

A Fuzzy Two-Warehouse Inventory Model for Weibull Deteriorating Items with Constant Demand, Shortages and Fully Backlogging

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Abstract: In this paper deals with fuzzy inventory model for deteriorating item, constant demand pattern, shortage under fully backlogged with two warehouse, is formulated and solved. After illustrate the model it test validity of the same, one numerical example have been solved then test sensitivity analyses. Fuzziness is applying by allowing the cost components (holding cost, shortage cost, deterioration cost etc). In fuzzy environment it considered all required parameter to be triangular fuzzy numbers. The purpose of the model is to minimize total cost function.

Keywords: Inventory, Two Ware-House, Constant demand, Fuzzy number, Shortages, Triangular fuzzy number

1. Introduction

An inventory deal with decision that minimum the total average cost or maximize The total average profit. For this purpose the task is to construct a mathematical model of the real life Inventory system, such a mathematical model is based on various assumption and approximation

In a inventory model deterioration and shortages is very important condition. There are many deterioration products in an inventory like drugs, foods, pharmaceuticals etc. During inventory there are several type of customer. At shortage period some customers are waiting for actual product and others do not it.

When a retailer purchases a large quantity of goods at a time, then it hired one or more warehouse. In this paper it considered two warehouse OW and RW.

Datta and pal investigated an inventory system with power demand pattern for item which variable rate deterioration. Park and Wang studied shortages and partial backlogging of items. Friedman (1978) presented continuous time inventory model with time varying demand. Ritchie(1984) studied in inventory model with linear increasing demand. Goswami, Chaudhuri (1991) discussed an inventory model with shortage. B. Das, and K. Maity (2008), a two warehouse supply-chain model. Gen et. Al. (1997) considered classical inventory model with Triangular fuzzy number .Yao and Lee(1998) considered an economic production quantity model in the fuzzy sense. Sujit Kumar De, P. K. Kundu and A. Goswami (2003) presented an economic production quantity inventory model involving fuzzy demand rate. J. K. Syde and L. A. Aziz (2007) applied sign distance method to fuzzy inventory model without shortage. M. K. Maity (2008), Fuzzy inventory with two warehouse under possibility measure of fuzzy goal. . D. Datta and Pravin Kumar published several paper of fuzzy inventory with or without shortage. In ordinary inventory model it consider all parameter like shortage cost, holding cost, unit cost as fixed.

But in real life situation it will have some little fluctuations. So consideration of fuzzy variables is more realistic.

In this paper we first consider crisp inventory model with power demand where shortage are allowed and partially backlogged. Thereafter we developed fuzzy inventory model with fuzzy power demand rate under partially backlogged. All inventory cost parameters are fuzzified as pentagonal fuzzy number.

2. Preliminaries

For graded representation method to defuzzyfy, we need the following definitions,

Definition2.1: A fuzzy set \tilde{A} on the given universal set X is a set of order pairs,

$\tilde{A}=\{(x, \mu_A(x)): x \in X\}$ where $\mu_A(x) \rightarrow [0,1]$ is called a membership function.

Definition2.2:The α -cut of \tilde{A} , is defined by $A_\alpha=\{x: \mu_A(x)=\alpha, \alpha \geq 0\}$

Definition2.3: \tilde{A} is normal if there exists $x \in X$ such that $\mu_A(x)=1$

Definition2.4:A triangular fuzzy number $\tilde{A}=(a,b,c)$ is represented with membership function \tilde{A} .

\tilde{A} is defined as,

$$\mu_A(X)=\begin{cases} L(x) = \frac{x-a}{b-a}, & a \leq x \leq b \\ R(x) = \frac{c-x}{c-b}, & b \leq x \leq c \\ 0, & \text{otherwise} \end{cases}$$

when $a=b=c$, we have fuzzy point $(a,a,a)=\tilde{a}$. The family of all triangular fuzzy number on R , denoted as $F_N=\{(a,b,c), a < b < c, \forall a,b,c \in R\}$. the α -cut of $\tilde{A}=(a,b,c) \in F_N, 0 \leq \alpha \leq 1$ is $A(\alpha)=[A_L(\alpha), A_R(\alpha)]$ where $A_L(\alpha)=a+(b-a)\alpha$ and $A_R(\alpha)=c-(c-b)\alpha$ are the left and right end Point of $A(\alpha)$.

