

Review Paper on: Image Processing Using Smooth Ordering of its Patches

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Abstract: *Now days, image processing field with its patches becomes highly popular. This reviewed system is based on image processing scheme with reordering of its patches. In this extract all patches with overlaps of an corrupted image, then reorders these patches as co-ordinates in high dimensional space and then order these patches so that they can form sequence in "shortest possible path", for solving travelling salesman problem. The obtained sequence then applied to the corrupted image to carry out permutation of the image pixels to obtain what should be a regular signal. By using relatively simple one-dimensional smoothing operations such as filtering or interpolation to the reordered set of pixels, by this we can obtain good recovery of clean image from corrupted one. Explore the use of this approach to image denoising and inpainting, and show promising result in both cases.*

Keywords: Pixel permutation, Patch-based processing, Travelling salesman problem, Denoising, Inpainting.

1. Introduction

Now days, image processing field with its local patches become highly popular and was shown highly effective for representing work. The idea behind this is: extract all possible patches of the given image to be processed which are very small as compared to original image. A typical patch size would be 8×8 pixels. The processing is carried out by operating on these patches and exploiting interrelations between them. The manipulated patches are then put back into the image to form the resulting clean image.

In various ways, the relation between the patches can be taken into account: Weighted averaging of pixels with similar surrounding patches, as NL-Means algorithm does, clustering the patches into disjoint sets and treating each set as different, seeking a representative dictionary for the patches and using it to sparsely represent them, gathering groups of similar patches and applying a sparsifying transform on them. A common method for this is to expect that every patch from image may find similar to extracted patch. The image patches are believed to exhibit a highly-geometrical form in the embedding space they reside in. A joint treatment of patches supports reconstruction process by applying non-local force, thus enables better recovery.

In this paper, we are adopting the core idea of reordering the patches. Thus, propose a very simple image processing scheme that depend solely on patch reordering. Firstly, extract all the patches of size with maximal overlaps. After extracting all patches, neglect their spatial relationships and seek a new way to organize them. refer to these patches as a cloud of vector/points in R^n , then order these patches so that they can form sequence in "shortest possible path", for solving travelling salesman problem. A key assumption is concurrency between two image patches implies concurrency between their center pixels. Therefore, if given image is of high quality, the new ordering of patches should be highly

regular one dimensional ordering of image pixels, being the center of these patches. When image is declined with noise or contains missing pixels, the ordering of patch must be robust. Thus, applying relatively simple one dimensional smoothing operation such as filtering or interpolation, to the altered set of pixels should enable good recovery of clear image.

The core process proposed in the paper is: For a given corrupted image, they altered its pixels, operate on the new one dimensional signal using simplified algorithms and transfer the resulting values to their original location [14]-[15]. Proposed method is applied to several randomly constructed orderings and combined with a proposed subimage averaging scheme, is able to lead to state-of-the-art results. With proposed scheme explore that it achieves better result for medium and high noise level BM3D algorithm [10]. It also explore image inpainting and show that it provides better results compared to ones obtained with a simple interpolation scheme and the method which employs sparse representation modeling via redundant DCT dictionary.

2. Image Processing Using Patch Ordering

2.1 Basic scheme

Let Y be an image of size $N = R \times C$, and let Z be a noisy or corrupted version of Y . Also, let y and z be the column stacked versions of Y and Z , respectively. A column stacked version of a matrix is a column vector, which is created by concatenating the columns of the matrix one by one. Then the corrupted image satisfies

$$z = M y + v \quad (1)$$

where the $N \times N$ matrix M denotes a linear operator which corrupts the data and v denotes an additive white Gaussian noise independent of y with zero mean and variance σ^2 . To

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reconstruct y from z this method employ a permutation matrix P of size $N \times N$. It is assumed that when P is applied to the target signal, it produces a smooth signal.

