

Utilization of Parametric and Non-parametric Statistical Test in Clinical Trials

Anirban Goswami

Investigator (Statistics), Regional Research Institute of Unani Medicine, Patna, Bihar, India

Abstract: *A clinical trial is increasingly based on the empirical studies and the results of these are usually presented and analyzed with statistical methods. Therefore discuss frequently used statistical tests for different type of data set under assumption of normality or non-normality. The parametric statistical tests applied when normality (and homogeneity of variance) assumptions are satisfied otherwise the equivalent non-parametric statistical test used. Advice will be presented for selecting statistical tests on the basis of very simple cases. It is therefore an advantage for any physician he/she is familiar with the frequently used parametric or non-parametric statistical tests, as this is the only way he or she can evaluate the statistical methods in scientific publications and thus correctly interpret their findings.*

Keywords: Clinical trials, Parametric, Nonparametric, Statistical Test

1. Introduction

Clinical trials are conducted to collect and recorded data on each subject, such as the patient's demographic characteristics, disease related risk factors, medical history, biochemical markers, pathological history, medical therapies, and outcome or endpoint data at different time points. This data may be continuous or discrete. Understanding that the types/assumptions of data are more important as they determine which method of data analysis is to be use and how to report the results (Wang & Bakhai, 2006). For the assessment of the safety, efficacy, and / or the mechanism of action of an investigational medicinal product, or new drug or device that is in development.

Data can be divided into two main types: quantitative and qualitative. Quantitative data can be either continuous variables that one can measure (such as height, weight, or blood pressure) or discrete variables (such as numbers of patients attained in OPD per day or numbers of attacks of asthma per child per month). Qualitative data tend to be categories; people are male or female, Indian or Bangladeshi, they have a disease or are in good health and they are belonging to lower or middle or higher socio-economic status. There are four types of scales that appear in social sciences: nominal, ordinal, interval, and ratio scales. They are categorized into two groups: categorical and continuous scale data. Nominal and ordinal scales are categorical data or non-parametric data; interval and ratio scales are continuous data or parametric data. When categorical data has unordered scales it is called nominal scales. Blood group, gender are example of the nominal scale. Categorical data that has ordered scales are called ordinal scale. Severities of illness, amount of pain are example of ordinal scale. There should be distinction between them because the data analysis method is different depending on the scale of measurement (Campbell, 2006).

In clinical trials, patient's and investigator's responses to treatments can be documented according to the occurrence of some meaningful and well-defined event such as death, infection, or cure of a certain disease, any serious adverse events, biochemical and pathological findings. In addition the nature of these data can be parametric or non-parametric.

Parametric test is used on parametric data, while non-parametric data is examined with a non-parametric test. Parametric statistical tests are done when data follow the normal distribution. Parametric test are the most powerful statistical test because they use all of the information in the numbers. Non-parametric statistical test are used when the data don't follow a particular distribution but can be ordered and sometimes are called distribution free test.

2. Parametric Statistical test used in Clinical Trial

Z-test: A Z-test is a hypothesis test based on the Z-statistic, which follows the standard normal distribution under the null hypothesis. This test is used when the outcome is continuous and the exposure, or predictor, is binary. We can use this test under the assuming for the sample size is greater than 30, observations should be independent from each other, one observation isn't related or doesn't affect another observations, data should be followed normally distributed and data should be randomly selected from a population, where each item has an equal chance of being selected. There are two type of test under Z-test as one sample Z-test and two sample Z-test. The one sample Z-test, which tests the mean of a normally distributed population with known variance. For example in clinical trials, if someone said they had found a new drug that cures cancer, some other would want to be sure it was probably true. A hypothesis test will tell him if it's probably true, or probably not true. The two sample Z-test used to determine whether two population means are different when the variances are known and statistic is assumed to have a normal distribution. For example in clinical trials, suppose two flu drugs A and B, Drug A works on 41 people out of a sample of 195, Drug B works on 351 people in a sample of 605. And to test the effect of two drugs equal or not.

