



























	③	②	④	①	①	③	
Taxon 1:	A	G	C	T	G	A	A
Taxon 2:	A	A	T	C	T	T	A
Taxon 3:	T	C	A	G	A	T	T

$sr^5 x_5 =$

	④	①	③	②	①	③	
Taxon 1:	A	G	C	T	G	A	A
Taxon 2:	A	A	T	C	T	T	A
Taxon 3:	T	C	A	G	A	T	T

**Remark 9:** We refer to ①, ②, ③, ④, ⑤ and ⑥ in example 1 to the frequencies of the patterns in DNA sequences.

## References

- [1] A. Dobra, "Markov bases for decomposable graphical models", Paper presented at Grostat V, New Orleans, 4-6 September 2001, submitted for publication, 2001.
- [2] Dobra, and S. Sullivant, "A divide-and-conquer algorithm for generating Markov bases of multi-way tables", Paper presented at the workshop "Multidimensional tables" statistics, combinatorial optimization, and Groebner bases", University of California at Davis, submitted for publication, 15-16 February 2002.
- [3] Takemura, and S. Aoki, "Some characterizations of minimal Markov basis for sampling from discrete conditional distributions", Annals of the Institute of Statistical Mathematics, 2003.
- [4] Takemura, and S. Aoki, "Distance reducing Markov bases for sampling from discrete space", Bernoulli, to appear, 2005.
- [5] Semple, M. Steel, "Phylogenetics", volume 24 of Oxford Lecture Series in Mathematics and its Applications, Oxford University Press, Oxford, (2003).
- [6] Agnarsson, R. Greenlaw. "Graph theory, modeling, applications, and algorithms", United States of America, (2007).
- [7] H. Abbass and H. S. Mohammed Hussein "On Toric Ideals for  $3 \times n/3$  - Contingency Tables with Fixed Two Dimensional Marginals,  $n$  is a multiple of 3", European Journal of Scientific Research, Vol. 123, pp. 83-98, 2014.
- [8] H. Abbass and H. S. Mohammed Hussein "Generating  $3 \times n/3$  -Contingency Tables Using The Action of Dihedral Group  $D_n$ ,  $n$  is Multiple of 6", J. of Karbala for Mathematics, (accept), 2014.
- [9] Felsenstein, "Inferring Phylogenies", Sinauer Associates, Sunderland, (2003).
- [10] M. Dyer, and C. Greenhill, "Polynomial-time counting and sampling of two-rowed contingency tables", Theoretical Computer Sciences, 246, (2000), pp. 265-278.
- [11] P. Diaconis, and B. Sturmfels, "Algebraic algorithms for sampling from conditional distributions", The Annals of Statistics, 26, pp. 363-397, (1998).
- [12] S. Aoki, A. Takemura, "The largest group of invariance for Markov bases and toric ideals", J. Symbolic Computation 43 (5) (2008) 342-358.
- [13] S. Aoki, and A. Takemura, "The list of indispensable moves of unique minimal Markov basis of  $3 \times 4 \times K$  and  $4 \times 4 \times K$  contingency tables with fixed two-dimensional

marginals", Technical Report METR 03-38, Department of Mathematical Engineering and Information Physics, The University of Tokyo. Submitted for publication, (2003).

- [14] S. Aoki, and A. Takemura, "Minimal basis for connected Markov chain over  $3 \times 3 \times K$  contingency tables with fixed two-dimensional marginals". Australian and New Zealand Journal of Statistics, 45, pp. 229-249, (2003).
- [15] S. Aoki, and A. Takemura, "Minimal Invariant Markov Basis for Sampling Contingency Tables with Fixed Marginals", Annals of the Institut of Statistical Mathematics, pp.230-256, 2006.
- [16] S. Sullivant, J. Rauh, T. Kahle. "Positive Margins and Primary Decomposition", North Carolina State, pp.1-22, 2012.
- [17] W. J. Gilbert, "Modern Algebra With Application", John Wiley, Inc., New Jersey, U.S.A, 2004.