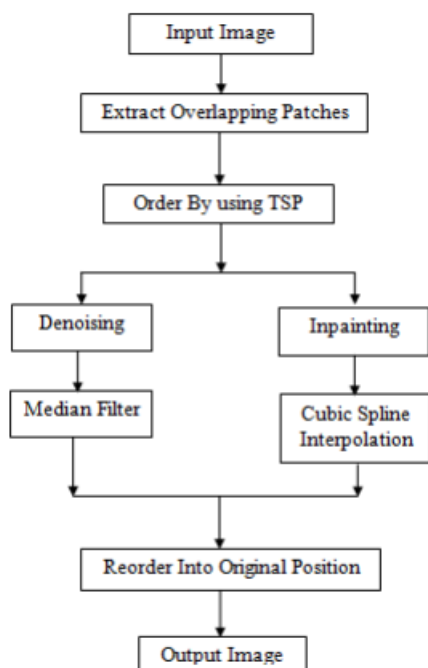


Fig. 1. Outline of the proposed method

This method starts by applying the permutation matrix P to z and obtain $z^p = Pz$. After that it applies a simple one dimensional smoothing operator H such as interpolation or filtering on z . And finally, it applies inverse permutation matrix P^{-1} to the result, and obtains the reconstructed image.

$$\hat{y} = P^{-1} H \{Pz\} \quad (2)$$

We use concept of “cycle spinning” method to better smooth the recovered image. For that, we randomly construct K different permutation matrices P_k , utilize each to denoising the image z and then average the results. This can be expressed by

$$\hat{y} = 1/k \sum_{k=1}^k P_k^{-1} H \{P_k z\} \quad (3)$$

2.2 Building the permutation matrix

In order to design the permutation matrix P for the corrupted image that may be noisy or containing missing pixels, any permutation defined by simply altering the corrupted pixels into a regular signal does not necessarily smooth. Since the pixels in the corrupted image are not helpful a suboptimal

* $\{j_2\}$ with probability

$$p_2 \propto \exp \left[-\frac{\omega(x_{\Omega(k)}, x_{j_2})}{\epsilon} \right]$$

Output: The set Ω holds the proposed ordering.

2.3 Subimage Averaging

The distances between the patches can also be used in the reconstruction process of the sub images. For the purpose of

ordering operation i.e. patches from the corrupted image are used.

Let y_i and z_i denote the i^{th} samples in the vectors y and z , respectively. Let x_i denotes the column stacked version of the $\sqrt{n} \times \sqrt{n}$ patch around the location of z_i in Z . It is assumed that under a distance measure $\omega(x_i, x_j)$, proximity between the two patches x_i and x_j suggests proximity between the uncorrupted versions of their centre pixels y_i and y_j , so the points x_i should be reordered so that they form a smooth path, hoping that the corresponding reordered one dimensional signal $y^p = py$ will also become smooth.

In the approximate travelling salesman problem, the proposed method restricts the nearest neighbor search for each patch to a surrounding square neighborhood containing $B \times B$ patches. When only one unvisited patch remains in that neighborhood, it simply continues to this patch, and in the case that no unvisited patches remain, it searches for the first and second nearest neighbors among all the unvisited patches in the image. This restriction decreases the overall computational complexity, and with a proper choice of B it could leads to improved results. The permutation applied by the matrix P is defined as the order in the found path.

Algorithm for Patch Altering-

Task: Reorder the image patches x_j .

Parameters: We are given image patches $\{x_j\}_{j=1}^N$, the distance function ω and ϵ which is used in the probabilistic part of the algorithm.

Initialization: Choose a random index j and set $\Omega(1) = \{j\}$.

Main theorem: Perform the following steps for $k=1, \dots, N-1$

- Set A_k to be the set of indices of the $B \times B$ patches around $x_{\Omega(k)}$.
- If $|A_k \setminus \Omega| = 1$
 - Set $\Omega(k+1)$ to be $A_k \setminus \Omega$.
- Else
 - If $|A_k \setminus \Omega| \geq 2$
 - * Find x_{j_1} - the nearest neighbor to $x_{\Omega(k)}$
 - Such that $j_1 \in A_k$ and $j_1 \notin \Omega$.
 - *Find x_{j_2} - the second nearest neighbor to $x_{\Omega(k)}$
 - Such that $j_2 \in A_k$ and $j_2 \notin \Omega$.
 - Else if $|A_k \setminus \Omega| = 0$
 - * find x_{j_1} - the nearest neighbor to $x_{\Omega(k)}$
 - Such that $j_1 \in A_k$ and $j_1 \notin \Omega$.
 - * Find x_{j_2} - the second nearest neighbor to $x_{\Omega(k)}$
 - Such that $j_2 \in A_k$ and $j_2 \notin \Omega$.
 - Set $\Omega(k+1)$ to be:
 - * $\{j_1\}$ with probability
 - $$p_1 \propto \exp \left[-\frac{\omega(x_{\Omega(k)}, x_{j_1})}{\epsilon} \right]$$