Student t-test: Student t-test, in statistics, a method of testing hypotheses about the mean of a small sample drawn from a normally distributed population when the population standard deviation is unknown. We can use this test under the assuming for the sample size is lesser than 30, observations should be independent from each other, one observation isn't related or doesn't affect another

observations, data should be followed normally distributed and data should be randomly selected from a population, where each item has an equal chance of being selected. There are two type of Student t-test under one sample and two sample. One sample student t-test is a statistical procedure used to examine the mean difference between the sample and the known value of the population mean. It is used to determine if a mean response changes under different experimental conditions. In other hand, two-sample t-test is used to compare the means of two independent populations, denoted μ_1 and μ_2 with standard deviation of the populations should be equal. This test has ubiquitous application in the analysis of controlled clinical trials. For example in clinical trials, the comparison of mean decreases in diastolic blood pressure between two groups of patients receiving different antihypertensive agents, or estimating pain relief from a new treatment relative to that of a placebo based on subjective assessment of percent improvement in two parallel groups (Box, 1987; Walker & Shostak, 2010)

Student paired 't' test: It is a statistical technique that is applied to paired data of independent observations from one sample only when each individual gives a pair of observation or compare two population means in the case of two samples that are correlated. Paired sample t-test is used in 'before-after' studies, or when the samples are the matched pairs, or when it is a case-control study. We can use this test under assumptions of the number of observations in each data set must be the same, and they must be organized in pairs, in which there is a definite relationship between each pair of data observations, data were taken as random samples follows as Normal distribution and the variance of two samples is equal, Cases must be independent of each other. This statistical test used in clinical trial to compare the effect of two drugs, given to the same individuals in the sample at two different occasions, e.g., adrenaline and noradrenalin on puls rate, number of hours for which sleep is induced by two hypnotics and so on (Mahajan, 2010).

ANOVA: Analysis of variance (ANOVA) is used in statistics that splits the total variability found inside a data set into two parts: systematic factors and random factors. The systematic factors have a statistical influence on the given data set, but the random factors do not. Analysts use the ANOVA test to determine the result independent variables have on the dependent variable amid a regression study. It is an extension of the two-sample t-test and Z-test. In 1918, Ronald Fisher developed a test called the analysis of variance. This test is also called the Fisher analysis of variance, used to the analysis of variance between and within the groups whenever the groups are more than two (Scheffé, 1999). When we set the Type one error to be 0.05, and we have several of groups, each time we tested a mean against another there would be a 0.05 probability of having a type one error rate. This would mean that with six T-tests we would have a 0.30 ($.05 \times 6$) probability of having a type one error rate. This is much higher than the desired 0.05. ANOVA creates a way to test several null hypothesis at the same time at the Type one error 0.05. We can use this test under the assuming, each group sample is drawn from a normally distributed population, all populations have a common variance, all samples are drawn independently of each other, within each sample, the observations are sampled

randomly & independently of each other and factor effects are additive in nature. Example in clinical trials, ANOVA method might be appropriate for comparing mean responses among a number of parallel-dose groups or among various strata based on patients' background information, such as race, age group, or disease severity (Walker & Shostak, 2010)

ANCOVA: In clinical trials, patients who meet inclusion and exclusion criteria are randomly assigned to each treatment group. Under the assumption of targeted patient population is homogeneous, we can expect that patient characteristics such as age, gender, and weight are comparable between treatment groups. If the patient population is known to be heterogeneous in terms of some demographic variables, then a stratified randomization according to these variables should be applied. At the beginning of the study, clinical data are usually collected at randomization to establish baseline values. After the administration of study drug, clinical data are often collected at each visit over the entire duration of study. These clinical data are analyzed to assess the efficacy and safety of the treatments. As pointed out earlier, before the analysis of endpoint values. Characteristics between treatments of the patient are usually examined by an analysis of variance (ANOVA) if the variable is continuous. For the analysis of endpoint values, although the technique of analysis of variance (ANOVA) can be directly applied, it is believed the endpoint values are usually linearly related to the baseline values. Therefore an adjusted analysis of variance should be considered to account for the baseline values. This adjusted analysis of variance is called analysis of covariance (ANCOVA) (Chow & Liu, 2004). In addition, ANCOVA provides a method for comparing response means among two or more groups adjusted for a quantitative concomitant variable, or 'covariate', thought to influence the response. The attention here is confined to cases in which the response, y , might be linearly related to the covariate, x . ANCOVA combines regression and ANOVA methods by fitting simple linear regression models within each group and comparing regressions among groups. Assumptions for ANCOVA as each independent variable, the relationship between the response (y) and the covariate (x) is linear, the lines expressing these linear relationships are all parallel (homogeneity of regression slopes), the covariate is independent of the treatment effects (i.e. the covariant and independent variables are independent. ANCOVA might be applied 1) comparing cholesterol levels (y) between a treated group and a reference group adjusted for age (x , in years) 2) comparing scar healing (y) between conventional and laser surgery adjusted for excision size (x , in mm) 3) comparing exercise tolerance (y) in 3 dose levels of a treatment used for angina patients adjusted for smoking habits (x , in cigarettes/day).

