$$z(x;\theta) = \psi(z(x)) \quad (2)$$

Training of the network

The weights of network are chosen such that the error is minimal. Quasi Newton Method was used in this study. This method was independently developed by the authors: Broyden, Fletcher and Goldfarb. It's commonly known to as the BFGS method.

Logistic Regression

Logistic regression is a category of generalized linear models. It is used to model discrete outcomes which are binary.

The logistic function is given as:

$$f(h) = \frac{\exp(h)}{1+\exp(h)} \quad (3)$$

$$= \frac{1}{1+\exp(-h)} \quad (4)$$

$$h = \beta 0 + \beta 1X1 + \beta 2X2 + \cdots + \beta kXk \quad (5)$$

3. Results

R software was used for data analysis

- Dependent variable was breast cancer biopsy outcome
- Independent variables were:
- Independent variable Measurement
- Age (<35, 35-55, >55)
- Sex (Male, Female)
- Menopause
- (Pre-menopause, peri-menopause, post menopause)
- Number of children (>6, 4-6, 1-3, 0)
- Age at first birth (≤30, >30, NA)
- Use of hormonal contraceptives (None Use)
- Personal history (Present, Not present)
- Family history (Present, Not present)
- Prior breast surgery (Present, Not present)
- Education level (Beyond high school, High school, Primary and below)
- Mass size (None, <2cm, 2-5cm, >5cm)
- Pain (Present, Not present)
- Nipple discharge (Present, Not present)
- Breast swelling (Present, Not present)
- Breast density (Present, Not present)
- Calcification (Present, Not present)

3.1 Descriptive statistics of the data

Biopsy outcome was coded as 0=benign and 1=malignant.

3.1.1 Age

Majority of breast cancer patients were between ages 35-55 with a frequency of 179. The age 35-55 was coded as 1 as shown below. The age group<35 was coded as 0 and >55 was coded as 2.

```
    biopsy
age   0   1
  0  37  40
  1  21 179
  2   5  88
```

3.1.2 Education

Majority of patients with breast cancer were in the category of primary education and below which was coded as 2. This category had a frequency of 119. Breast cancer patients who had an education level of beyond high school were 86 and were coded as 0. Those who had high school education were coded as 1and had a frequency of 102. The data suggest that cancer risk decreases with increase in the level of education.

```
          biopsy
education   0   1
        0  20  86
        1  35 102
        2   8 119
```

3.1.3 Sex

Male patient was coded as 0 and a female patient was coded as 1. There were more women with breast cancer with a frequency of 302. All male patients had cancer with a frequency of 5.

```
    biopsy
sex   0   1
  0   0   5
  1  63 302
```

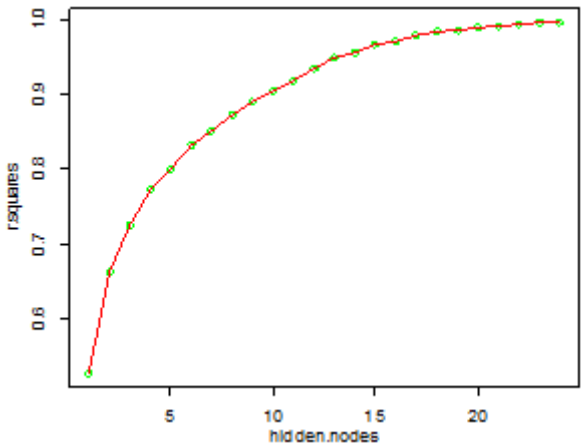
3.2 Artificial neural network model

A 3 layer feed forward neural network was fitted. The specific model was defined as shown below

Training data consisted of 320 observations out of 370.

nn.nnet=nnet (newx, y, data=datatrain, size=23, entropy=T, abstol=0.0001)

3.3 Identifying the number of hidden nodes



The optimal number of hidden nodes was the node with the highest coefficient of determination (R^2). A neural network of size [1-24] was matched with the respective R^2 value. R^2 was iterated 1000 times and the mean was obtained for each size of the ANN. Hence a curve of R^2 against the respective

hidden nodes was plotted to determine the optimal number of nodes as shown above. The optimal size was found to be 23 with an R^2 of 0.996