averaging, starting from top most left to right, we extract all the patches column by column. For the calculation of permutation matrix P , we assume that every patch is associated only with its middle pixel. P is designed to alter the signal made by middle points in the patches, which lies in middle of pixel row X . Also we can alternatively choose patches to associate them with a pixel lies in some different position. The role of matrix P is to alter any one out of all

signals located in the rows of X. These all signals are column stacked versions of all the subimages contained in corrupted image Z. When all the sub images of noisy images are active in its denoising process, we get improved denoising results. In our system, we also use similar technique in order to improve the quality of the recovered image.

2.4 Connection to BM3D and Clustering-Based Methods

The BM3D algorithm [12] bundle the image patches into groups. After grouping, implements 1D mechanism on patches. Then return the patches into their place in original image and finally average the results [4]. Before performing 1D processing on the patches, BM3D algorithm also applies a 2D transform to the patches. This feature can be used in our proposed method. BM3D algorithm creates a group of neighbors for each patch where it structures all the patches into one chain, which describes local neighbors [10]-[12]. Feature of BM3D algorithm is that the patch order in each group is not restricted. But in our proposed method, order of patches is determined attentively as it plays major role. The 1D processing applied by the BM3D consists of the use of a 1D transform, followed by thresholding and the inverse transform, implying a specific denoising.

Algorithm Steps:

- Perform grouping and sampling process for a noisy image. Add 2D spatial coordinate that belongs to image domain with original image
- Measure the block-distance by using a coarse prefiltering.
- Taking results from step 2 a new set can be obtained whose elements are the coordinates of the blocks that are similar to Resultant Image.
- Obtain fixed parameter match τ_{match}^h from deterministic speculations about the acceptable value of the ideal difference, mainly ignoring the noisy components of the image.
- Perform block-matching, by comparing a single pixel gray value, with another according to the gray distribution.
- A pixel is denoted as $v(r, c)$, whose horizontal and vertical gradients as follows respectively

$$V_x = V(r, c) - V(r, c-1)$$

$$V_y = V(r, c) - V(r-1, c)$$

3. Applications

3.1 Image Denoising

Image denoising is very fundamental challenges in the field of image processing and computer vision. Our focus is to obtain the original image by suppressing noise from a noise-contaminated version of the image. Image denoising can be caused by different conditions which are often not possible to avoid in practical situations. So, it plays an important role in a wide range of applications such as image restoration, visual tracking, image registration, image segmentation, and image classification, where obtaining the original image content is vital for strong performance. Different approaches for denoising are spatial adaptive filters, stochastic analysis, partial differential equations, transform-domain methods, and

other approximation theory methods, morphological analysis, differential geometry, order statistics. The main properties of a good image denoising model are that it will remove noise while preserving edges [9].

There are basically two types of model for filtering i.e. linear and non linear. One common approach is to use a Gaussian filter. For some purposes this kind of denoising is adequate. One big advantage of linear noise removal models is the speed but a drawback is that they are not able to preserve edges in a good manner. Nonlinear models on the other hand can handle edges in a much better way than linear models can. Most popular models for nonlinear image denoising are the Median filter and Total Variation (TV)-filter. Linear filter is the filtering in which the value of an output pixel is a linear combination of neighborhood values, which can produce blur in the image. Thus a variety of smoothing techniques have been developed that are non linear [4].

Image de-noising is additionally referred to as filter, it's the method of removing the assorted forms of noise or unwanted data gift in a picture primarily based upon their properties whereas keeping the main points of the image preserved. Image filtering isn't solely accustomed improve the image quality however additionally used as a preprocessing stage in several applications as well as image encryption, pattern recognition. General purpose image filter lack the flexibility and adaptability of un-modeled noise sorts.