Definition2.5: If $\tilde{A}=(a,b,c)$ is a triangular fuzzy number then the graded mean integration of

\tilde{A} is defined as,

$$P(\tilde{A}) = \frac{\int_0^{W_A} \left(\frac{L^{-1}(h) + R^{-1}(h)}{2} \right) dh}{\int_0^{W_A} h dh}, (0 \leq h \leq W_A \text{ and } 0 \leq W_A \leq 1)$$

$$P(\tilde{A}) = \frac{\int_0^1 \left[\frac{a + (b-a)h + c - (c-b)h}{2} \right] dh}{\int_0^1 h dh}$$

$$= \frac{a + 4b + c}{6}$$

Suppose $\tilde{a}=(a_1, a_2, a_3)$ and $\tilde{b}=(b_1, b_2, b_3)$ are two fuzzy triangular number then

- (1) $\tilde{a} + \tilde{b} = (a_1, a_2, a_3) + (b_1, b_2, b_3) = (a_1 + b_1, a_2 + b_2, a_3 + b_3)$.
- (2) $\tilde{a} - \tilde{b} = (a_1, a_2, a_3) - (b_1, b_2, b_3) = (a_1 - b_1, a_2 - b_2, a_3 - b_3)$.
- (3) $\tilde{a} \times \tilde{b} = (a_1, a_2, a_3) \times (b_1, b_2, b_3) = (a_1 b_1, a_2 b_2, a_3 b_3)$.
- (4) $\frac{1}{\tilde{b}} = \left(\frac{1}{b_3}, \frac{1}{b_2}, \frac{1}{b_1} \right)$ where b_1, b_2, b_3 are all non zero positive real number, then
 $\frac{\tilde{a}}{\tilde{b}} = \left(\frac{a_1}{b_3}, \frac{a_2}{b_2}, \frac{a_3}{b_1} \right)$.
- (5) Let $k \in \mathbb{R}$, then $k\tilde{a} = k(a_1, a_2, a_3) = (ka_1, ka_2, ka_3)$ for $k \geq 0$.

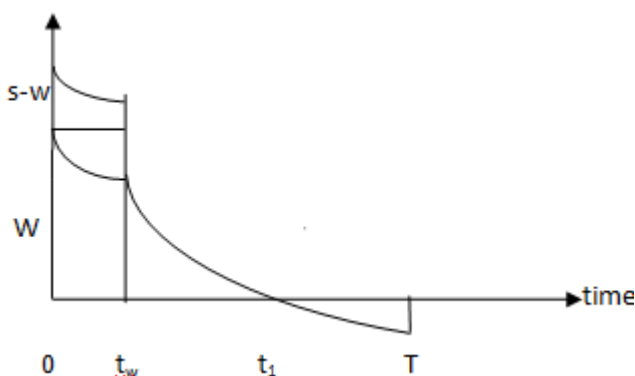
2.1. Notation

$I_r(t)$: Inventory level at time t in RW, $t \geq 0$.
 $I_0(t)$: Inventory level at time t in OW, $t \geq 0$.
 T : Cycle of length.
 t_w : Time point when stock level of RW reaches to zero.
 t_1 : Time point when stock level of OW reaches to zero.
 c_1 : Fixed cost.
 c_2 : Shortages cost per unit.
 c_3 : Opportunity cost due to lost sales.
 C_4 : Holding cost per unit per unit time.
 S : Highest stock level at the beginning of the cycle.
 W : Storage capacity of OW.
 R : Highest shortages level.
 Q : Total order quantity per cycle.
 $TAC(t_w, t_1)$: Total average cost per unit.
 \tilde{c}_1 : Fuzzy fixed cost.
 \tilde{c}_2 : Fuzzy shortage cost per unit.
 \tilde{c}_3 : Fuzzy opportunity cost due to lost sales.
 \tilde{c}_4 : Fuzzy holding cost per unit.
 $TAC(\tilde{t}_w, \tilde{t}_1)$: Fuzzy total cost per unit.

