

$$F \left\{ \begin{array}{l} M(Sw, Tz, kt), M(Aw, Bz, t), M(Sw, Aw, t), \\ M(Tz, Bz, t), M(Sw, Bz, t), M(Tz, Aw, t) \end{array} \right\} = F(M(Sw, z, kt), 1, M(Sw, z, t), 1, M(Sw, z, t), 1) \geq 1$$

and

$$F \left\{ \begin{array}{l} N(Sw, Tz, kt), N(Aw, Bz, t), N(Sw, Aw, t), \\ N(Tz, Bz, t), N(Sw, Bz, t), N(Tz, Aw, t) \end{array} \right\} = F(N(Sw, z, kt), 0, N(Sw, z, t), 0, N(Sw, z, t), 0) \leq 0$$

And, by (F-2), we have $z = Sw = Aw$. Since $Sw = Aw = z$ and S, A are compatible of type (α) , we have $z = Sz = SAw = AAw = Az$ and thus $z = Az$. Consequently, z is a common fixed point of S, T, A and B . The same result holds if we assume that T is continuous instead of S .

Finally, we show that the point z is unique common fixed point of S, T, A and B . Suppose that S, T, A and B have another common fixed point z_1 . Then, by (4), we have, for any $t > 0$,

$$F \left(\begin{array}{l} M(Sz, Tz_1, kt), M(Az, Bz_1, t), M(Sz, Az, t), \\ M(Tz_1, Bz_1, t), M(Sz, Bz_1, t), M(Tz_1, Az, t) \end{array} \right) = F(M(z, z_1, kt), M(z, z_1, t), 1, 1, M(z, z_1, t), M(z, z_1, t)) \geq 1, \text{ and}$$

$$F \left(\begin{array}{l} N(Sz, Tz_1, kt), N(Az, Bz_1, t), N(Sz, Az, t), \\ N(Tz_1, Bz_1, t), N(Sz, Bz_1, t), N(Tz_1, Az, t) \end{array} \right) = F(N(z, z_1, kt), N(z, z_1, t), 0, 0, N(z, z_1, t), N(z, z_1, t)) \leq 0$$

Thus, (F-3), we have $M(z, z_1, kt) \geq M(z, z_1, t)$ and $N(z, z_1, kt) \leq N(z, z_1, t)$. From lemma-7.1, we have $z = z_1$. This completes the proof.

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