Repeated Measurement of ANOVA: In a Clinical Research we record the data on the patients more than two times. In such a situation using the standard ANOVA procedures is not appropriate as it does not consider dependencies between observations within subjects in the analysis. To deal with such types of study data Repeated Measure ANOVA should be used (Singh, Rana, & Singhal, 2013). We can use this method under the assumptions,

(1) the dependent variable should be measured at the continuous level (i.e. measured in hours), intelligence (measured using IQ score), exam performance (measured from 0 to 100), weight (measured in kg), and so forth. (2) the independent variable should consist of at least two categorical, "related groups" or "matched pairs". "Related groups" indicates that the same subjects are present in both groups. (3) the distribution of the dependent variable in the two or more related groups should be approximately normally distributed. (4) the variances of the differences between all combinations of related groups must be equal and there should be no significant outliers in the related groups. Example in clinical trial, consider the two groups with two different treatment modalities with measured different physical and biochemical parameters (e.g pulse, systolic blood pressure, serum sodium level etc.) in each group at different time intervals (say pre-intervention, after 1 month and after two months) and to test the effect of each treatment modality on these parameters over time and at the same time look for any significant difference existing between the two groups using repeated measurement of ANOVA.

Repeated Measurement of ANCOVA: It is used in randomized clinical trials, suppose measurements are often collected on each patient at a baseline visit and several post-randomization time points. In the longitudinal analysis of covariance in which the post baseline values form the response vector and the baseline value is treated as a covariate can be used to evaluate the treatment differences at the post baseline time points. A constrained longitudinal data analysis in which the baseline value is included in the response vector together with the post baseline values and a constraint of a common baseline mean across treatment groups is imposed on the model as a result of randomization (Liang & Zeger, 2000). If the baseline value is subject to missingness, the constrained longitudinal data analysis is shown to be more efficient for estimating the treatment differences at post baseline time points than the longitudinal analysis of covariance. The efficiency gain increases with the number of subjects missing baseline and the number of subjects missing all post baseline values, and, for the pre-post design, decreases with the absolute correlation between baseline and post baseline values.

Pearson Correlation Test: Pearson Correlation is a statistical procedure applied to calculate association between two continuous or ordinal scale variables. It is used when both variables being studied are normally distributed. This coefficient is affected by extreme values, which may exaggerate or dampen the strength of relationship, and is therefore inappropriate when either or both variables are not normally distributed. Pearson's coefficient test while the significance of the coefficient is expressed by *p*-value. Pearson's correlation is denoted by a small letter *r* and its values may range from -1 to +1. The value of the correlation coefficient from 0 to 1 is positive correlation and it designates proportional growth of values in both variables. An example of positive correlation is the duration of diabetes mellitus and the degree of damage of eye capillaries. The correlation coefficient value from 0 to -1 indicates negative correlation, i.e. a rise in the value of one variable that is proportional to a decline in the value of the

other; e.g. oxygen concentration in the air drops with the rise in altitude above sea level. Perfect correlations, i.e. the values of the coefficient of correlation $r = \pm 1$ are not characteristically for biological systems and most frequently refer to theoretical models. The zero value of the coefficient of correlation indicates absence of linear correlation, i.e. by knowing the values of one variable, we can conclude nothing on the values of the other.

3. Nonparametric Statistical test used in Clinical Trial

Chi-square test: The chi-square test of independency is used to the association between two independence categorical variables. The idea behind this test is to compare the observed frequencies with the frequencies that would be expected if the null hypothesis of no association/statistically independence were true. By assuming the variables are independent, we can also predict an expected frequency for each cell in the contingency table. If the value of the test statistic for the chi-squared test of association is too large, it indicates a poor agreement between the observed and expected frequencies and the null hypothesis of independence/no association is rejected. For example in clinical trials, it will be used to test the association between adverse event and the treatment used. The assumptions of chi-square test as independent random sampling, no more than 20% of the cells have an expected frequency less than five, and no empty cells. If the chi-square test shows significant result, then we may be interested to see the degree or strength of association among variables, but it fails to explain another situation where more than or equal to 20% of the cells have an expected frequency less than five. In this case, the usual chi-square test is not valid. Then the Fisher Exact test will be used to test the association among variables. This method also fails to give the strength of association among variables.