2.2. Assumption

- a: The inventory system involves only one item.
- b: The replenishment occur instantaneously at infinite rate.
- c: The lead time is negligible.
- d: Demand rate is constant, assume it D .
- e: Shortages with fully backlogged.

2.3. Model Development (CRISP SET)



Initially w units are store in OW and the rest ($S-W$) in RW. During $0 \leq t \leq t_w$, the inventory ($S-W$) units in RW decrease due to customer demand, deterioration and it vanishes at $t=t_w$. during the time interval $0 \leq t \leq t_w$, the inventory level decrease due to deterioration in OW and during the interval $t_w \leq t \leq t_1$ it decrease due to customer demand, deterioration and reaches to zero at $t=t_1$. During the time interval $t_1 < t \leq T$, the fully backlogged shortages are allowed.

So the differential equation describing as follows

$$\frac{dI_r(t)}{dt} + \alpha \beta t^{\beta-1} = -D, 0 \leq t \leq t_w \quad (3.1)$$

Subject to boundary condition $I_r(t_w)=0$, and $I_r(0)=S-W$.

$$\frac{dI_0(t)}{dt} + \alpha \beta t^{\beta-1} = 0, 0 \leq t \leq t_w \quad (3.2)$$

Subject to boundary condition $I_0(t_0)=W$.

$$\frac{dI_0(t)}{dt} + \alpha \beta t^{\beta-1} = -D, t_w \leq t \leq t_1 \quad (3.3)$$

Subject to boundary condition $I_0(t_1)=0$.

$$\frac{dI_0(t)}{dt} = -D, t_1 \leq t \leq T \quad (3.4)$$

Subject to boundary condition $I_0(t_1)=0$. And $I_0(T)=-R$

Here α is too small so it neglecting the higher power of α .

From (3.1) we get,

$$I_r(t) = D(t_w - t)(1 - \alpha t^\beta) + \frac{\alpha}{\beta+1} (t_w^{\beta+1} - t^{\beta+1}) \quad (3.5)$$

$$\text{So } S-W = Dt_w + \frac{\alpha}{\beta+1} t_w^{\beta+1}$$

$$\text{And } S = W + Dt_w + \frac{\alpha}{\beta+1} t_w^{\beta+1}.$$

From (3.2) we get,

$$I_0(t) = W(1 - \alpha t^\beta) \quad (3.6)$$

From (3.3) we get,

$$I_0(t) = D(t_1 - t)(1 - \alpha t^\beta) + \frac{\alpha}{\beta+1} (t_1^{\beta+1} - t^{\beta+1}) \quad (3.7)$$

From (3.4) we get,

$$I_0(t) = D(t_1 - t) \quad (3.8)$$

So the maximum stock level at the beginning of the cycle is,

$$S = W + Dt_w + \frac{\alpha}{\beta+1} t_w^{\beta+1} \quad (3.9)$$

And the maximum amount of demand backlogging is,

$$R = -I_0(T) = -D(T - t_1) \quad (3.10)$$

Hence the order quantity per cycle is;

$$Q = S + R = W + Dt_w + \frac{\alpha}{\beta+1} t_w^{\beta+1} + D(T - t_1) \quad (3.11)$$

The fixed cost per cycle is,

$$FC = c_1$$

Shortages cost per cycle is,

$$SC = -c_2 \int_{t_1}^T I_0(t) dt, \\ = -c_2 D(t_1 T - \frac{T^2}{2} - \frac{t_1^2}{2})$$

