# Experimental Measurement of Viscosity of N-Octane at Elevated Pressure and Temperature 

Dr. Jamuna Prasad<br>Associate Professor, Department of Physics, M.M.H College, Ghaziabad, Uttar Pradesh, India


#### Abstract

We have measured the viscosity of normal octane at temperature $30^{\circ} \mathrm{C}, 50^{\circ} \mathrm{C}, 75^{\circ} \mathrm{C}$, and $100^{\circ} \mathrm{Catpressure}$ up to 5.5 kbar by using the rolling-ball viscometer. The estimated accuracy in the viscosity data is $\pm 1$ percent. The experimental data obtained have been compared with values reported by other authors in the literature and found to be in good agreement. The results for pressure variation are represented by an empirical relation. We have also checked upto 4 kbar the validity of some observations made by Kiran and Senregarding the relationship between viscosity and density of n-octane.


Keywords: Viscosity, Rolling-ball Viscometer, Density, Pressure, Temperature, n-Octane

## 1. Introduction

A study of variation of viscosity of liquids as a function of pressure and temperature has considerable importance both for understanding of the fundamental problem of the liquid state and for ever increasing engineering application. The effect of pressure and temperature on the viscosity of liquids is strongly dependent on molecular structure which, in turn, determines properties such as specific volume, phase transition, dielectric relaxation etc. It is observed mostly for liquids that a pressure change of a few kbar produces several orders of magnitude variation in viscosity. This type of observed behavior could be explained by any theory of viscosity of liquids.

The effect of temperature and pressure on the viscosity of $n$ paraffins has been investigated earlier also by several authors from time to time using diverse methods. The earliest detailed investigation in this connection is due to Bridgman [1]. He measured the viscosity of numerous liquids including four n-paraffins at pressures up to 10 kbar by the falling weight method (estimated error 2 to $5 \%$ ). Hogenboom etal [2] investigated the viscosity of some liquids as a function of temperature and pressure including three n-paraffins by the rolling ball method for pressures up to 3.6 k bar (error $+2 \%$ ). Dymond etal [3-5] investigated extensively the viscosity behavior of several pure hydrocarbons including n-octane for pressures up to 5 k bar in the temperature range 25 to $100^{\circ} \mathrm{C}$ (error $+2 \%$ ). Using a vibrating crystal, Kashiwagi and Makita [6] measured the viscosity of n -hexane, n -heptane, n -octane, n -decane and n dodecane in the temperature range 25 to $75^{\circ} \mathrm{C}$ but pressure range limited to 1 kbar. Kiran and Sen [7] have reported their viscosity results for some n-paraffins over a wide temperature range lying between 37 and $177^{\circ} \mathrm{C}$ but their maximum pressure does not exceed 0.7 k bar. Hseen O . Baled etal [8] determined experimentally viscosity of noctane and isooctane at pressures between 4 and 242 MPa
and temperatures between 303 K and 523 K . Recently, A. Darysafar and Khalil Shahbzi [9] gave a model to predict the dynamic viscosity of the $n$-alkanes as a function of pressure, temperature and n -alkane's molecular weight.

## 2. Experimental and Materials

In this work viscosity measurements have been carried out for n-octane by using the rolling-ball viscometer. The pressure range in our experiments is up to 5.5 kbar . The measurements are carried out at temperatures $30^{\circ} \mathrm{C}, 50^{\circ} \mathrm{C} 75$ and $100^{\circ} \mathrm{C}$. Procedure and other details used in this measurement have been described in [10]. The normal octane used in this study is obtained from E. Merc (Germany), who claim purity of 99.5 percent.

## 3. Results and Discussion

Relative viscosity $\eta_{\mathrm{r}}$ (the ratio of viscosity at elevated pressure to the viscosity at atmospheric pressure) at each temperature is determined in the pressure range up to 5.5 kbar at temperatures $30^{\circ} \mathrm{C}, 50^{\circ} \mathrm{C}, 75^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$ using relation

$$
\begin{equation*}
\eta=(\mathrm{K} / \mathrm{L})\left(\mathbf{p}_{\mathrm{b}}-\boldsymbol{\rho}\right) \mathrm{t} \operatorname{Sin} \boldsymbol{\theta} \tag{1}
\end{equation*}
$$

Where $\eta$ is the coefficient of viscosity, $K$ is the calibration constant, $\boldsymbol{\theta}$ is the inclination of the rolling plane with the horizontal, $\boldsymbol{\rho}_{\mathrm{b}}$ and $\boldsymbol{\rho}$ the density of the material of the ball and the liquid respectively and 't is the rolling time of the ball for covering the distance L in the tube. The experimental results of our measurements and calculated values (from eq.2) of relative viscosity are given in Table 1. In Fig.1, we plotted $\log _{10} \boldsymbol{\eta}_{\mathrm{r}}$ (logarithm base 10 of relative viscosity) versus pressure at different temperatures. It is clear from the figure that as expected, the viscosity increases with pressure and decreases with temperature.

