Analysis of Hypertension Factors in Diabetic Patients Using Mathematical Model

R. Jayakumar¹, G. Komahan²

¹Research scholar, Department of Mathematics, A.V.V.M. Sri Pushpam College, Poondi, Thanjavur, Tamil Nadu
²Department of Mathematics, A.V.V.M. Sri Pushpam College, Poondi, Thanjavur, Tamil Nadu

Abstract: Hypertension is an extremely common co-morbidity of diabetes, affecting 20–60% of individuals with diabetes. Hypertension (HP) is commonly found in large number of diabetic peoples in Tamil Nadu. Therefore, hypertension should be screened for and promptly diagnosed with aggressive blood glucose and lipid profile control in patients with diabetes. In this paper to find out the major diagnostic factors to develop the hypertension in diabetic patients using fuzzy relational map (FRM). Based on this study the major risk factor of hypertension and the preventing measure using it is determined.

Keywords: Hypertension, Diabetic, Fuzzy relational map, Glucose

1. Introduction

Hypertension is an extremely common co-morbidity of diabetes, affecting 20–60% of individuals with diabetes. The prevalence of hypertension in the diabetic population is 1.5 to 3 times higher than that of non-diabetic age-matched groups. Many patients with diabetes have hypertension at the time of diagnosis, while others develop hypertension as the duration of the disease lengthens. Conversely a number of patients with systemic hypertension develop diabetes in the course of their disease. Therefore, hypertension should be screened for and promptly diagnosed with aggressive blood glucose and lipid profile control instituted in all patients with diabetes [1, 2].

In Vasantha Kandaswamy and Yasmin sultana [3] a new notion called Fuzzy Relational Maps (FRMs) was introduced. To define a FRM a domain space and a range space which are disjoint in the sense of concepts is needed. The number of elements in the range space need not in general be equal to the number of elements in the domain space. In FRMs the very causal associations is divided into two disjoint units for example the relationship between a teacher and a student or relation between doctor and patient and so on. Further it is assumed that no intermediate relations exist within the domain element or node and the range space. Hypertension can be defined as a blood carried from the heart to all parts of the body in the vessels. Each time the heart beats it pumps blood into the vessels (arteries) as it pumped by the heart. Blood pressure measurements for diabetic patients are classified into the four categories: 1. Normal blood pressure less than 120/80, 2. Pre-hypertension 120-139/80-89, 3. High blood pressure (stage 1) 140-159/90-99 and 4. High blood pressure (stage 2) higher than 160/100. FRM model is used to find out the major diagnostic factor to develop the hypertension in diabetic patients [5]. Diabetic is the major risk factor for hypertension [5, 6].

2. Fuzzy Relational Maps (FRMs)

In Fuzzy relational maps (FRMs) the elements of the domain space are taken from the real vector space of dimension n and that of the range space are real vectors from the vector dimension m (m in general need not be equal to n). Denote R as the set of nodes R1,…,Rm of the range space, where R= {(X1,…,Xm/Xj=0 or 1) for j=1,2,…,m. if Xi=1 it means that the node Ri is in the ON state and if Xi=0 it means that the node Ri is in the OFF state. Similarly D denotes the nodes D1, D2,…,Dn of the domain space, where D= {(X1,…,Xn/Xj=0 or 1) for i=1,2,…,n if Xi=1 it means that the node Di is in the ON state and if Xi=0 it means that the node Di is in the OFF state [3].

Definition 1.1.1: Let Di Rj (or Rj Di), 1≤ j ≤ m, 1≤ i ≤ n when Ri (or Dj) is switched on and if causality flows through edges of the cycle and if it again causes Ri (or Dj) we say that the dynamical system goes round and round. This is true for any node Rj (or Di) for 1≤ j ≤ n, (or 1≤ j ≤ m) the equilibrium state of this dynamical system is called the hidden pattern.

Definition 1.1.2: If the equilibrium state of a dynamical system is a unique state vector, then it is called a fixed point. Consider an FRM with R1,R2,…,Rm and D1,D2,…,Dn as nodes for example, let us start the dynamical system by switching on n1R1(or D1).Let us assume that the FRM settles down with R1 and Dm(or D1 and Dn) ON i.e. the state vector remains as(1,0,…,0,1) in R) or ((1,0,…,0,1) in D).this state vector is called the fixed point.

Definition 1.1.3: If the FRM settles down with a state vector repeating in the form A1→A2→A3→…→Ai→A1(orB1→B2→…→Bi→B1) then this equilibrium is called a limit cycle.

Methods of determining the hidden pattern
Let R1, R2,…Rm and D1, D2,…Dn be the nodes of a FRM with feedback. Let E be the relational matrix. Let us find a hidden pattern when D1 is switched on i.e. When an input is given as vector A1= (1, 0, 0,0) in D1, the data should pass through the relational matrix. This is done by multiplying A1 with the relational matrix E. Let A1E= (r1, r2,…,rm), after thresholding and updating the resultant vector we get...
Now let $B = A^E$, we pass on $B$ into $E^T$ and obtain $BE^T$. We update and threshold the vector $BE^T$ so that $BE^T \preceq D$. This procedure is repeated till we get a limit cycle or a fixed point \cite{7, 8}.