Deterioration cost per cycle is,

$$DC = c_3 \int_0^{t_w} \alpha t^{\beta-1} I_r(t) dt + c_3 \int_0^{t_w} \alpha t^{\beta-1} I_0(t) dt + c_3 \int_{t_w}^{t_1} \alpha t^{\beta-1} I_0(t) dt \\ = c_3 D \left[\frac{\alpha}{\beta+1} t_w^{\beta+1} + \alpha t_w^{\beta+1} + \alpha t_w^{\beta+1} - \frac{\alpha \beta}{\beta+1} t_1^{\beta+1} - \frac{\alpha}{\beta+1} t_w^{\beta+1} \right].$$

Holding cost per cycle is,

$$HC = c_4 \int_0^{t_w} I_r(t) dt + c_4 \int_0^{t_w} I_0(t) dt + c_4 \int_{t_w}^{t_1} I_0(t) dt \\ = c_4 \left[\frac{t_w^2}{2} - \frac{\alpha t_w^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)} + \frac{W}{D} t_w - \frac{\alpha t_w^{\beta+2}}{(\beta+1)} + \frac{t_1^2}{2} - \frac{\alpha t_1^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - (t_1 t_w - \frac{t_w^2}{2} - \frac{\alpha t_1 t_w^{\beta+1}}{(\beta+1)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)}) - \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - \frac{\alpha}{\beta+1} (t_1^{\beta+1} t_w - \frac{t_w^{\beta+2}}{\beta+2}) \right].$$

So total average cost per cycle is,

$$TAC(t_w, t_1) = \frac{1}{T} [FC + SC + DC + HC]$$

$$= \frac{D}{T} \left[\frac{c_1}{D} - c_2 \left(t_1 T - \frac{T^2}{2} - \frac{t_1^2}{2} \right) + c_3 \left(\frac{\alpha}{\beta+1} t_w^{\beta+1} + w a t_w^{\beta} + a t_w t_1^{\beta} - \frac{\alpha \beta}{\beta+1} t_1^{\beta+1} - \frac{\alpha}{\beta+1} t_w^{\beta+1} + c_4 \left\{ \frac{t_w^2}{2} - \frac{\alpha t_w^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)} + \frac{w}{D} (t_w - \frac{\alpha t_w^{\beta}}{(\beta+1)}) + \frac{t_1^2}{2} - \frac{\alpha t_1^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - (t_1 t_w - \frac{t_w^2}{2} - \frac{\alpha t_1 t_w^{\beta+1}}{(\beta+1)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)}) \right\} - \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - \frac{\alpha}{\beta+1} (t_1^{\beta+1} t_w - \frac{t_w^{\beta+2}}{\beta+2}) \right] \right]$$

For minimum cost it should be,

$$\frac{\partial TAC(t_w, t_1)}{\partial t_w} = 0, \quad \frac{\partial TAC(t_w, t_1)}{\partial t_1} = 0$$

Provided it satisfies equation,

$$\frac{\partial^2 TAC(t_w, t_1)}{\partial t_w^2} > 0, \quad \frac{\partial^2 TAC(t_w, t_1)}{\partial t_1^2} > 0$$

$$\text{And } \left[\frac{\partial^2 TAC(t_w, t_1)}{\partial t_w^2} \right] \left[\frac{\partial^2 TAC(t_w, t_1)}{\partial t_w^2} \right] - \left[\frac{\partial^2 TAC(t_w, t_1)}{\partial t_w \partial t_1} \right]^2 > 0.$$

2.4 FUZZY MODEL

Due to uncertainly lets us assume that,

$\tilde{c}_1 = (c_1^1, c_1^2, c_1^3)$, $\tilde{c}_2 = (c_2^1, c_2^2, c_2^3)$, $\tilde{c}_3 = (c_3^1, c_3^2, c_3^3)$, $\tilde{c}_4 = (c_4^1, c_4^2, c_4^3)$, be triangular fuzzy number then the total average cost is given by,

