

CFD Analysis

CFD analysis is done on the plate by applying velocity of fluid and using mixed convection flow to determine outlet velocities, Reynolds number, entropy, Nusselt number, Heat transfer coefficient, skin friction coefficient and heat transfer rates.

**Aluminum Oxide (Al_2O_3) with VF - 0.4
Prandtl Number: 0.01**

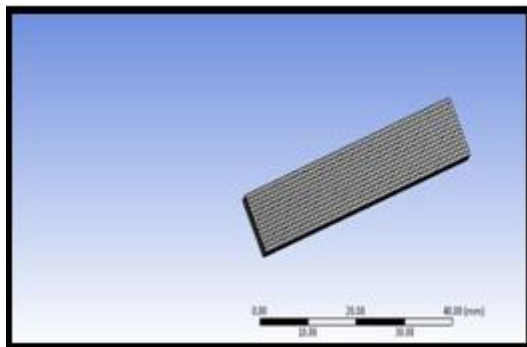


Figure 1: Meshed model

Viscous → edit → k- epsilon

Select Viscous Model – Laminar

Boundary conditions → select air inlet → Edit → Enter Inlet Velocity

The velocity values are calculated from the Prandtl number. The mixed convection is considered for the analysis. In wall, select thermal and select Mixed option. Enter heat transfer coefficient of water and free stream temperature.