Table 1: Relative viscosity ( $\eta \mathrm{r}$ ) of n-Octane as a function of pressure and temperature

| $\mathrm{P}($ bar $)$ | $\left(30^{\circ} \mathrm{C}\right) \eta_{\mathrm{r}}$ |  | $\mathrm{P}($ bar $)$ | $\left(50^{\circ} \mathrm{C}\right) \eta_{\mathrm{r}}$ |  | $\mathrm{P}($ bar $)$ | $\left(75^{\circ} \mathrm{C}\right) \eta_{\mathrm{r}}$ |  | $\mathrm{P}(\mathrm{bar})$ | $\left(100^{\circ} \mathrm{C}\right) \eta_{\mathrm{r}}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Exptl | Cal |  | Exptl | Cal |  | Exptl | Cal |  | Exptl | Cal |
| 1 | 1 | 0.997 | 1 | 1 | 1.002 | 1 | 1 | 1.002 | 1 | 1 | 1.005 |
| 412 | 1.446 | 1.454 | 415 | 1.496 | 1.487 | 475 | 1.575 | 1.569 | 396 | 1.523 | 1.504 |
| 815 | 1.993 | 1.993 | 798 | 2.011 | 2.021 | 751 | 1.955 | 1.951 | 753 | 1.996 | 2.007 |


| 1039 | 2.4 | 2.336 | 1213 | 2.69 | 2.689 | 1032 | 2.377 | 2.375 | 1037 | 2.421 | 2.431 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1452 | 3.061 | 3.057 | 1568 | 3.328 | 3.335 | 1423 | 2.997 | 3.018 | 1391 | 2.978 | 2.985 |
| 1880 | 3.955 | 3.951 | 2009 | 4.27 | 4.247 | 1718 | 3.544 | 3.546 | 1789 | 3.639 | 3.651 |
| 2040 | 4.337 | 4.332 | 2535 | 5.526 | 5.54 | 2035 | 4.156 | 4.159 | 2163 | 4.315 | 4.339 |
| 2541 | 5.731 | 5.737 | 3012 | 6.947 | 6.971 | 2526 | 5.235 | 5.225 | 2508 | 4.982 | 5.048 |
| 3029 | 7.478 | 7.496 | 3521 | 8.893 | 8.857 | 3033 | 6.552 | 6.523 | 3025 | 6.329 | 6.286 |
| 3540 | 9.852 | 9.873 | 4004 | 11.055 | 11.061 | 3515 | 7.99 | 8.001 | 3521 | 7.628 | 7.674 |
| 4060 | 13.017 | 12.951 | 4512 | 13.839 | 13.842 | 4011 | 9.81 | 9.822 | 4045 | 9.244 | 9.222 |
| 4602 | 16.792 | 16.823 | 5023 | 16.984 | 17.014 | 4529 | 12.012 | 12.045 | 4601 | 10.507 | 10.51 |
|  |  |  | 5316 | 18.86 | 18.845 | 5031 | 14.433 | 14.398 |  |  |  |
|  |  |  |  |  |  | 5515 | 16.547 | 16.554 |  |  |  |



Figure 1: Relative viscosity ( $\eta \mathrm{r}$ ) of n -Octane as a function of pressure and temperature

At each temperature our results could be fitted to polynomial equation

$$
\log _{10} \eta_{\mathrm{F}}=\sum_{\mathrm{i}=0}^{\mathrm{n}} \mathrm{a}_{\mathrm{i}} \mathrm{p}^{\mathrm{i}}
$$

Where pressure P is measured in bar. The values of the coefficients in each case are given in Table 2. A fourth order polynomial is found to give a good representative of our results within the estimated accuracy of $\pm 1$ percent. The estimated error in the present viscosity data is $\pm 1$ percent, which is equal or less than reported by earlier authors.

