

# Digital Image Compression and Analysis

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**Abstract:** *Today Medical Imaging is a important discipline for research since the biological imaging which incorporates radiology and nuclear medicine needs high resolution images for medical procedures seeking to reveal, diagnose and examine the disease. Compression and analysis of image using high resolution grid and SPIHT encoding technique is a novel approach to address this issue Firstly the original image is converted in to low resolution (less size) image, then quantization and SPIHT encoding, techniques are applied to compress the image. To restore the original image, the compressed image is decompressed (dequantized & decoded) and interpolation techniques using high resolution grid (tukey window and PG algorithm) are applied to achieve high resolution decompressed image. The PSNR of the high resolution decompressed image is high compared to PSNR of low resolution original image. At last we found the compression ratio is directly proportional to PSNR.*

**Keywords:** SPIHT, ROI Compression, MIC, Peak Signal to Noise Ratio (PSNR), Compression Ratio (CR), Tukey-wind, PG algorithm (Papoulis-Gerchberg method).

## 1. Introduction

### 1.1 Background

Image compression is the process of identifying and removing redundant data from images and then encodes it with a lossless or lossy encoder in such a way that the information is represented with less number of bits than the original image. Uncompressed high resolution images take lot of memory. For example, a single small 4" × 4" size colour picture, scanned at 300 dots per inch (dpi) with 24 bits/pixel of true colour, will produce a file containing more than 4 megabytes of data. This picture requires more than one minute for transmission by a typical transmission line (64k bit/second ISDN). Therefore large image files remain a major bottleneck in a distributed environment. This problem is generally overcome by various image compression techniques like JPEG compression. From the discussion it is clear that an image compression is essentially a quantization technique. Therefore at the receiver when the image is represented, there will be information loss which affects the overall resolution and clarity of the images. This is a major problem in medical images. With increasing number of medical image acquisition every day, storage, transmission and information preservation in such images have become a huge challenge. In this work we addressed this issue by proposing a novel technique for medical image compression and by showing the efficiency of the same.

In recent years, there have been significant advancements in algorithms and architectures for the processing of image, video, and audio signals. These advancements have proceeded along several directions. On the algorithmic front, new techniques have led to the development of robust methods to reduce the size of the image, video, or audio data. Such methods are extremely vital in many applications that manipulate and store digital data. Informally, we refer to the process of size reduction as a compression process. We will define this process in a more formal way later. On the architecture front, it is now feasible to put sophisticated compression processes on a relatively low-cost single chip;

this has spurred a great deal of activity in developing multimedia systems for the large consumer market.

One of the exciting prospects of such advancements is that multimedia information comprising image, video, and audio has the potential to become just another data type. This usually implies that multimedia information will be digitally encoded so that it can be manipulated, stored, and transmitted along with other digital data types. For such data usage to be pervasive, it is essential that the data encoding is standard across different platforms and applications. This will foster widespread development of applications and will also promote interoperability among systems from different vendors. Furthermore, standardisation can lead to the development of cost-effective implementations, which in turn will promote the widespread use of multimedia information. This is the primary motivation behind the emergence of image and video compression standards.

Compression is a process intended to yield a compact digital representation of a signal. In the literature, the terms *source coding*, *data compression*, *bandwidth compression*, and *signal compression* are all used to refer to the process of compression. In case, where the signal is defined as an image, a video stream, or an audio signal, the generic problem of compression is to minimise the bit rate of their digital representation. There are many applications that benefit when image, video, and audio signals are available in compressed form. **Without compression, most of these applications would not be feasible!**

**Example 1:** Let us consider facsimile image transmission. In most facsimile machines, the document is scanned and digitised. Typically, an 8.5x11 inches page is scanned at 200 dpi; thus, resulting in 3.74 Mbits. Transmitting this data over a low-cost 14.4 kbits/s modem would require 5.62 minutes. With compression, the transmission time can be reduced to 17 seconds. This results in substantial savings in transmission costs.

**Example 2:** Let us consider a video-based CD-ROM application. Full-motion video, at 30 fps and a 720 x 480 resolution, generates data at 20.736 Mbytes/s. At this rate,

only 31 seconds of video can be stored on a 650 MByte CD-ROM. Compression technology can increase the storage capacity to 74 minutes, for VHS-grade video quality.