Pictures area unit typically corrupted by random variations in intensity, illumination, or have poor distinction and cannot be used directly. The term Filtering is outlined as rework component intensity values to reveal sure image characteristics

- Enhancement: improves distinction
- Smoothing: take away noises
- Template matching: detects better-known patterns.

Image denoising consists of 2 steps. First is noise detection and another one is noise replacement. The noise detection is that the opening move, location of noise is known. The noise replacement is that the second step, within which the detected reedy pixels area unit replaced by the calculable values.

Median Filter

Median filter is that the easy and powerful filter. It's used for reducing the number of intensity variation between one component and also the alternative component. During this filter, we tend to replace component worth with the average. The median is calculated by initial sorting all the component worth's into ascending order so replaces the component being calculated with the center component value.

$$L(u, v) \text{ mid } \{|(u+i, v+j)|(i, j) \in R\}$$

- Step 1: Put the pixel values of the surrounding (of noisy pixel) pixels in a single dimensional array
- Step 2: Sort this array in ascending order
- Step 3: The noisy pixel value is replaced by middle element of the sorted array.

Syntax to remove the salt and pepper noise using median filter:

- Read the image from the file system to matrix I
- Creates a new figure to show the image.
- Show the loaded image as a figure1.
- Apply median filter using the function medfilt2.
- Show image after applying the filter as a figure2.
- Write the new image to the file system.

3.2 Image Inpainting

Image inpainting also referred as image retouching. Inpainting is the process of reconstructing lost or deteriorated parts of an images based on the background information in a visually logical way. It consists of filling in the missing areas or modifying the damaged pixels in a non-exposable way by an observer, not familiar with the original images. Different approaches of image inpainting scheme are restoration of photographs, films and paintings, to removal of occlusions, such as text, subtitles, stamps and publicity from images. Inpainting can also be used to produce special effects [17].

Large areas with lots of information lost are harder to reconstruct, because information in other parts of the image is not enough to get an impression of what is missing. Details that are completely hidden/occluded by the object to be removed cannot be recovered by any mathematical method. Therefore the objective for image inpainting is not to recover the original image, but to create some image that has a close resemblance with the original image [12].

4. Assessment on ordering of patches

Idan Ram, Michael Elad propose that Image processing using smooth ordering have proposed a new image processing scheme which depends on smooth 1D ordering of the pixels in the given image. The scheme accomplishes high quality outcomes for image denoising and inpainting, using permutation matrices and 1D operation such as linear filtering and interpolation. Proposed scheme practices the distances between the patches not only to find the ordering matrices, but also in the reconstruction process of the subimages. These distances between patches consist of some additive information which might be help in enhancement of results. Enhancement in results can also be made to the patch altering scheme. A different direction is to develop new image processing algorithms which involve optimization problems in which the 1D image reordering act as regularizes. This may lead improvement in both image denoising and inpainting results. The proposed image denoising scheme can be developed by dividing the patches to more than two types, and operating each type differently [1].

W. Dong, X. Li, L. Zhang, and G. Shi, proposed in “Sparsity-based image denoising via dictionary learning and structural clustering,” from complex point of view, it is instructive to understand the relationship between dictionary learning and structural clustering, in Cluster based Sparse Representation (CSR). The collection of patches of natural images would form a nonlinear complex structure in many

circumstances. Identification of local geometry of such nonlinear complex structure is attracted issue in now days. The term image denoising can also be fits in the framework of complex learning/reconstruction. Dictionary learning such as K-SVD algorithm separates image signals from additive noise by change-of-coordinates, while structural clustering such as BM3D achieves the same objective by locally fitting the hyper surface in the patch space i.e., iterative shrinkage [4].

Guoshen YU, Guillermo SAPIRO, and St'ephane MALLAT gives in “Solving inverse problems with piecewise linear estimators: from gaussian mixture models to structured sparsity,” that patch based models are simple to understand, less complex and to work with than entire image models. We have shown that patch models which give great reasonable result for patches sampled from natural images carry out advance in patch and image restoration task. By result, these recommended framework permitted the use of patch models for entire image restoration, stimulate through the concept that restored image should be under the preceding. Early days used this framework which increase the result of whole image restored image significantly when compared to simple patch averaging. At the end here we set a latest, simple as well rich Gaussian Mixture which performs specifically well on image denoising. Although the manifest our framework by few priors, best strengths is that serve as a “plug-in” system. It can work with any current patch restoring method. BM3D and LLSC are patch based methods which use simple patch averaging, possibly best result of this work, and the direction in which much is left to be explored, is the stellar performance of the GMM Model. Use of GMM Model is acutely simple, Gaussians mixture full covariance matrices. So that Gaussian Mixtures studied area that combines more sophisticated machinery into research learning and representation of this model occupy much assurance and this outcome from the research [7].

