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A Feedback Based Closed Loop Circuit to Control Chaos in Nonlinear Circuits

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Abstract: This paper presents a simple circuit for control of chaos in nonlinear oscillator circuit. Numerical and circuit simulation results are used to visualize and illustrate the effectiveness of chaos control. Duffing Holmes oscillator circuit is considered as a nonlinear circuit.

Keywords: nonlinear dynamic, suppression of chaos, chaos control, Duffing Holmes oscillator, coupling.

1. Introduction

Over the past few decades, the complex and chaotic behavior of nonlinear dynamic system has attracted the attention of many researchers, scientists and engineers in both the academic area and industry. Most of the electronic/ electrical devices are nonlinear in nature that shows chaotic behavior. There are some practical situations where one needs to improve the performance of a dynamical system by avoiding / controlling chaos.

The deterministic chaos seems to explain many natural phenomena and there has been growing interest to use chaos profitably by synchronizing chaotic orbits [1] [2] due to its potential application in communication [3][4][5][6][7]. However, in many situations chaos is undesirable phenomenon, which may lead to irregular operation in physical systems. Thus from a practical point of view one would like to convert chaotic solutions into periodic or limit cycle solutions.

The strategies for the control of chaos can be classified into two main classes, which involve either stabilizing or suppressing chaos. The first category of methods includes the control of chaos by stabilizing the unstable periodic orbits embedded in a chaotic attractor such as OGY [8], proportional feedback [9], occasional proportional feedback [10] [11], continuous feedback [12] [13], delayed continuous feedback [14][15][16], extended delayed continuous feedback [17] and pulsed proportional feedback [18]. The second category of methods includes the control of chaos by converting chaotic behaviour into any one of the desired periodic behaviour exhibited by the system such as adaptive control algorithm [19] [20], parametric perturbation [21], using second periodic force [22], weak feedback control [23], addition of noise [24] and constant feedback [25], etc. The algorithms used for control of chaos have also been classified into closed loop or feedback methods [26] [9] and open loop or non-feedback methods [21]. In a closed loop method the perturbation is based upon the prior knowledge of the state of the system whereas in a open loop method the perturbation is independent of the knowledge of the state of the system.

Patidar et al [27] presented a simple method to control chaotic oscillations of systems described by second or third order nonlinear differential equations. Their method was a closed loop or feedback method and can be classified as a suppressing chaos algorithm, as it converts chaotic behavior into a desired periodic behavior. They do not require any prior knowledge of the system dynamics, such as location of unstable periodic orbits, periodic orbits or stable fixed points. They only required a weak periodic oscillator of the same kind as the chaotic oscillator. They introduced a mutual coupling between the state variables of both chaotic and weak periodic oscillators. They have introduced a new parameter called coupling strength to control the mutual coupling between the chaotic and weak periodic oscillators.

Based on the literature review it is observed that the feedback control method is one of the most effective methods of chaos control. The algorithm given by [27] is one of the effective methods for the chaos control. The work presented in this paper proposes a new circuit based on the algorithm introduced by [27] for control of chaos in Duffing Holmes oscillator circuit. The effectiveness of the proposed work is illustrated through matlab simulation and PSpice circuit simulation.

2. Duffing Holmes Oscillator Circuit [28]

The Duffing-Holmes oscillator is given either by the second order nonautonomous differential equation [26][29][30][31]:

$$\ddot{x} + b\dot{x} - x + x^3 = a\sin\omega t \tag{1}$$

or by an equivalent set of two first order nonautonomous equations

$$\dot{x} = y \tag{2a}$$

$$\dot{y} = F(x) - b y + a \sin \omega t$$
 (2b)

with $F(x) = x - x^3$. In (1) and (2) b, a, and ω are the damping coefficient, the amplitude and the frequency of the external driving force, respectively.



Figure 1: Duffing Holmes Oscillator Circuit

Differential equations describing the circuit can be easily obtained using the Kirchhoff's laws: -

$$c \frac{dVc}{dt} = I_L,$$

$$L \frac{dI_L}{dt} = F_E(Vc) - I_L R + A\sin(\omega t - \pi)$$

where, Vc is the voltage across the capacitor C and I_L is the current through the inductor L.

$$F_{E}(Vc) = -(Vc+kV^{*}), \text{ for } Vc < V$$

= (k-1) Vc, for -V \leq Vc \leq V*
= -(Vc-kV^{*}), for Vc>V*

where k = (R2/R1) + 1 is the gain of the amplifying stage and V* is the voltage drop across an opened diode (for silicon diode V* = 0.5V at 0.1mA).