## 2. Objectives

1. Study of Various Image compression Techniques.
2. Detailed study of SPIHT Encoding and Decoding Techniques.
3. To achieve high resolution image with low memory occupancy.
4. Implementation of New Image compression Technique which produces Best result in comparison with the state of the Art Techniques.
5. A Very High Compression ratio is to be obtained without losing much information in the image and image is to be compressed with minimum loss in quality.
6. Objective and Subjective Quality measures will be compared.
7. It is also proposed to compare the Execution Speed of the new algorithm with the state of the art.

Image, video, and audio signals are amenable to compression due to the factors below.

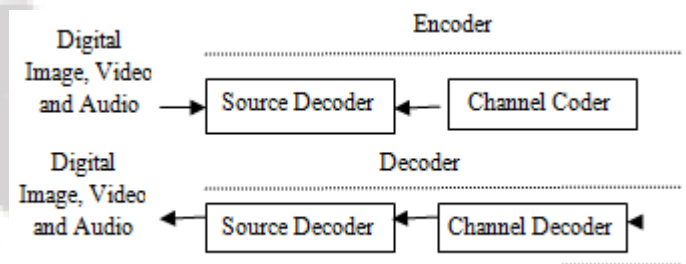
1. There is considerable statistical redundancy in the signal.
  2. Within a single image or a single video frame, there exists significant correlation among neighbour samples. This correlation is referred to as spatial correlation.
  3. For data acquired from multiple sensors (such as satellite images), there exists significant correlation amongst samples from these sensors. This correlation is referred to as spectral correlation.
  4. For temporal data (such as video), there is significant correlation amongst samples in different segments of time. This is referred to as temporal correlation.
- There is considerable information in the signal that is irrelevant from a perceptual point of view.
  - Some data tends to have high-level features that are redundant across space and time; that is, the data is of a fractal nature.

For a given application, compression schemes may exploit any one or all of the above factors to achieve the desired compression data rate. There are many applications that benefit from the data compression technology. Table 1.1 lists a representative set of such applications for image, video, and audio data, as well as typical data rates of the corresponding compressed bit streams. Typical data rates for the uncompressed bit streams are also shown.

**Table 1.1:** Applications for image, video, and audio compression

Application	Data	Rate
	Uncompressed	Compressed
Voice 8 ksamples/s, 8 bits/sample	64 kbps	2-4 kbps
Slow motion video (10fps) framesize 176x120, 8bits/pixel	5.07 Mbps	8-16 kbps
Audio conference 8 ksamples/s, 8 bits/sample	64 kbps	16-64 kbps
Video conference (15fps) framesize 352x240, 8bits/pixel	30.41 Mbps	64-768 kbps
Digital audio 44.1 ksamples/s, 16 bits/sample	1.5 Mbps	1.28-1.5 Mbps
Video file transfer (15fps) framesize 352x240, 8bits/pixel	30.41 Mbps	384 kbps
Digital video on CD-ROM (30fps) framesize 352x240, 8bits/pixel	60.83 Mbps	1.5-4 Mbps
Broadcast video (30fps) framesize 720x480, 8bits/pixel	248.83 Mbps	3-8 Mbps
HDTV (59.94 fps) framesize 1280x720, 8bits/pixel	1.33 Gbps	20 Mbps

In the following figure, a systems view of the compression process is depicted.



**Figure 1.1:** Generic Compression System

The core of the encoder is the source coder. The source coder performs the compression process by reducing the input data rate to a level that can be supported by the storage or transmission medium. The bit rate output of the encoder is measured in bits per sample or bits per second. For image or video data, a pixel is the basic element; thus, bits per sample is also referred to as bits per pixel or bits per pel. In the literature, the term *compression ratio*, denoted as  $c_r$ , is also used instead of *bit rate* to characterise the capability of the compression system. An intuitive definition of  $c_r$  is

$$c_r = \frac{\text{source coder input size}}{\text{source coder output size}}$$

This definition is somewhat ambiguous and depends on the data type and the specific compression method that is employed. For a still-image, size could refer to the bits needed to represent the entire image. For video, size could refer to the bits needed to represent one frame of video. Many compression methods for video do not process each frame of video, hence, a more commonly used notion for size is the bits needed to represent one second of video.