The chi-square test of homogeneity is applied to a single categorical variable from two different populations. It is used to determine whether frequency counts are distributed identically across different populations. We can use this test under the assuming for each population, the sampling method is simple random sampling and sample data are displayed in a contingency table (Populations x Category levels), the expected frequency count for each cell of the table is at least 5. For example, in multicenter clinical trials it will be used to test differences among the centres for response of the particular drug(s).

Fisher Exact Test: The Fisher's exact test is used in the approximation of the chi-squared and normal test for a 2 x 2 contingency table, when cells have an expected frequency of five or less (Fisher, 1925). The chi-square test assumes that each cells has an expected frequency of five or more, but the Fisher's exact test has no such assumption and can be used regardless of how small the expected frequency is. For example in clinical trials, a study to compare two treatment regimes for controlling bleeding in haemophiliacs undergoing surgery when cell frequency of 2 x 2 contingency table is five or less (Sarmukaddan, 2014).

Binomial Test: It is used for testing whether a proportion from a single dichotomous variable is equal to a presumed population value. Binomial test as an alternative to the z - test for population proportions. *The assumptions* for the test are that a) the data are dichotomous, b) observations should be independent from each other, and c) the total number of observations in category A multiplied by the total number of observations (i.e. $A + B > 10$), and that the total number of observations in category B multiplied by the total number of observations > 10 (this way we can use the normal approximation for the binomial test and calculate the z-score). In clinical trials, a common use of the binomial test is for estimating a response rate, p, using the number of patients (X) who respond to an investigative treatment out of a total of n studied.

McNemar test: In clinical trials, It's used when researcher interested to the test of improvement in response rate after a particular treatment or finding a change in proportion for the paired data (e.g., studies in which patients serve as their own control, or in studies with before and after design). The three main assumptions for this test are variable must be nominal with two categories (i.e. dichotomous variables) and one independent variable with two connected groups, two groups of the dependent variable must be mutually exclusive and sample must be a random sample and no expected frequencies should be less than five. Data should be placed into a 2×2 contingency table, with the cell frequencies equalling the number of pairs. For example, a researcher is testing a new medication and records if the drug worked ("yes") or did not ("no").

Cochran's Q tests : This test is used to determine if there are differences on a dichotomous dependent variable between three or more related groups. In addition, when a binary response is measured several times or under different conditions, Cochran's tests that the marginal probability of a positive response is unchanged across the times or conditions. The Cochran Q test is an extension to the McNemar test for related samples that provides a method for testing the differences between three or more matched sets of frequencies or proportions. We can use this test under the assuming for one dependent variable with two, mutually exclusive groups (i.e., the variable is dichotomous), dichotomous variables include perceived safety (two groups: "safe" and "unsafe"), one independent variable with three or more related groups and the cases (e.g., participants) are a random sample from the population of interest. For example, the data set drugs contain data for a study of three drugs to treat a chronic disease (Agresti, 2002). and forty-six subjects receives drugs A, B, and C. The response to each drug is either favorable or unfavorable and to test that differences of favorable response for the three drugs.

Bhapkar's test: This test is the marginal homogeneity by exploiting the asymptotic normality of marginal proportion (Bhapkar, 1966). The idea of constructing test statistic is similar to the one of generalized McNemar's test statistic, and the main difference lies in the calculation of elements in variance-covariance matrix. Although the Bhapkar and Stuart-Maxwell tests are asymptotically equivalent (Keefe, 1982). Bhapkar test is a more powerful alternative to the

Stuart-Maxwell test. In large sample both will produce the same chi-squared value (Bhapkar, 1966).

Wilcoxon signed-rank test: The Wilcoxon signed rank test is a non-parametric or distribution free test for the case of two related samples or repeated measurements on a single sample. It can be used (a) in place of a one-sample t-test (b) in place of a paired t-test or (c) for ordered categorical data where a numerical scale is inappropriate but where it is possible to rank the observations when the population can't be assumed to be normally distributed. For example, the hours of relief provided by two analgesic drugs in patients suffering from arthritis and to test that one drug provides longer relief than the other.

