









$$\begin{aligned} \cos(\theta) &= \sin(\delta) \sin \varphi \cos(\beta) - \sin(\delta) \cos(\varphi) \sin(\beta) \cos(\gamma) \\ &+ \cos(\delta) \cos(\varphi) \cos(\beta) \\ \cos(\omega) &+ \cos(\delta) \sin(\varphi) \sin(\beta) \cos(\gamma) \cos(\omega) \\ &+ \cos(\delta) \sin(\beta) \sin(\gamma) \sin(\omega) \end{aligned} \quad (3)$$

For horizontal surface  $\beta=0$ . Thus,

$$\cos(\theta) = \cos(\delta) \cos(\varphi) \cos(\omega) + \sin(\delta) \sin(\varphi) \quad (4)$$

$$\sin(\alpha) = \cos(\delta) \cos(\varphi) \cos(\omega) + \sin(\delta) \sin(\varphi) \quad (5)$$

$$\tan(\gamma_s) = \frac{\sin(\omega)}{\sin(\varphi) \cos(\omega) - \cos(\varphi) \tan(\delta)} \quad (6)$$

$$\omega_o = \cos^{-1}[-\tan(\varphi) \tan(\delta)] \quad (7)$$

$$\text{It } N = \frac{2}{15} \cos^{-1}[-\tan(\varphi) \tan(\delta)] \quad (8)$$

$$H_o (\text{J/m}^2) = \frac{86400}{\pi} I_{sc} \left[ 1 + 0.033 \cos\left(\frac{360 ND}{365}\right) \right] * (\cos\varphi \cos\delta \sin\omega_o + \omega_o * \sin\varphi \sin\delta) \quad (9)$$

$$\frac{H_g}{H_o} = a + b \left(\frac{n}{N}\right) \quad (10)$$

$a = 0.25$  and  $b = 0.5$  are recommended and applicable anywhere in the world [20].

$$H_d = H_g (1.354 - 1.57 \overline{K_T}) \quad (11)$$

$$H_b = H_g - H_d \quad (12)$$

$$\frac{H_T}{H_g} = \left(1 - \frac{H_d}{H_g}\right) R_b + \frac{H_d}{H_g} R_d + R_r \quad (13)$$

For south facing surface,  $\gamma = 0^\circ$

$$R_b = \frac{\omega_{st} \sin \delta \sin(\theta - \beta) + \cos \delta \cos \omega_{st} \cos(\theta - \beta)}{\omega_s \sin \delta \sin \theta + \cos \delta \cos \omega_s \cos \theta} \quad (14)$$

$$R_d = \frac{1 + \cos \beta}{2} \quad (15)$$

$$R_r = \rho \left(\frac{1 - \cos \beta}{2}\right) \quad (16)$$