$$TAC(\tilde{t}_w, \tilde{t}_1) = \frac{1}{T} [FC + SC + DC + HC]$$

$$= \frac{D}{T} \left[\frac{\tilde{c}_1}{D} - \tilde{c}_2 \left(t_1 T - \frac{T^2}{2} - \frac{t_1^2}{2} \right) + \tilde{c}_3 \left(\frac{\alpha}{\beta+1} t_w^{\beta+1} + w a t_w^{\beta} + a t_w t_1^{\beta} - \frac{\alpha \beta}{\beta+1} t_1^{\beta+1} - \frac{\alpha}{\beta+1} t_w^{\beta+1} + \tilde{c}_4 \left\{ \frac{t_w^2}{2} - \frac{\alpha t_w^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)} + \frac{w}{D} (t_w - \frac{\alpha t_w^{\beta}}{(\beta+1)}) + \frac{t_1^2}{2} - \frac{\alpha t_1^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - (t_1 t_w - \frac{t_w^2}{2} - \frac{\alpha t_1 t_w^{\beta+1}}{(\beta+1)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)}) \right\} - \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - \frac{\alpha}{\beta+1} (t_1^{\beta+1} t_w - \frac{t_w^{\beta+2}}{\beta+2}) \right] \right]$$

We defuzzyfi the fuzzy total cost $TAC(\tilde{t}_w, \tilde{t}_1)$ by graded mean representation method as follows,

$$TAC(\tilde{t}_w, \tilde{t}_1) = \frac{1}{6} [TAC^1(t_w, t_1), TAC^2(t_w, t_1), TAC^3(t_w, t_1)]$$

Where

$$TAC^r(\tilde{t}_w, \tilde{t}_1) = \frac{1}{T} [FC + SC + DC + HC]$$

$$= \frac{D}{T} \left[\frac{\tilde{c}_1^r}{D} - \tilde{c}_2^r \left(t_1 T - \frac{T^2}{2} - \frac{t_1^2}{2} \right) + \tilde{c}_3^r \left(\frac{\alpha}{\beta+1} t_w^{\beta+1} + w a t_w^{\beta} + a t_w t_1^{\beta} - \frac{\alpha \beta}{\beta+1} t_1^{\beta+1} - \frac{\alpha}{\beta+1} t_w^{\beta+1} + \tilde{c}_4^r \left\{ \frac{t_w^2}{2} - \frac{\alpha t_w^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)} + \frac{w}{D} (t_w - \frac{\alpha t_w^{\beta}}{(\beta+1)}) + \frac{t_1^2}{2} - \frac{\alpha t_1^{\beta+2}}{(\beta+1)(\beta+2)} + \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - (t_1 t_w - \frac{t_w^2}{2} - \frac{\alpha t_1 t_w^{\beta+1}}{(\beta+1)} + \frac{\alpha t_w^{\beta+2}}{(\beta+2)}) \right\} - \frac{\alpha t_1^{\beta+2}}{(\beta+2)} - \frac{\alpha}{\beta+1} (t_1^{\beta+1} t_w - \frac{t_w^{\beta+2}}{\beta+2}) \right] \right]$$

$$TAC(\tilde{t}_w, \tilde{t}_1) = \frac{1}{6} [TAC^1(t_w, t_1) + 4TAC^2(t_w, t_1) + TAC^3(t_w, t_1)]$$

For minimum cost it should be,

$$\frac{\partial TAC(\tilde{t}_w, \tilde{t}_1)}{\partial t_w} = 0, \quad \frac{\partial TAC(\tilde{t}_w, \tilde{t}_1)}{\partial t_1} = 0$$

Provided it satisfies equation,

$$\frac{\partial^2 TAC(\tilde{t}_w, \tilde{t}_1)}{\partial t_w^2} > 0, \quad \frac{\partial^2 TAC(\tilde{t}_w, \tilde{t}_1)}{\partial t_1^2} > 0$$

$$\text{And } \left[\frac{\partial^2 TAC(\tilde{t}_w, \tilde{t}_1)}{\partial t_w^2} \right] \left[\frac{\partial^2 TAC(\tilde{t}_w, \tilde{t}_1)}{\partial t_w^2} \right] - \left[\frac{\partial^2 TAC(\tilde{t}_w, \tilde{t}_1)}{\partial t_w \partial t_1} \right]^2 > 0.$$