Mann-Whitney U test: The Mann-Whitney U test is a non-parametric or distribution free test to compare differences between two independent groups when the dependent variable is either ordinal or continuous, but not normally distributed. The Mann-Whitney (or Wilcoxon-Mann-Whitney) test is sometimes used for comparing the efficacy of two treatments in clinical trials. It is often presented as an alternative to a t- test when the data are not normally distributed. Whereas a t-test is a test of population means, the Mann-Whitney test is commonly regarded as a test of population.

Kruskal-Wallis H test: The Kruskal-Wallis H test is a rank-based nonparametric test that can be used to determine if there are statistically significant differences between two or more groups of an independent variable on a continuous or ordinal dependent variable. Sometimes this test described as an ANOVA with the data replaced by their ranks. It is an extension of the Mann-Whitney U test to three or more groups. For example in clinical trials, it will be used to test assess differences in albumin levels in adults different diets with different amounts of protein.

Friedman Post Hoc test: It is a non-parametric test (distribution-free) used to compare observations repeated on the same subjects. This test is an alternative to the repeated measures ANOVA, when the assumption of normality or equality of variance is not met. Friedman's Test and found a significant P- value, that means that some of the groups in data have different distribution from one another, but it is don't know which. There for, it is needed to find out which pairs of groups are significantly different then each other. But when we have N groups, checking all of their pairs will be to perform $[n \text{ over } 2]$ comparisons, thus the need to correct for multiple comparisons arises. In that situation we will used the Friedman Post Hoc test. In clinical trials, this test find out the improvement of the drug(s) among the patients follow ups for a particular disease.

Log-rank test: The Log-rank test is a nonparametric test to comparing distributions of time until the occurrence of an event of interest among independent groups. The event is often death due to disease, but event might be any binomial outcome, such as cure, response, relapse, or failure. Examples where use of the log-rank test might be appropriate include comparing survival times in cancer patients who are given a new treatment with patients who

receive standard chemotherapy, or comparing times-to-cure among several doses of a topical antifungal preparation where the patient is treated for 10 weeks or until cured, whichever comes first.

Tukey Multiple Comparison Test: In clinical trial, the researcher may still need to understand subgroup differences among the different experimental and control groups. The subgroup differences are called “pairwise” differences. ANOVA does not provide tests of pairwise differences when the researcher needs to test pairwise differences. Tukey’s multiple comparison analysis method tests each experimental group against each control group (Mary, 2011). The Tukey method is preferred if there are equal group sizes among the experimental and control groups. A modified Tukey-Kramer method can be applied for comparisons of unequal-sized groups. We can use this test under assuming the observations being tested are independent within and among the groups, the groups associated with each mean in the test are normally distributed and there is equal within-group variance across the groups associated with each mean in the test (homogeneity of variance). Example in clinical trial, consider the data on effect of maternal smoking on child birth weight, in this case only the effect of duration of smoking is statistically significant. To find which duration or duration are making a significant impact, compare mean birth weight for different duration.

Spearman Correlation Test: Spearman correlation to test the association between two ranked variables, or one ranked variable and one measurement variable. It is appropriate when one or both variables are skewed or ordinal (Altman, 1990) and is robust when extreme values are present. It is used instead of linear regression/correlation for two measurement variables if you're worried about non-normality, but this is not usually necessary. Spearman correlation coefficient solely tests for monotonous relationships for at least ordinally scaled parameters. The advantages of the latter are its robustness to outliers and skew distributions. Correlation coefficients measure the strength of association and can have values between -1 and $+1$. The closer they are to 1 , the stronger is the association. A test variable and a statistical test can be constructed from the correlation coefficient. The null hypothesis to be tested is then that there is no linear (or monotonous) correlation.

4. Conclusion

Parametric and Non-parametric Statistical test are used to analyze the different type of data in different situations and nature of the data set. The statistical test has its limitations, and to overcome that another method is used. Before using the statistical test we need to check the assumptions and type of the study. Most of these statistical tests play a very important role to getting appropriate and desired result in clinical trials, to make the decision on the objectives. Researchers / Physicians are helpful to used statistical tests to determine results from experiments, clinical trials of medicine and symptoms of diseases. The use of statistical test in medicine provides generalizations for the public to better understand their risks for certain diseases, links

between certain behaviors of diseases, effectiveness of drug(s) and to significant finding of experimental objectives.

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