In a practical system, the source coder is usually followed by a second level of coding: the channel coder (Figure 1.1). The channel coder translates the compressed bit stream into a signal suitable for either storage or transmission. In most

systems, source coding and channel coding are distinct processes. In recent years, methods to perform combined source and channel coding have also been developed. Note that, in order to reconstruct the image, video, or audio signal, one need to reverse the processes of channel coding and source coding. This is usually performed at the decoder. From a system design viewpoint, one can restate the compression problem as a bit rate minimisation problem, where several constraints may have to be met, including the following:

- **Specified level of signal quality.** This constraint is usually applied at the decoder.
- **Implementation complexity.** This constraint is often applied at the decoder, and in some instances at both the encoder and the decoder.
- **Communication delay.** This constraint refers to the end to end delay, and is measured from the start of encoding a sample to the complete decoding of that sample.

Note that, these constraints have different importance in different applications. For example, in a two-way teleconferencing system, the communication delay might be the major constraint, whereas, in a television broadcasting system, signal quality and decoder complexity might be the main constraints.

### 3. Methodology

#### 3.1 Lossless versus lossy compression

##### 3.1.1 Lossless Compression

In many applications, the decoder has to reconstruct without any loss the original data. For a lossless compression process, the reconstructed data and the original data must be identical in value for each and every data sample. This is also referred to as a reversible process. In lossless compression, for a specific application, the choice of a compression method involves a trade-off along the three dimensions depicted in Figure 1.2; i.e coding efficiency, coding complexity and coding delay.

##### 3.1.2 Coding Efficiency

This is usually measured in bits per sample or bits per second (bps). Coding efficiency is usually limited by the information content or *entropy* of the source. In intuitive terms, the entropy of a source  $X$  provides a measure for the "randomness" of  $X$ . From a compression theory point of view, sources with large entropy are more difficult to compress (for example, random noise is very hard to compress).

##### 3.1.3 Coding Complexity

The complexity of a compression process is analogous to the computational effort needed to implement the encoder and decoder functions. The computational effort is usually measured in terms of memory requirements and number of arithmetic operations. The operations count is characterised by the term millions of operations per second and is often referred to as MOPS. Here, by operation, we imply a basic arithmetic operation that is supported by the computational engine. In the compression literature, the term MIPS (millions of instructions per second) is sometimes used. This

is specific to a computational engine's architecture; thus, in this text we refer to coding complexity in terms of MOPS. In some applications, such as portable devices, coding complexity may be characterised by the power requirements of a hardware implementation.

##### 3.1.4 Coding Delay

A complex compression process often leads to increased coding delays at the encoder and the decoder. Coding delays can be alleviated by increasing the processing power of the computational engine; however, this may be impractical in environments where there is a power constraint or when the underlying computational engine cannot be improved. Furthermore, in many applications, coding delays have to be constrained; for example, in interactive communications. The need to constrain the coding delay often forces the compression system designer to use a less sophisticated algorithm for the compression processes. From this discussion, it can be concluded that these trade-offs in coding complexity, delay, and efficiency are usually limited to a small set of choices along these axes. In a subsequent section, we will briefly describe the trade-offs within the context of specific lossless compression methods.

##### 3.1.5 Lossy Compression

The majority of the applications in image or video data processing do not require that the reconstructed data and the original data are identical in value. Thus, some amount of loss is permitted in the reconstructed data.

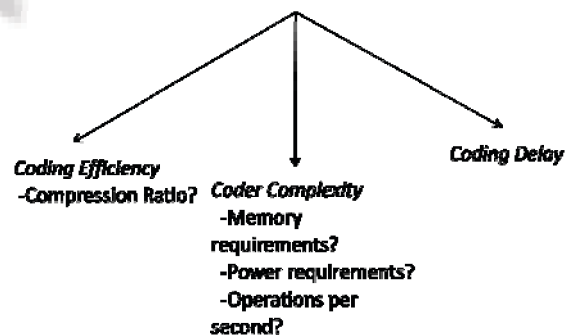


Figure 1.2: Trade-offs in lossless compression.

A compression process that results in an imperfect reconstruction is referred to as a lossy compression process. This compression process is irreversible. In practice, most irreversible compression processes degrade rapidly the signal quality when they are repeatedly applied on previously decompressed data. The choice of a specific lossy compression method involves trade-offs along the four dimensions shown in Figure 1.3. Due to the additional degree of freedom, namely, in the signal quality, a lossy compression process can yield higher compression ratios than a lossless compression scheme.