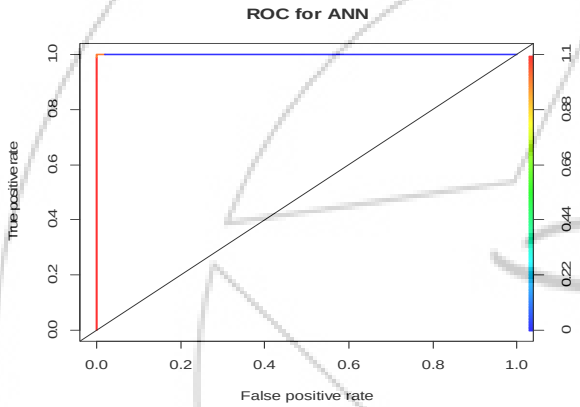
3.4 Sensitivity analysis for the ANN

Sensitivity = 1 { (Misclassification Error when Response = TRUE)
Specificity = 1 { (Misclassification Error when Response = FALSE)

predicted.biopsy.outcome	original.biopsy.outcome 0	1
0	55	0
1	0	265

There were no false positives and no false negatives. Hence artificial neural network has a very good predictive capability

3.5 Receiver operating Curve for the neural network




```
Call:  glm(formula = biopsy ~ age + meno + ph + b.density + calcif,
    family = binomial, data = datatrain)

Coefficients:
(Intercept)         age1         age2        meno1        meno2          ph1
     -3.287        1.901        2.855       -2.961       -0.187        3.288
 b.density1      calcif1
      3.554        5.553

Degrees of Freedom: 319 Total (i.e. Null);  312 Residual
Null Deviance:      294
Residual Deviance: 79.5         AIC: 95.5
```

Hence the reduced model was found to be: Call: glm(formula = biopsy ~ age + menopause + personal.history + breast.density + calcification, family = binomial(logit), data = datatrain) (As shown in appendix **[ii]**)

However even though personal history was not significant in the full model, it was included in the reduced model. Personal history is known to be a high risk factor for breast cancer. A patient who had had breast cancer in one breast can have recurrence of cancer in the same breast, in the other breast or in both breasts.

3.6 Logistic regression

- Model selection
  The significant independent variables at 5% level of significance were
- Age
  Patients aged between 35-55 years were at a higher risk of breast cancer.
- Education
  Patients who had an education level of primary and below were at a higher risk of breast cancer. This could be due to ignorance
- Breast density
  Patients with dense breast are deemed to have a higher risk of breast cancer.
- Calcification
  Patients with micro-calcification are at a higher risk of breast cancer
  (As shown in appendix**[i]**)
  Out of the 21 variables, only 4 variables were significant, hence a reduced model was deemed necessary

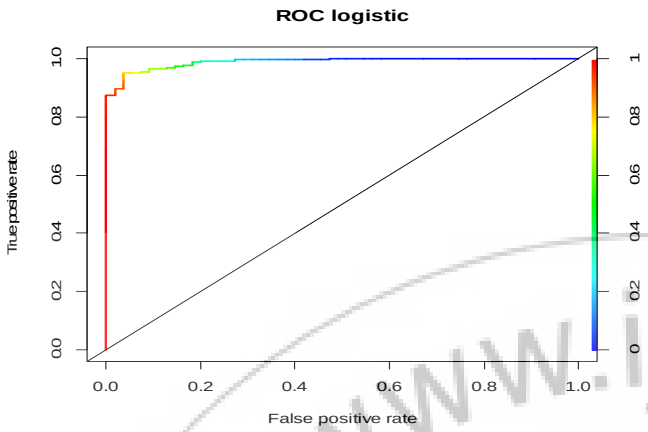
3.7 Obtaining a reduced model using stepAIC for stepwise regression

3.8 Sensitivity analysis

predicted.biopsy.outcome	original.biopsy.outcome 0	1
0	47	7
1	8	258

There were 7 false positives and 8 false negative.

3.9 Receiver Operating Curve for the logistic regression



AUC for logistic model was 0.9890909 while AUC for ANN was 1. Hence ANN was found to be a better model than logistic regression model in terms of discrimination capability.

