Ramifications of SS Method

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Abstract: This paper discusses about ramifications of SS method as propounded by A. Seethalakshmy and Dr. N. Srinivasan (2016)^[2] SS method does not give optimal solution in some transportation problems whereas MODI method^[1] proves itself effective invariably in all cases. Two counter examples are given in this paper to prove this assertion.

Keywords: Transportation problem, optimal solution, transportation cost, SS method, MODI method

1. Introduction

As by Hamdy.A.Taha[3],Transportation problem deals with transportation of single commodity from fixed number of sources to a fixed number of destinations ,given the level of supply at each source , amount of demand at each destination and the unit transportation cost of the commodity from each source to each destination. The objective of the transportation problem is to determine the amount to transported from each source to each destination, such that the total transportation cost is minimized.

Transportation problem can be represented as a LPP as follows

Minimize : Z =

 $\sum_{i=1}^{m} \sum_{j=1}^{n} cij xij$ Subject to $\sum_{j=1}^{n} xij \le ai, i=1,2,3....m$ $\sum_{i=1}^{m} xij \ge bj, j=1,2,3....n$

 $X_{ij} \ge 0$ for all i,j

i=1,2,3...,m is the set of sources.

J=1,2,3,...n is the set of destinations.

ai = availability of material at ith source.

 b_j = requirement of material at J^{th} destination

cij =cost of transportation of one unit of material from ith source to jth destination.

xij = number of units of material to be transported from ith source to jth destination.

2. Numerical Examples

Example 1: Transportation model of problem is given below

Sources	D	Е	F	G	Н	supply
Α	8	8	9	4	3	800
В	5	8	5	11	6	500
С	8	9	7	3	3	900

Requirements 400 350 300 250 900 2200

Solution of transportation problem using MODI method Optimal solution of the problem by MODI method is represented in the following table

Destinations						
	D	Е	F	G	Н	supply
Α	8	8(350)	9	4	3(450)	800
В	5 ₍₄₀₀₎	8	5 ₍₁₀₀₎	11	6	500
С	8	9	$7_{(200)}$	$3_{(250)}$	$3_{(450)}$	900

Req. 400 350 300 250 900

Total transportation cost

8*350+3*450+5*400+5*100+7*200+3*250+3*450 =Rs. 10,150

Solution of transportation problem using the SS method Optimal solution of transportation problem by SS method is represented in the following table

Destinations						
Source	D	Е	F	G	Н	Supply
Α	8	8	9	4	$3_{(800)}$	800
В	5 ₍₄₀₀₎	8	5 ₍₁₀₀₎	11	6	500
С	8	9 ₍₃₅₀₎	7(200)	3(250)	3(100)	900
Req.	400	350	300	250	900	2200

Total transportation cost

=3*800+5*400+5*100+9*350+7*200+ 3*250+3*100 =Rs. 10,500

Example 2: Transportation model of a problem is given below

Destinations						
Source	D1	D2	D3	D4	Supply	
S1	6	1	9	3	70	
S2	11	5	2	8	55	
S3	10	12	4	7	90	
Req.	85	35	50	45	215	

Optimal solution of the problem by MOD1 method is represented in the following table.

Destinations						
Source	D1	D2	D3	D4	Supply	
S1	6(40)	$1_{(30)}$	9	3	70	
S2	11	5(5)	$2_{(50)}$	8	55	
S3	10(45)	12	4	$7_{(45)}$	90	
Req.	85	35	50	45	215	

Total transportations cost

=6*40+1*30+5*5+2*50+10*45+7*45 =Rs.1,160.

Optimal solution of the problem by SS method is represented in the following table.

Destinations

Source	D1	D2	D3	D4	Supply
S1	6	1(35)	9	3(35)	70
S2	11	5	$2_{(50)}$	8(5)	55
S3	10(85)	12	4	7(5)	90
Rea.	85	35	50	45	215

Total transportation cost

=1*35+3*35+2*50+8*5+10*85+7*5 =Rs.1,165.

3. Result Analysis

Above examples show that in some cases optimal solution is only given by MODI method and not by SS method. The comparison table of the solutions given by both the methods is given below.

	Total Transportation Cost			
Methods	Example 1	Example 2		
MODI	Rs. 10150	Rs.1160		
S S	Rs.10500	Rs.1165		

4. Conclusion

Above noted study proves that SS method cannot be an alternative to MODI method for finding optimal solution of a transportation problem.

References

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