

Theorem (2.4) If $f : x \rightarrow y$ is lower weakly semi-precontinuous, for every fuzzy pre- semiopen set V in $F(v)$ \dot{C} SPint $F(SCIV)$.

Theorem (2.5) Iff $: x \rightarrow y$ is fuzzy upper weakly semi-precontinuous for every fuzzy pre-semiopen set V in Y , $F(V) \dot{C}$ SPint $F(SCIV)$.

Theorem(2.6) If $f : x \rightarrow y$ is fuzzy lower weakly semi-precontinuous on X ,Then SPCL $f(V) \dot{C}$ $F(SCLV)$ for any fuzzy open set V in Y .

Theorem (2.7) If $f: x \rightarrow y$ is fuzzy upper weakly semi-precontinuous on X , Then SPCL $f(V) \dot{C}$ $F(SCLV)$ for any fuzzy open set V in Y .

Theorem (2.8) Let $f : x \rightarrow y$ is fuzzy multifunction then following are equivalent :

- (a) F is lower weakly semi-precontinuous.
- (b) For any fuzzy open set V in $Y, F(V) \dot{C}$ SP int $F(SCLV)$ int $F(SCLV)$ and $F(V) \dot{C}$ $F(SCLV)$.

Theorem (2.9) Let $f : x \rightarrow y$ is fuzzy lower weakly semi-precontinuous if for each fuzzy open $V, F(SCLV)$ is fuzzy semi pre-open set.

Definition(2.2) For a fuzzy multifunction $f : x \rightarrow y$ the $F^-(A)$ and $F^+(A)$ of a fuzzy set λ in Y are defined as follows:
 $F^-(\lambda) = \{x \in X : F(x) \leq \lambda\}$
 $F^+(\lambda) = \{x \in X : F(x) \geq \lambda\}$

Definition (2.3) A fuzzy multifunction $f: (x, \tau) \rightarrow (y, \sigma)$ is said to be :

- (a) Fuzzy upper continuous at a point x of X for any fuzzy open set λ of Y such that $F(x) \leq \lambda$ there exist $u \in \tau$ containing x such that $F(u) \leq \lambda$ for all $u \in U$.
- (b) Fuzzy upper continuous at a point x of X for any fuzzy open set λ of Y such that $F(x) \geq \lambda$, there exist $u \in \tau$ containing x such that $F(u) \geq \lambda$ for all $u \in U$.
- (c) For upper (resp.fuzzy lower) continuous if it is fuzzy upper (resp.lower) continuous at every point of X .

Definition (2.4): A fuzzy multifunction $f : x \rightarrow y$ is called:

- (a) A fuzzy lower weakly α -continuous at a point $x \in X$ if for every fuzzy open set λ in Y with $x \in F^+(\lambda)$. There exist a nbd u of x_0 in X such that $U \dot{C} F^-(\text{Cl}(\lambda))$
- (b) A fuzzy upper weakly α -continuous at a point $x \in X$ if for every fuzzy open set λ in Y with $x \in F^-(\lambda)$. There exist a nbd u of x_0 in X such that $U \dot{C} F^+(\text{Cl}(\lambda))$

3. Lower and Upper Weakly α -Continuous Fuzzy Multifunctions

Definition (3.1): For a fuzzy multifunction $f : x \rightarrow y$ is called:

- (a) Fuzzy lower weakly α -continuous at a point $x \in X$ if for every fuzzy open set λ in Y with $x \in F^+(\lambda)$. There exist a α -nbd u of x_0 in X such that $U \dot{C} F^-(\alpha(\text{cl}(\lambda)))$.

- (b) Fuzzy lower weakly α -continuous at a point $x \in X$ if for every fuzzy openset λ in Y with $x_0 \in F^+(\lambda)$. There exist a α -nbd u of x_0 in X such that $U \dot{C} F^-(\alpha(\text{cl}(\lambda)))$.
- (c) Fuzzy lower weakly α -continuous on X if it is respectively so as each $x_0 \in X$.
- (d) Fuzzy weakly α -continuous on X if it is fuzzy lower weakly α - continuous and fuzzy upper weakly continuous.

Theorem (3.1) Let $f : x \rightarrow y$ is fuzzy multifunction, Then following are equivalent:

- (a) F is fuzzy weakly α -continuous.
- (b) For any fuzzy open set in $Y, F^-(\lambda) \dot{C} \alpha \text{ int } F^-(\alpha(\text{cl}(\lambda)))$.

Proof: Evident.

Theorem (3.2): Let $f : x \rightarrow y$ is fuzzy lower weakly α -continuous if for each fuzzy open set $\lambda, F^-(\text{cl}(\lambda))$ is fuzzy α -open set.

Proof: Straight forward.

References

- [1] Ajamal N and Sharma R.D.Fuzzy subcontinuity inverse fuzzy subcontinuity and a new category of fuzzy topological spaces. Fuzzy sets and systems,73(1995),13-24.
- [2] Chang C.L.Fuzzy topological spaces J.Math.Anal.24(1968),182-190.
- [3] Ekici.E.On some types of continuous functions,Appl.Math.E-Not 4(2004),21-25.
- [4] Ewert J. On normal fuzzy topological spaces ,Mathematics,31(54)(1989),39-45.
- [5] Ewert J.Fuzzy valued maps ,Math,Nachr,137(1998),79-87.
- [6] Mukherjee, M.N. and Malakar,S.,On almost continuous and weakly continuous fuzzy multifunctions,Fuzzy sets and Systems,41(1991),113-125.
- [7] Nanda S. On Fuzzy topological spaces, Fuzzy Sets Systems 42(1991),259-262.
- [8] Papageorgiou, N.S,Fuzzy topology and fuzzy multifunctions, jour.Math.Anal,Appl, 109(1985),397-425..
- [9] Thakur S.S.and Malviya R, Pairwise fuzzy irresolute mappings, Math Bohemica 121(3)(1996),273-280.
- [10] Zadeh A.Fuzzy sets ,Inform and Control,8(1965),338-358.