3. Numerical Solution

For crisp model:

Let us take the in-pur value:

C ₁	C ₂	C ₃	C ₄	α	β	D	T	W
100	20	70	50	0.1	0.2	5	10	4

And the out-pur value is:

t _w	t ₁	S	Q	TAC(t _w , t ₁)
1.162	3.379	9.910	43.015	363.433

For fuzzy model:

$\tilde{c}_1 = (95, 100, 105)$, $\tilde{c}_2 = (18, 20, 22)$, $\tilde{c}_3 = (65, 70, 75)$,

$\tilde{c}_4 = (47, 50, 53)$

The solution of fuzzy model by graded mean representation is,

- 1) When $\tilde{c}_1, \tilde{c}_2, \tilde{c}_3, \tilde{c}_4$ are all triangular fuzzy numbers then, TAC(t_w, t₁)=363.389, t_w=1.161 t₁=3.377
- 2) When $\tilde{c}_1, \tilde{c}_2, \tilde{c}_3$, are all triangular fuzzy numbers then TAC(t_w, t₁)=363.171, t_w=1.160 t₁=3.376
- 3) When \tilde{c}_1, \tilde{c}_2 , are triangular fuzzy numbers then, TAC(t_w, t₁)=363.154, t_w=1.160 t₁=3.375
- 4) When \tilde{c}_1 , is triangular fuzzy numbers then, TAC(t_w, t₁)=363.433, t_w=1.160 t₁=3.379

3.1 Sensitivity Analysis (Crisp Model)

We now examine to sensitivity analysis of the optimal solution of the model for change in I, keeping the other parameters unchanged. The initial data from the above numerical example.

Parameter % of change	TAC(t _w , t ₁)	t _w	t ₁
C ₁ =50.0	-50	358.433	1.162 3.379
C ₁ =75.0	-25	360.933	1.162 3.379
C ₁ =100	0	363.433	1.162 3.379
C ₁ =125	25	365.933	1.162 3.379
C ₁ =150	50	368.433	1.162 3.379
C ₂ =10	-50	221.020	0.000 1.530
C ₂ =15	-25	302.483	0.802 2.676
C ₂ =20	0	363.433	1.162 3.379
C ₂ =25	25	413.477	1.451 3.952
C ₂ =30	50	455.574	1.691 4.431
C ₃ =35	-50	354.724	1.258 3.434
C ₃ =52.5	-25	359.117	1.210 3.407
C ₃ =70	0	363.433	1.162 3.379
C ₃ =87.5	25	367.667	1.112 3.351
C ₃ =105	50	371.817	1.062 3.322
C ₄ =25	-50	277.048	1.901 5.117
C ₄ =37.5	-25	328.471	1.476 4.840
C ₄ =50	0	363.433	1.162 3.379
C ₄ =62.5	25	388.571	0.924 2.856
C ₄ =75	50	407.359	0.739 2.455

3.2 Effect, for increment parameters-

- (1) TAC(t_w, t₁) increase and t_w, t₁ remain same, for increase of c₁.
- (2) TAC(t_w, t₁), t_w, t₁ increase, for increase of c₂.
- (3) TAC(t_w, t₁) increase and t_w, t₁ decrease, for increase of c₃.
- (4) TAC(t_w, t₁) increase and t_w, t₁ decrease, for increase of c₄.

4. Conclusion

In this paper, we have proposed a real life two warehouse inventory problem in a fuzzy environment and presented solution along with sensitivity analysis approach. The inventory model developed with constant demand with shortages. Shortages have been allow fully backlogged in this model. Here deterioration also be used, and which is weibull deterioration. In this paper, we have considered triangular fuzzy number and solved by graded mean integration method. In future, the other type of membership functions such as piecewise linear hyperbolic, L-R fuzzy number, fuzzy pentagonal number, etc can be considered to construct the membership function and then model can be easily solved.

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