**Signal Quality:** This term is often used to characterise the signal at the output of the decoder. There is no universally accepted measure for signal quality. One measure that is often cited is the signal to noise ratio  $SNR$ , which can be expressed as

$$SNR = 10 \log_{10} \frac{\text{encoder input signal energy}}{\text{noise signal energy}}$$

The noise signal energy is defined as the energy measured for a hypothetical signal that is the difference between the encoder input signal and the decoder output signal. Note that, *SNR* as defined here is given in decibels (dB). In the case of images or video, *PSNR* (peak signal-to-noise ratio) is used instead of *SNR*. The calculations are essentially the same as in the case of *SNR*, however, in the numerator, instead of using the encoder input signal one uses a hypothetical signal with a signal strength of 255 (the maximum decimal value of an unsigned 8-bit number, such as in a pixel).

High *SNR* or *PSNR* values do not always correspond to signals with perceptually high quality. Another measure of signal quality is the mean opinion score, where the performance of a compression process is characterised by the subjective quality of the decoded signal. For instance, a five point scale such as *very annoying*, *annoying*, *slightly annoying*, *perceptible but not annoying*, and *imperceptible* might be used to characterise the impairments in the decoder output.

In either lossless or lossy compression schemes, the quality of the input data affects the compression ratio. For instance, acquisition noise, data sampling timing errors, and even the analogue-to-digital conversion process affects the signal quality and reduces the spatial and temporal correlation. Some compression schemes are quite sensitive to the loss in correlation and may yield significantly worse compression in the presence of noise.

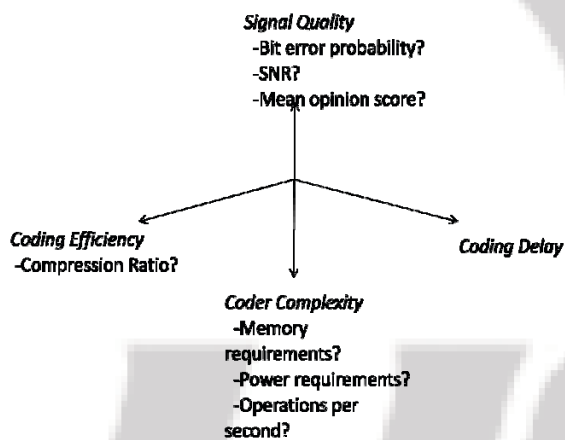


Figure 1.3: Trade-offs in lossy compression.

#### 4. Issues in Compression Method Selection

While choosing a specific compression method, the following issues are to be considered.

- Lossless or lossy. This is usually dictated by the coding efficiency requirements.
- Coding efficiency. Even in a lossy compression process, the desirable coding efficiency might not be achievable. This is especially the case when there are specific constraints on output signal quality.
- Variability in coding efficiency. In some applications, large variations in coding efficiency among different data sets may not be acceptable.

- Resilience to transmission errors. Some compression methods are more robust to transmission errors than others. If retransmissions are not permitted, then this requirement may impact on the overall encoder- decoder design.
- Complexity trade-offs. In most implementations, it is important to keep the overall encoder-decoder complexity low. However, certain applications may require only a low decoding complexity.
- Nature of degradations in decoder output. Lossy compression methods introduce artifacts in the decoded signal. The nature of artifacts depends on the compression method that is employed. The degree to which these artifacts are judged also varies from application to application. In communication systems, there is often an interplay between the transmission errors and the coding artifacts introduced by the coder. Thus, it is important to consider all types of error in a system design.
- Data representation. In many applications, there is a need to support two decoding phases. In the first phase, decoding is performed to derive an intelligible signal; this is the case in data browsing. In the second phase, decoding is performed to derive a higher quality signal. One can generalise this notion to suggest that some applications require a hierarchical representation of the data. In the compression context, we refer to such compression schemes as scalable compression methods. The notion of scalability has been adopted in the compression standards.
- Multiple usage of the encoding-decoding random. In many applications, such as video editing, there is a need to perform multiple encode-decode operations using results from a previous encode-decode operation. This is not an issue for lossless compression; however, for lossy schemes, resilience to multiple encoding-decoding cycles is essential.
- Interplay with other data modalities, such as audio and video. In a system where several data modalities have to be supported, the compression methods for each modality should have some common elements. For instance, in an interactive videophone system, the audio compression method should have a frame structure that is consistent with the video frame structure. Otherwise, there will be unnecessary requirements on buffers at the decoder and a reduced tolerance to timing errors.
- Interworking with other systems. In a mass-market environment, there will be multiple data modalities and multiple compression systems. In such an environment, transcoding from one compression method to another may be needed. For instance, video editing might be done on a frame by frame basis; hence, a compression method that does not exploit temporal redundancies might be used here. After video editing, there might be a need to broadcast this video. In this case, temporal redundancies can be exploited to achieve a higher coding efficiency. In such a scenario, it is important to select compression methods that support transcoding from one compressed stream format to another. Interworking is important in many communications environments as well.