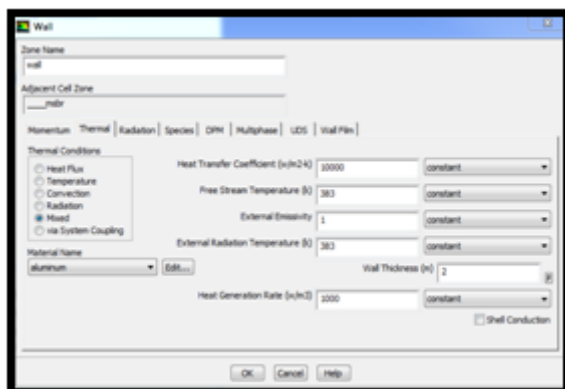


Figure 2: Velocity Inlet for Aluminum oxide with VF 0.4 at Pr = 0.01

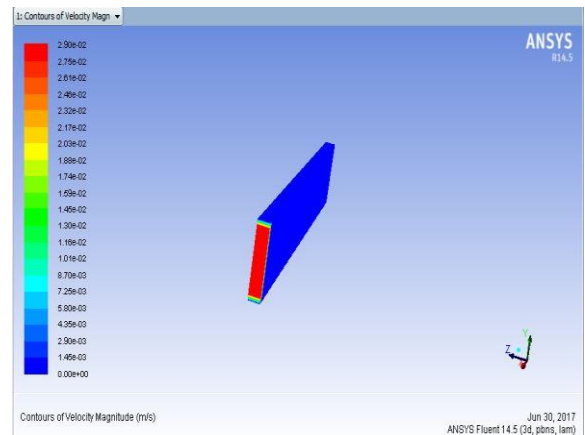


Figure 3: Velocity value for Aluminum oxide with VF 0.4 at Pr = 0.01

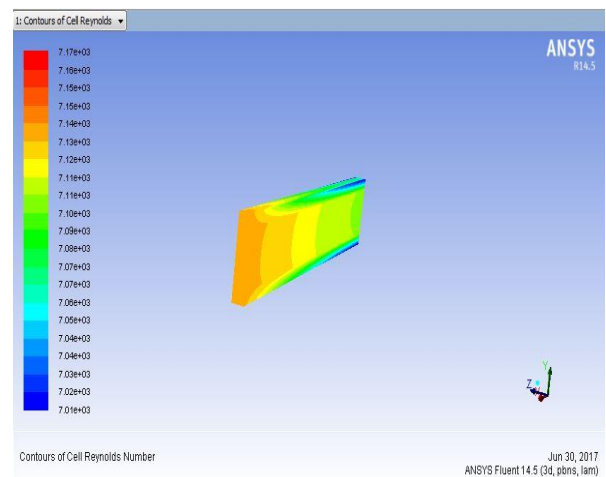


Figure 4: Reynolds number for Aluminum oxide with VF 0.4 at Pr = 0.01

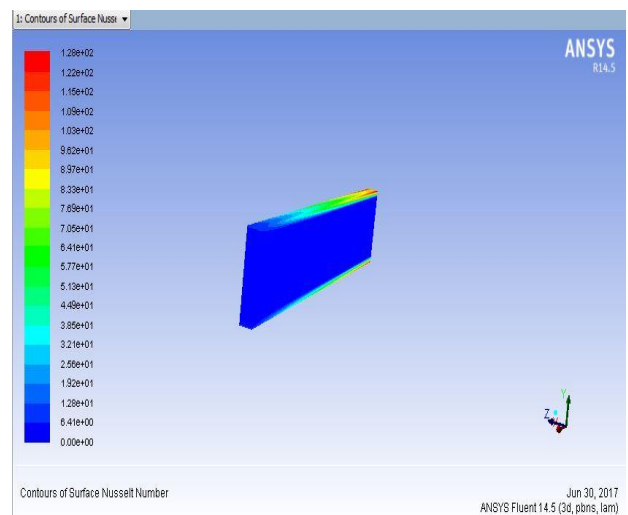


Figure 5: Nusselt number for Aluminum oxide with VF 0.4 at Pr = 0.01

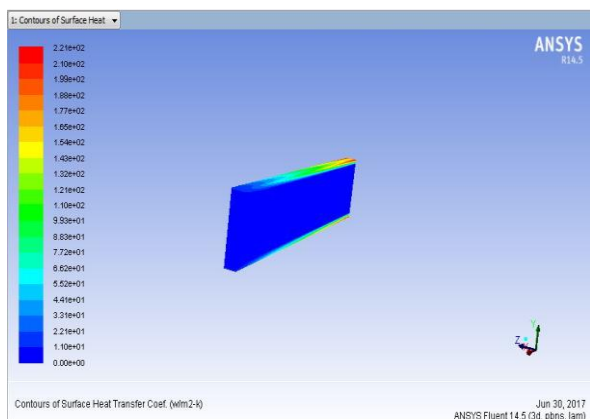


Figure 6: Velocity value for Aluminium oxide with VF 0.4 at Pr = 0.01

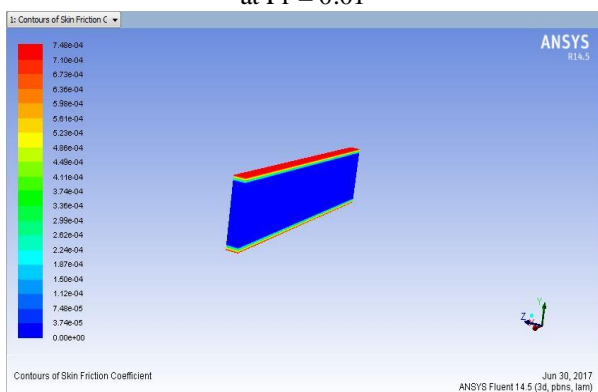


Figure 7: Skin friction coefficient for Aluminium oxide with VF 0.4 at Pr = 0.01

Total Heat Transfer Rate (W)	
inlet	253.23094
outlet	-77.108101
wall	0.83091736
wall-nsbr	-176.96509
Net	-0.011329651

Figure 8: Skin friction coefficient for Aluminum oxide with VF 0.4 at Pr = 0.01

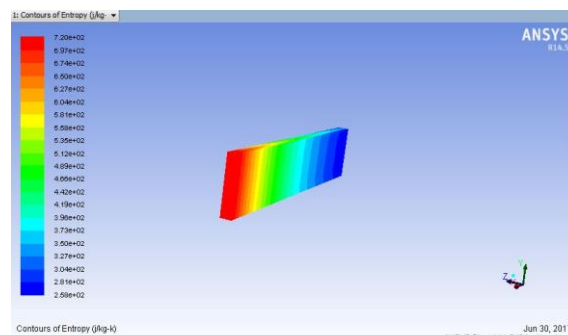


Figure 9: Entropy for Aluminum oxide with VF 0.4 at Pr = 0.01

3. Results & Discussions

Fluid = Al_2O_3 (0.4)

Table 1: Resultant Parameters of the Aluminium oxide Nanofluid @ VF 0.4

Results	Prandtl Number				
	0.01	0.1	1	10	100
Velocity (m/s)	2.90E-02	2.95E-01	2.95E+00	2.95E+01	2.95E+02
Reynolds number	7.17E+03	7.30E+03	7.30E+03	7.30E+03	7.30E+03
Nusselt number	1.28E+02	1.93E+01	7.99E+00	6.87E+00	6.76E+00
Heat Transfer Coefficient ($\text{W/m}^2\text{-k}$)	2.21E+02	3.32E+01	1.37E+01	1.18E+01	1.16E+01
Skin friction coefficient	7.48E-04	7.61E-02	7.61E+00	7.61E+02	7.61E+04
Entropy (J/kg-k)	7.20E+02	7.26E+02	7.27E+02	7.27E+02	7.27E+02
Total heat transfer rate (W)	0.011329651	0.08340928	0.078575537	1.857763	8.6138779