3. Chaos Control

The schematic representation of an algorithm used for suppression of chaos is shown in Fig. 2. It is a two oscillator system in which one is a chaotic which is to be suppressed and another one is a weak periodic but of the same kind of the chaotic oscillator. Here the mixing of signals is controlled by coupling strength parameter (c). In this algorithm the mixing of signals is bidirectional i.e. the percentage of mixing depends upon the value of mutual coupling strength (i.e. if c =0.5 then the percentage of mixing will be only 50%).



Figure 2: Schematic representation of the algorithm for suppression of chaos.

We have constructed an analog circuit equivalent to the schematic representation of the algorithm for suppression of chaos given in Fig. 2 with Duffing Holmes Oscillators as chaotic oscillator and periodic oscillator by using conventional operational amplifiers and diodes, which is shown in Fig. 3.



Figure 3: Circuit Diagram for the control of chaos in Duffing-Holmes oscillator

The circuit is constructed using conventional operational amplifiers and diodes. The operational amplifiers used are op-amp μ A741C and diodes used are D1N4148. The values of various resistors, inductors and capacitors used in the circuit are as given below: -

R1 = R2 = R3 = R7 = R10 = R11 = R12 = $R16 = 10k\Omega, R4 = R13 = 20\Omega, R8 = R9 =$ $R17 = R18 = 1k\Omega, Variable resistors: R5 =$ $R6 = R14 = R15 = 10k\Omega, L1 = L2 =$ $19mH \text{ and } C1 = C2 = 470nF. \text{ Here } c = \frac{R6}{R7} =$ $\frac{R15}{R16} \text{ and } (1 - c) = \frac{R6}{R5} = \frac{R15}{R14}$

4. Simulation Results

We present the results of PSpice simulation study and their comparison with the numerical results in Fig. 4 – Fig. 8. When c=0, the circuit of Fig. 3 behaves as normal Duffing Holmes Oscillators. In these figures we can see that for different forcing amplitudes it generates chaotic signals. These chaotic signals are suppressed by mixing (as per the algorithm) a very small periodic signal generated by another Duffing Holmes Oscillator with small forcing amplitude of 0.005V. The numerical results are obtained by using the damping coefficient and the frequency of the external driving force as b = 0.1 and $\omega = 1.3$ respectively for different values of forcing amplitude F, at which chaotic signals are generated.





We can see in Fig. 4, the chaotic signal generated at forcing amplitude F = 0.2 ((a) and (b)) is suppressed by mixing of

signals with 20% coupling strength parameter (c) as shown in figures (c) and (d).



Figure 5: Phase Plots (x vs x i.e. x on Y-axis and x on X-axis): (a) and (c) are Numerical Simulation Result and (b) and (d) are PSpice Simulation Result.

We can see in Fig. 5, the chaotic signal generated at forcing amplitude F = 0.22 ((a) and (b)) is suppressed by mixing of signals with 25% coupling strength parameter (c) as shown in figures (c) and (d).



Figure 6: Phase Plots (\dot{x} vs x i.e. \dot{x} on Y-axis and x on X-axis): (a) and (c) are Numerical Simulation Result and (b) and (d) are PSpice Simulation Result.

We can see in Fig. 6, the chaotic signal generated at forcing amplitude F = 0.24 ((a) and (b)) is suppressed by mixing of signals with 25% coupling strength parameter (c) as shown in figures (c) and (d).



Figure 7: Phase Plots (x vs x i.e. x on Y-axis and x on X-axis): (a) and (c) are Numerical Simulation Result and (b) and (d) are PSpice Simulation Result.

We can see in Fig. 7, the chaotic signal generated at forcing amplitude F = 0.35 ((a) and (b)) is suppressed by mixing of signals with 38% coupling strength parameter (c) as shown in figures (c) and (d).



Figure 8: Phase Plots (\dot{x} vs x i.e. \dot{x} on Y-axis and x on X-axis): (a) and (c) are Numerical Simulation Result and (b) and (d) are PSpice Simulation Result.

We can see in Fig. 8, the chaotic signal generated at forcing amplitude F = 0.45 ((a) and (b)) is suppressed by mixing of signals with 40% coupling strength parameter (c) as shown in figures (c) and (d).

5. Conclusion

In this paper we propose a new circuit to control chaos in nonlinear circuits. Using Duffing Holmes Oscillator as nonlinear circuit, we have demonstrated in numerical and PSpice simulations that chaos can be controlled in nonlinear circuit. We have observed that by varying mutual coupling strength we can control chaos obtained at various external forcing amplitude.

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