P. Chatterjee and P. Milanfar proposed that Gaussian mixture models (GMM) and a MAP-EM algorithm furnish general and computational dynamic solutions. The result is same as state-of-the-art in various image inverse problems. A dual mathematical analysis of the framework with structured sparse estimation displays that the occurring piecewise linear estimate stabilizes and improves the traditional sparse inverse problem approach. Also this connection advice dynamic dictionary triggered initialization for the MAP-EM algorithm. The same application can be used in a number of image restoration applications, such as inpainting, zooming, and deblurring, to produce either equal or often better results than the best published ones, with computational complexity typically one or two magnitude smaller than sparse estimations [9].

M. Elad and M. Aharon proposed in “Image denoising via sparse and redundant representations over learned dictionaries,” that many patch based processing schemes for corrupted image are exists. The proposed novel sparse representation based image deblurring and super-resolution method using adaptive sparse domain selection (ASDS) and adaptive regularization (AReg) acknowledge the case that the optimal sparse domains of natural images can range

significantly across different images and different image patches in a single image. For that select attentively the dictionaries that were pre-learned from a dataset of high quality example patches for each local patch. The ASDS powerfully improves the effectiveness of sparse modeling and subsequently the results of image restoration. For further enhancement of quality of reconstructed images, method proposed two AReg terms into the ASDS based image restoration framework. It is proven experimentally on natural images that the proposed ASDS-AReg approach exceeds many state-of-the-art methods in both PSNR and visual quality [13].

D. Zoran and Y. Weiss proposed that Cluster based denoising presented a general framework for image denoising based on learning a geometric descriptor using local kernels. The outcome of this approach comes under a class that can be categorized as kernel regression based, and whose aim is to learn the best global dictionary. The proposed way is to cluster the image using meaningful features to understand the underlying geometry in the presence of noise. A dictionary is analyzed for each of the clusters to carry out the generalized kernel regression to form denoised evaluation for each pixel. Method proposed new way to bring out each of steps namely, clustering, dictionary learning, and coefficient calculation. Each block can be replaced by approximately similar equitable. Performance of cluster based denoising seems to be competitive, qualitative as well as quantitative as it is compared with state of art denoising. This method is sensitive for large number of clusters within a particular range. Use of K-means algorithm assembles the optimal number of clusters automatically. Other unsupervised algorithm such as mean shift method can be taken into account for the same. Feature of cluster based denoising stage is the selection of an informative distance metric [17].

5. Conclusions

A new image reconstruction scheme using smooth one dimensional ordering of the pixels in the image is proposed in this paper. It can be implemented by using a carefully designed permutation matrix and simple one dimensional operation such as linear filtering and interpolation. This scheme can be used for image denoising and inpainting. For image denoising it treats the smooth areas and edges differently and uses the Median filter which gives a good result for medium and high noise levels. For image inpainting it uses cubic spline interpolation which yields better results compared to the ones obtained with a simple interpolation scheme. The proposed method can be extended in several ways. The other distance measures can be used. The distances between the patches can also be used in the reconstruction process of the sub images. The proposed image denoising scheme may be improved by dividing the patches to more than two types, and treating each type differently.

We have proposed a new image processing scheme which is based on smooth one dimensional ordering of the pixels in the given image. We have shown that using a carefully designed permutation matrices and simple and intuitive one

dimensional operations such as linear filtering and interpolation, the proposed scheme can be used for image denoising and inpainting, where it achieves high quality results. Therefore, we tend to specialize in the image denoising, the planned ways area unit utilized in order to scale back the unwanted data or distortion that is termed as noise which will be caused by the external force whereas a picture is being transmitted, where as transmittal a picture knowledge over Associate in Nursing unsecure channel, a noise also can be other by effort.

6. Other recommendations

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