### Symptoms of Hypertension

According to research studies, the risk of dying of a heart attack is directly linked to high blood pressure particularly systolic hypertension. High blood pressure usually causes no symptoms and high blood pressure often labeled "the silent killer" people who have high blood pressure typically don’t know it until their blood pressure is measured sometimes people with markedly elevated blood pressure may develop Headache, dizziness, blurred vision, nausea, vomiting, chest pain, shortness of breath. People often do not seek medical care until they have no symptoms arising from organ damage caused by chronic high blood pressure the organ damage are commonly seen in chronic high blood pressure \cite{9}.

### Basic Model

The relational between the risk factors and the symptoms of diabetes among adults using fuzzy relational maps A. Victor Devadoss et al \cite{10} Diabetes is a problem body fuel system which is Cause due to lack of insulin hormone in the pancreases that is essential for getting energy from food. causes of diabetes continues to be a mystery till now it is both genetic and environmental factors. The main causes may be due to genetics and environmental factors. The study shows that diabetes patients increase in the urban population because the low amount of physical activity in the urban population. This leads to increasing urbanization tends to lower the physical activity worldwide.

### 3. Model: Implementation of FRM Model in Study of Hypertension Problem

100 diabetic patients were interviewed using a linguistic questionnaire regarding hypertension for a period of one month in the Sivaprithi hospital (Thanjavur, Tamil Nadu). The fuzzy concepts, attributes are first given in the form of matrix relational equations and then solved. The patients who have been investigated reported the symptoms of Hypertension. FRM model is used to find the major diagnostic factor develop the hypertension in diabetic patients. Diabetes is assessable on the basis of the diagnosis by ascertaining Glucose, Cholesterol, Triglyceride, Being weight loss, Hæmoglobin, Age, Having family history, Insulin, HDL Cholesterol and Other medical problems.

### Attributes related to diagnostic factors

The domain space $R$ connected with the diagnostic factors are given by $R = \{R1, R2…R10\}$

- R1: Glucose
- R2: Cholesterol
- R3: Triglyceride
- R4: Being weight loss
- R5: Hæmoglobin
- R6: Age
- R7: Having family history

- R8: Insulin
- R9: HDL Cholesterol
- R10: Other medical problems

### Attributes related to the symptoms

The Range space $S$ connected with the symptoms are given by $S = \{S1, S2…S7\}$

- S1: Headache
- S2: Dizziness
- S3: Nausea
- S4: Chest pain
- S5: Blurred vision
- S6: Shortness of breath
- S7: Tiredness

### First Expert’s Opinion

The opinion of the first expert is a hypertension from urban and is given vital importance. This opinion is transformed into the fuzzy relational matrix $M_1$ is given by

$$
M_1 = \begin{bmatrix}
S1 & S2 & S3 & S4 & S5 & S6 & S7 \\
1 & 1 & 0 & 1 & 1 & 1 & 1 \\
R1 & 1 & 1 & 0 & 1 & 1 & 1 \\
R2 & 1 & 1 & 0 & 1 & 1 & 1 \\
R3 & 1 & 1 & 0 & 1 & 1 & 1 \\
R4 & 1 & 1 & 0 & 0 & 1 & 1 \\
R5 & 1 & 1 & 0 & 0 & 0 & 1 \\
R6 & 0 & 0 & 0 & 1 & 1 & 1 \\
R7 & 0 & 1 & 0 & 1 & 0 & 0 \\
R8 & 1 & 1 & 0 & 1 & 1 & 1 \\
R9 & 1 & 1 & 0 & 1 & 1 & 1 \\
R10 & 1 & 1 & 0 & 1 & 1 & 1 \\
\end{bmatrix}
$$

The hidden pattern of the state $X = (0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0)$ is obtained by the following method

$$
XM_1 \rightarrow (1 \ 1 \ 0 \ 1 \ 1 \ 1 \ 1) = Y \\
YM_1 \rightarrow (1 \ 1 \ 0 \ 1 \ 1 \ 1 \ 1) = X_1
$$

(Where denotes after thresholding and updating the resultant vector)

When only the nodes R1 Glucose in the ON state and all other attributes to be in the OFF state then all the nodes in the domain space come to ON state. It is seen that the effect of X on the dynamical system M is a fixed point given by the binary pair \{110111111\}. When having glucose node alone in the ON state and let $X = (1111111)$, then the resultant is the fixed point given by the binary pair \{111111111\}. When ON state is taken as node R1. It is seen that the hidden pattern is the fixed point. This is the same binary pair which makes all the nodes to be in the ON state in the Domain Space and also it makes all the nodes in the range space to be in ON state.

### 4. Conclusion

Hypertension is a silent killer and it is the major risk factor for Diabetic. Based on the graph blood glucose, cholesterol, triglycerides leads to the risks of hypertension. From the study, it is seen that while using FRM, blood glucose is the
Hypertension is a major risk factor for hypertension. Hypertension may be prevented by living a healthy lifestyle such as eating a nutritious, low-fat diet, exercising regularly, maintaining a healthy weight, monitoring blood glucose level and reduce stress in day to day life.

Figure 1: Diagrammatic representation of FRM

Figure 2: Glucose vs Symptoms

Figure 3: Cholesterol vs Symptoms

Figure 4: Triglycerides vs Symptoms

Figure 5: Being weight loss vs Symptoms

Figure 6: Hemoglobin vs Symptoms

Figure 7: Age vs Symptoms
References