3.10 Predicting biopsy outcome using test data

Predicted ANN output	*Original biopsy outcome*	*Predicted logistic output*
0.0000000000	0	0.0078638287
1.0000000000	1	0.9999475275
0.0000009390	0	0.0495028208
0.9999981442	1	0.9974520437

The predicted outcome was approximately the same as the original biopsy outcome for both models.

4. Summary and Conclusions

The authors' artificial neural network has high discriminative performance and can accurately predict breast cancer risks.
According to the authors' logistic regression the following were the crucial breast cancer risks; age, menopause age, personal history, education, breast density and micro-calcification.

Most breast cancer patients were aged between 35-55 years which is a younger age compared to the age of breast cancer patients in developed countries.

5. Limitations

- Missing information in patients files
- Long duration to obtain ethical clearance

6. Recommendations

The Kenyan government should increase breast cancer awareness campaign. Kenyatta National Hospital should computerize all patients' information to reduce missing information. Further research using a larger data set is recommended

7. Conflict of interest declaration

No conflict of interest.

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Appendices

[i]

```
Call:
glm(formula = biopsy ~ age + sex + meno + N.child + first.birth +
    pills + ph + fh + b.surg + edu + m.size + duration + n.retract +
    skin.c + l.node + progr + pain + n.discharg + b.swell + b.density +
    calcif, family = binomial, data = datatrain)

Deviance Residuals:
    Min       1Q   Median       3Q      Max
-2.4804   0.0014   0.0086   0.0431   2.4657

Coefficients:
             Estimate Std. Error z value Pr(>|z|)
(Intercept)    5.4607  1612.7192    0.00  0.99730
age1           2.6691     1.2877    2.07  0.03819 *
age2           2.8506     2.0285    1.41  0.15995
sex1         -13.9824  1612.7169   -0.01  0.99308
meno1         -2.7878     1.6958   -1.64  0.10018
meno2         -0.0914     1.5665   -0.06  0.95350
N.child1       0.9849     1.7027    0.58  0.56296
N.child2       1.9490     1.5951    1.22  0.22175
N.child3      11.2076    16.2044    0.69  0.48916
first.birth1  -1.4465     1.8188   -0.80  0.42642
first.birth2  -7.3794    15.9547   -0.46  0.64371
pills1         0.5461     0.9830    0.56  0.57855
ph1            1.6218     1.3395    1.21  0.22600
fh1            1.3545     1.3367    1.01  0.31093
b.surg1        1.8137     1.3589    1.33  0.18199
edu1           1.2014     1.1991    1.00  0.31639
edu2           2.6306     1.3308    1.98  0.04807 *
m.size1       -0.9269     1.7899   -0.52  0.60455
m.size2       -0.8377     1.3564   -0.62  0.53684
m.size3       -1.5583     1.6113   -0.97  0.33350
duration1     -0.6876     2.0312   -0.34  0.73499
duration2      0.9014     2.2200    0.41  0.68471
duration3      0.9423     2.0360    0.46  0.64348
n.retract1    -0.2402     1.3420   -0.18  0.85794
skin.c1        0.4488     1.0923    0.41  0.68115
l.node1       -0.1883     0.9010   -0.21  0.83446
progr1         0.9639     1.0602    0.91  0.36328
pain1         -0.5537     0.8656   -0.64  0.52243
n.discharg1   -0.4786     1.0368   -0.46  0.64434
b.swell1       1.5275     1.0347    1.48  0.13988
b.density1     4.6694     1.2556    3.72  0.00020 ***
calcif1        7.3862     1.9428    3.80  0.00014 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 293.662  on 319  degrees of freedom
Residual deviance:  64.074  on 288  degrees of freedom
AIC: 128.1

Number of Fisher Scoring iterations: 16
```

[ii]

```
Call:  glm(formula = biopsy ~ age + meno + ph + b.density + calcif,
    family = binomial, data = datatrain)

Coefficients:
(Intercept)        age1        age2       meno1       meno2         ph1
     -3.287       1.901       2.855      -2.961      -0.187       3.288
 b.density1     calcif1
      3.554       5.553

Degrees of Freedom: 319 Total (i.e. Null);  312 Residual
Null Deviance:      294
Residual Deviance: 79.5         AIC: 95.5
```

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