Graphs

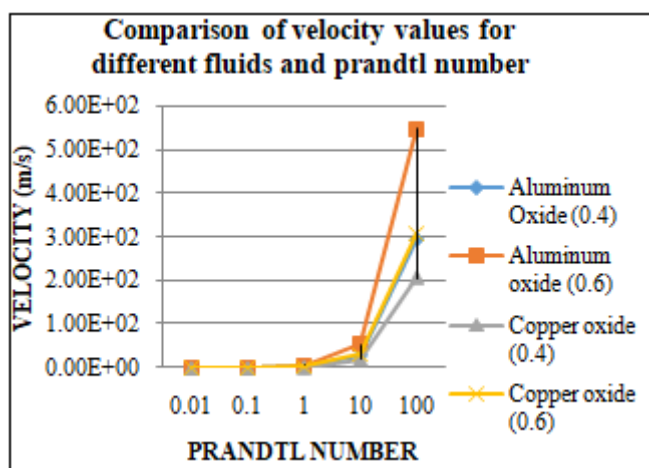


Figure 10: Comparison of velocity values for different fluids and Prandtl number

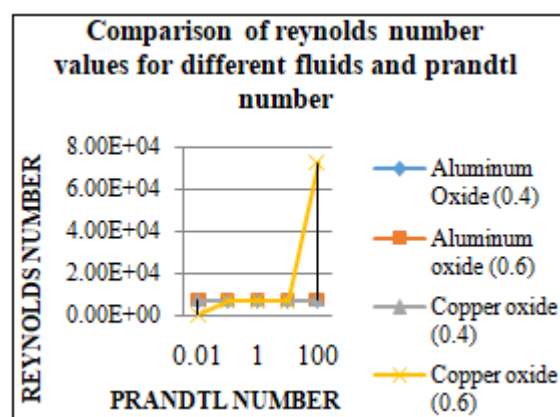


Figure 11: Comparison of Reynolds number for different fluids and Prandtl number

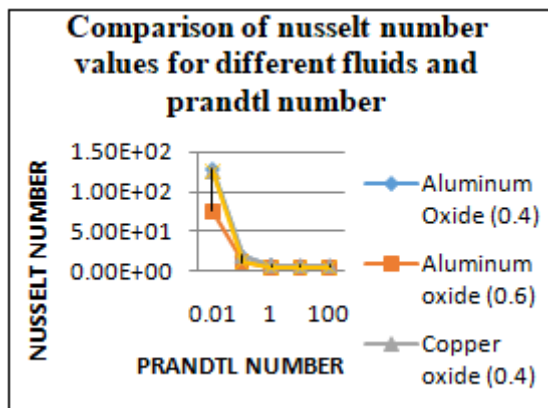


Figure 12: Comparison of Nusselt number for different fluids and Prandtl number

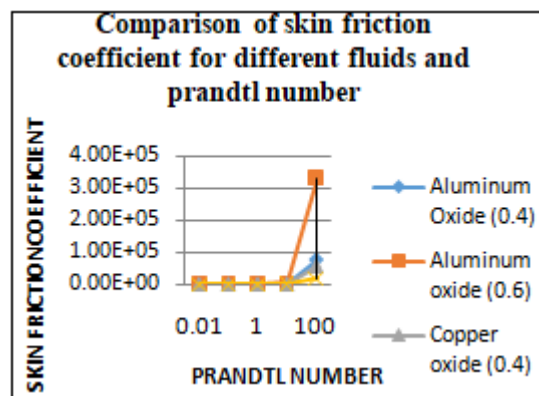


Figure 15: Comparison of Skin Friction Coefficient for different fluids and Prandtl number

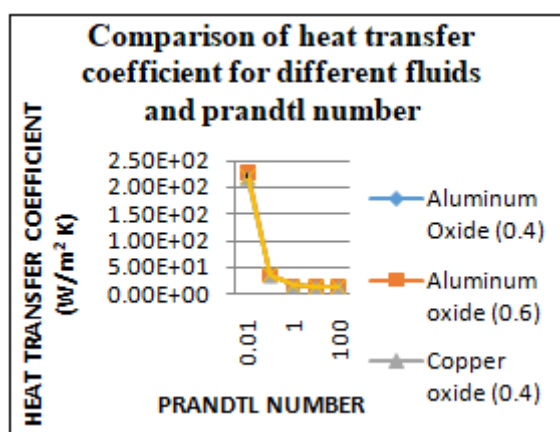


Figure 13: Comparison of Heat Transfer Coefficient for different fluids and Prandtl number