#### 5. Work Elements / Methodology

There are many methods of lossless compression which are discussed earlier sections. By using this research work both

colour and gray scale images can be processed and their respective high quality high resolution images can be obtained. In terms of efficiency, this project is much superior to other methods of image compression and retrieval in the sense that this project produces effective PSNR and Normalized Cross Correlation (NCC). In this project, care is taken to register the input image without any loss. But as there is no integration mechanism involved for frame by frame storage, only steady images can be compressed and their high resolution outputs can be produced. By introducing an integration mechanism of frame by frame storage of the processed input images, we can extend the same concept of first compressing and retrieving the same on a higher resolution to even video images. If the same concept of first compressing and retrieving on a high resolution is applied to video images, we can save large memory spaces, due to which the videos can be downloaded as uploaded very fastly. Apart from fast access of the large video file, less storage memory is required so that many such files can be stored in a low memory space.

The coding of this research work will be done using Matlab Software. The high resolution input image is compressed to a low resolution image using SPIHT Codes. The compressed low resolution image is to be scaled. In other words, a scaling factor is selected and a new high resolution grid is created which is scaling factor times the dimensions of the low resolution grid. After the high resolution grid is created, now we should determine the new pixel values of each pixel in the high resolution grid. This is done by interpolation i.e. the known values are assigned directly and the unknown values of the pixels are determined by knowing the shift and rotate angles whose relations are explained in the coming sections and applying these shift and rotate angles to the known pixel values. Finally, all the pixel values of the high resolution grid are determined and stored to achieve the high resolution image with superior image quality and low memory occupancy.

- High resolution images such as Medical images are very sensitive to losses as the details are critical in terms of diagnosis and medical observation. Hence conventional image compression techniques are avoided in medical images. Medical Images need compression in such a way that medically relevant information (called ROI or region of interest) suffers minimum loss.
- A variable bit stream coding is adopted for ROI image compression. A ROI coding is simply an image compression technique where different parts of the images are encoded at different rates, therefore having different compression ratio and PSNR. In a medical image, the area of the image over which the information is present is called ROI. In medical image compression scheme, a ROI can be determined by manual outlining or by segmentation technique. So the approach is to divide an image into regions and then apply encoding with different rates over transformed data of those images. So while encoding ROI part, quantization will consider more distinct levels where as non ROI part should be encoded by considering lesser number of quantization level.
- The quantized values with the help of an encoding technique like entropy coding, Huffman coding, zero tree coding, SPIHT and so on. Quantization requires image

values to be unique and need to remove the sparse information. Therefore representing the image in the transformed domain is important as against spatial domain as the significance of the pixels in spatial domain are not known and therefore assigning them bits is difficult. Most widely used transformation for the image is wavelet transform.

- A better choice is to first scale down the image resolution to an acceptable level (say 256x256), Apply compression and store or transmits. At the decoder, the image must be uncompressed and then should be mapped to a high resolution plane (1024x1024) using interpolation technique using Papoulis-Gerchberg method.

## 6. Expected Results

Experiments will be performed on various images capture from mobile phones and digital camera and compare PSNR of low resolution image and high resolution image. In the new technique a original image is converted in to low resolution then quantization and SPIHT encoding will be done after then decoding of image will be done at receiver side. Techniques such as eleven iteration technique for decompression of image to original image. A new method to increase the PSNR value at this stage may be used. A suitable data set w. A multi level compression technique any be developed for better results.

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