Table 2: Values of the coefficients in eq 2

| Temp $\left({ }^{\circ} \mathrm{C}\right)$ | $\mathrm{a}_{0} \times 10^{3}$ | $\mathrm{a}_{1} \times 10^{4}$ | $\mathrm{a}_{2} \times 10^{7}$ | $\mathrm{a}_{3} \times 10^{11}$ | $\mathrm{a}_{4} \times 10^{15}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 1.1149 | 4.3161 | -0.91965 | 1.993 | -1.6811 |
| 50 | 0.42655 | 4.5417 | -1.051 | 2.0247 | -1.5165 |
| 75 | 1.0838 | 4.585 | -1.1296 | 2.1301 | -1.5654 |
| 100 | 2.0219 | 5.0117 | -1.6249 | 3.8477 | -3.5573 |

We show some illustrative comparison of our results with other author's data at $50^{\circ} \mathrm{C}$ in Fig.2. In this figure, our smoothed values from Eq. 2 are shown in a yellow line curve while the results of other authors in the form reported
by them are shown by a black line (Dickinson), redline (Dymond) and green line (Kashiwagi) curve.

It is clear from the figure that the limited pressure results of Kashiwagi and Makita [6] up to 1 kbar are in good agreement with ours while those of Dymond etal [5] and Dickinson [11] show respectively progressively increasing negative and positive deviations. In the former case the maximum deviation is $2 \%$ while in the latter case it is $3 \%$. Details of comparisons in later two cases are given quantitatively in Table 3

Table 3: Quantitative comparison between present results, Dickinson and Dymond's data at $50^{\circ} \mathrm{C}$

| P (bar) | This work | Dickinson | P (bar) | This work | Dymond etal |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 | 1 | 1 |
| 510 | 1.612 | 1.637 | 524 | 1.631 | 1.612 |
| 1045 | 2.408 | 2.402 | 999 | 2.333 | 2.271 |
| 1780 | 3.757 | 3.716 | 2002 | 4.232 | 4.116 |
| 2565 | 5.623 | 5.629 | 3020 | 6.998 | 6.858 |
| 3380 | 8.293 | 8.321 | 4080 | 11.491 | 11.147 |
| 4035 | 11.22 | 11.18 | 5055 | 17.209 | 16.788 |



Figure 2: A comparison between present results, Kashiwagi, Dickinson and Dymond' s data at $50^{\circ} \mathrm{C}$

Lastly, we also analyzed our viscosity data using a threeparameter relation given by Kiran and Sen [7] of the form

$$
\begin{equation*}
\eta=B_{1} \exp \left(B_{2} \times \boldsymbol{\rho}\right)+B_{3} \tag{3}
\end{equation*}
$$

Where $B_{1}, B_{2}, B_{3}$ are parameters to be determined from the data. Evidently, according to Kiran and Sen, one set $B_{1}, B_{2}$, $\mathrm{B}_{3}$ values would be needed for each n-paraffin data below 0.7 k bar. We have, however, tried Eq. (3) for the representation of viscosity data for pressures up to 4 kbar. This, however, makes it necessary to $\mathrm{B}_{1}, \mathrm{~B}_{2}, \mathrm{~B}_{3}$ to be temperature dependent. The values of these parameters are given in Table 4. Average modulus of the deviation (M.D) of the values calculated from the Eq. (3) using these parameter values from our smoothed experimental values are given in Table 4. Our analysis shows that with our parameter values, MD is less than 2.0 percent.

Table 4: Values of the coefficients in eq 3

| Temp $\left({ }^{\circ} \mathrm{C}\right)$ | $\mathrm{B}_{1} \times 10^{11}$ | $\mathrm{~B}_{2} \times 10^{2}$ | $\mathrm{~B} 3(\mathrm{mPa} . \mathrm{S})$ | $\mathrm{MD}(\%)$ |
| :---: | :---: | :---: | :---: | :---: |
| 30 | 1.1878 | 2.3684 | 0.327 | 2 |
| 50 | 21.338 | 2.0084 | 0.214 | 0.9 |
| 75 | 119.32 | 1.7777 | 0.164 | 1.4 |
| 100 | 378.01 | 1.6216 | 0.129 | 1.6 |

## 4. Conclusion

The present study contributed to a reliable experimental database for n -octane at temperatures $30^{\circ} \mathrm{C}, 50^{\circ} \mathrm{C}, 75^{\circ} \mathrm{C}$, and $100^{\circ} \mathrm{C}$ and pressures range up to 5.5 kbar . It is evident from illustrations that as expected, the viscosity increases with pressure and decreases with temperature. Based on the measured data, empirical relation is developed which is found to give a good representative of our results within the estimated accuracy of $\pm 1$ percent. The estimated error in the present viscosity data is $\pm 1$ percent. A comparison shows that our data is in good agreement with available literature data. Average modulus of the deviation (M.D) of the values calculated from the Eq. (3) using these parameter
values from our smoothed experimental values are reported. Our analysis shows that with our parameter values, MD is less than 2.0 percent. It is hoped that this data could be useful to physicists, chemists and engineers for scientific and practical applications.

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