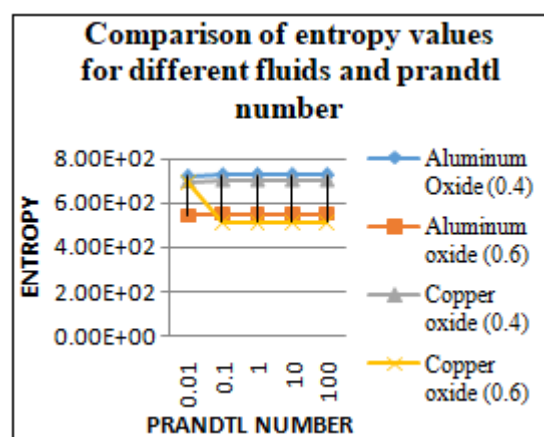


Figure 16: Comparison of Entropy values for different fluids and Prandtl number

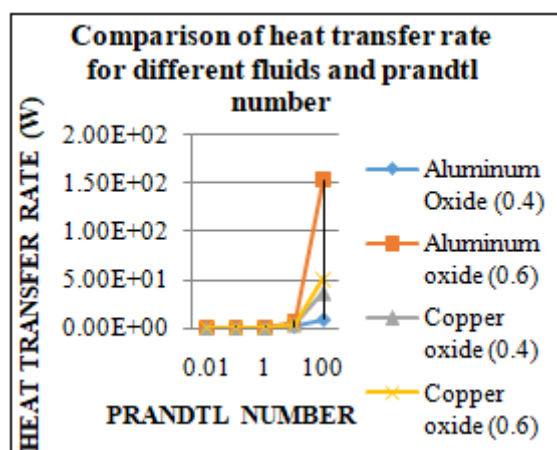


Figure 14: Comparison of Heat Transfer Rate for different fluids and Prandtl number

4. Conclusion and Future Scope

From the analysis results, it is observed that the heat transfer increases with the values of Prandtl number. Since the higher Prandtl number has very low thermal conductivity, the local Nusselt number increases rapidly. This means that the variation of the heat transfer rate is more sensitive to the larger Prandtl number than the smaller one. Skin friction coefficient is also increasing with increase of Prandtl number. Taking volume fractions and comparing the results between Al_2O_3 nano fluid and CuO nano fluid, the velocities are not affected by the change in volume fractions of nano fluids. Reynolds number and Heat Transfer Rate, Nusselt number and Heat Transfer coefficient are increasing with increase of volume fraction. The values are more when Copper oxide is used. The Heat transfer rate is more when Aluminum oxide is used. The entropy values does not effect with the change in Prandtl number. It is increasing with decrease in volume fraction. This work can be extended by performing experimental investigations and validating, considering other nano fluids and volume fractions.

References

- [1] M.Chandrasekar, M.S.Kasisviswanathan, Magnetohydrodynamic mixed convection flow and boundary layer control of a nanofluid with heat generation/absorption effects, Volume 6, Issue 6, June (2015), pp. 18-32, Article ID: 30120150606003,

International Journal of Mechanical Engineering and Technology

- [2] SatyajitMojumder, Numerical study on mixed convection heat transfer in a porous L-shaped cavity.
- [3] SadiaSiddiq, Mixed Convection Boundary Layer Flow over a Vertical Flat Plate with Radiative Heat Transfer.
- [4] Md. Kamrujjaman, Mixed Convection Flow Along a Horizontal Circular Cylinder with Small Amplitude Oscillation in Surface Temperature and Free Stream.
- [5] Mohsen Sheikholeslami, Numerical simulation of MHD nanofluid flow and heat transfer considering viscous dissipation.
- [6] M. Hatami, Analytical investigation of MHD nanofluid flow in a semi-porous channel
- [7] M. Gorji-Bandpy, Numerical investigation of MHD effects on Al_2O_3 -water nanofluid flow and heat transfer in a semi-annulus enclosure using LBM.
- [8] DavoodDomiriGanji, Nanofluid flow and heat transfer between parallel plates considering Brownian motion using DTM.
- [9] UzmaShaheen, Marangoni, Mixed convection flow with Joule heating and nonlinear radiation.
- [10] A. Aghaei, Numerical Investigation of Mixed Convection Fluid Flow, Heat Transfer and Entropy Generation in Triangular Enclosure Filled with a Nanofluid.